#### Natural Language Processing

WBAI059-05



faculty of science and engineering

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Lecture 2: n-gram Language Models

## Today's lecture plan

- What is N-gram Language model
- Text Generating from a language model
- Evaluating a language model (perplexity)

Recommended reading: JM3 3.1-3.5

CHAPTER 3

N-gram Language Models

What is an n-gram language model?

#### Language models and n-gram

- Models that assign probabilities to sequences of words (n-gram) are called language models or LMs.
  - An n-gram is a sequence of n words

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Example: "Please turn your homework": a 2-gram (bigram) will be "please turn", "turn your", "your homework"
```

 Language can be defined as a model that assigns probabilities to sentences

### (Probabilistic) Language Modeling

• Goal: compute the probability of a sentence or sequence of words:

```
P(W) = P(w_1, w_2, w_3, w_4, w_5...w_n) \rightarrow Joint probability
```

- Related task: probability of an upcoming word:  $P(w_5|w_1,w_2,w_3,w_4) \rightarrow$  Conditional probability
- A model that computes either of these:

```
P(W) or P(w_n|w_1,w_2...w_{n-1}) is called a language model.
```

#### What is a language model?

- Language Modeling is the task of predicting the probability of a sentence or what word comes next.
- More formally: given a sequence of words  $w_{1'}$   $w_{2}$ ..., $w_{t}$  compute the probability distribution of the next word  $w_{t+1}$ .

$$P(w_{(t+1)}|w_1,w_2,w_3,...,w_t)$$

- Where w<sub>(t+1)</sub> can be any word in the vocabulary
- You can also think of a Language Model as a system that assigns probability to a piece of text.

# How to compute P(W)

How to compute this joint probability:

P(its, water, is, so, transparent, that)

Intuition: let's rely on the Chain Rule of Probability

#### Reminder: The Chain Rule

Recall the definition of conditional probabilities

$$P(A \mid B) = P(A,B)/P(B)$$
 Rewriting:  $P(A,B) = P(B)P(A \mid B)$ 

• More variables:

$$P(A,B,C,D) = P(A)P(B|A)P(C|A,B)P(D|A,B,C)$$

The Chain Rule in General

$$P(x_1,x_2,x_3,...,x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1,x_2)...P(x_n|x_1,...,x_{n-1})$$

#### Using Chain rule

• For example, if we have some text  $w_1, \ldots, w_n$  then the probability of this text (according to the Language Model) is:

Conditional probability:  $p(w_{2} \mid w_{1}), \forall w \in V$   $P(w_{1}, w_{2}, w_{3}, ..., w_{n}) = P(w_{1})P(w_{2} \mid w_{1})P(w_{3} \mid w_{1}, w_{2})...P(w_{n} \mid w_{1}, ..., w_{n-1})$ 

$$P(w_1 w_2 \dots w_n) = \prod_i P(w_i \mid w_1 w_2 \dots w_{i-1})$$

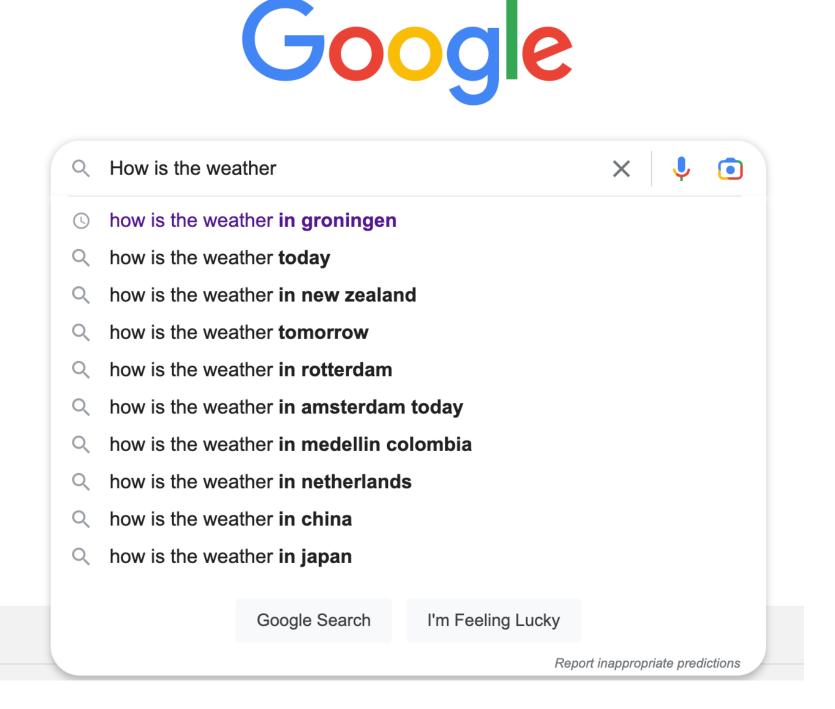
This is what our LM provides

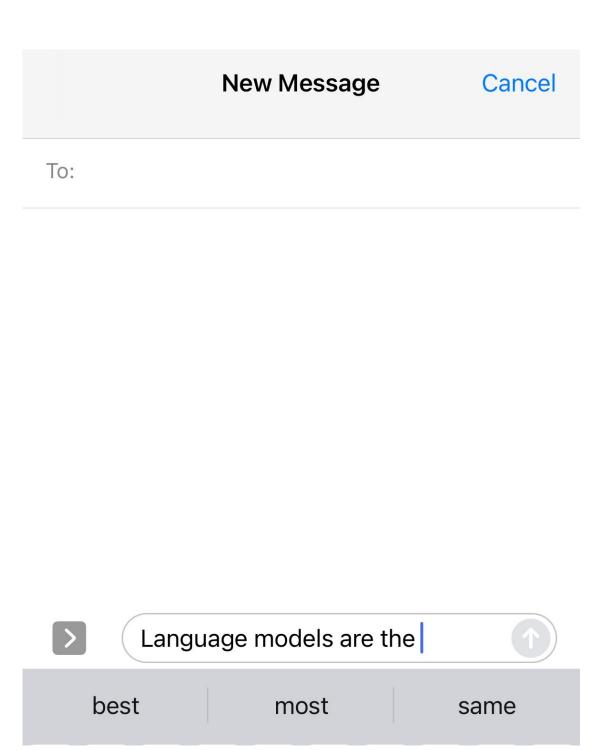
### Example

Example Sentence: "the cat sat on the mat"

P(the cat sat on the mat) = P(the) \* P(cat | the) \* P(sat | the cat) \* P(on | the cat sat) \* P(the | the cat sat on) \* P(mat | the cat sat on the)

### Language models are everywhere





#### Estimating probabilities

One way to estimate this probability is from relative frequency counts



$$P(\text{sat} | \text{the cat}) = \frac{\text{count}(\text{the cat sat})}{\text{count}(\text{the cat sat on})}$$

$$P(\text{on} | \text{the cat sat}) = \frac{\text{count}(\text{the cat sat on})}{\text{count}(\text{the cat sat})}$$

- Assume we have a vocabulary of size V, how many sequences of length n do we have?
  - With a vocabulary of size V, # sequences of length  $n = V^n$
- Typical English vocabulary ~ 40k words

### Markov assumption

- Use only the recent past to predict the next word
- Reduces the number of estimated parameters in exchange for modeling capacity.
- 1st order

 $P(\text{mat/the cat sat on the}) \approx P(\text{mat/the})$ 

2nd order

 $P(\text{mat/the cat sat on the}) \approx P(\text{mat/on the})$ 



#### n-gram Language Models- Markov assumption

• First, we make a Markov assumption:  $w_i$  depends only on the preceding n-1 words: Consider only the last k words (or less) for context

$$P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-k} ... w_{i-1})$$

which implies the probability of a sequence is:

$$P(w_1 w_2 ... w_n) \approx \prod_{i} P(w_i | w_{i-k} ... w_{i-1})$$

- Question: How do we get these n-gram and (k-1)-gram probabilities?
- Answer: By counting them in some large corpus of text!

# n-gram Language Models

- Definition: A n-gram is a chunk of n consecutive words.
  - unigrams: "the", "students", "opened", "their"
  - bigrams: "the students", "students opened", "opened their"
  - trigrams: "the students opened", "students opened their"
  - 4-grams: "the students opened their"
- Idea: Collect statistics about how frequent different n-grams are and use these to predict next word.

#### n-gram language models

• Unigram: In the Unigram model, we estimate the probability of a whole sequence of words by the product of probabilities of individual words.

$$P(w_1, w_2,...w_n) \approx \prod_{i=1}^n P(wi)$$
 E.g.  $P(the) P(cat) P(sat)$ 

- Bigram: we estimate the probability of a word, given the entire prefix from the beginning to the previous word.
- We condition on a single previous word

$$P(w_i \mid w_1, w_2,...w_{i-1}) \approx P(w_i \mid w_{i-1}) \approx \prod_{i=1}^n P(w_i \mid w_{i-1})$$
  
E.g.  $P(\text{the}) P(\text{cat} \mid \text{the}) P(\text{sat} \mid \text{cat})$ 

Larger the n, more accurate and better the language model (but also higher costs)

### N-gram models

- We can extend to trigrams, 4-grams, 5-grams
- In general this is an insufficient model of language
  - because language has long-distance dependencies:

"The computer which I had just put into the machine room on the fifth floor crashed."

• But we can often get away with N-gram models

## Estimating bigram probabilities

How do we estimate these n-gram probabilities?

$$P(w_{i} | w_{i-1}) = \frac{count(w_{i-1}, w_{i})}{count(w_{i-1})}$$

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$

# n-gram Language Models: Example

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})} \quad \begin{array}{l} < \text{s} > \text{l am Sam } < / \text{s} > \\ < \text{s} > \text{Sam I am } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \text{I do not like green eggs and ham } < / \text{s} > \\ < \text{s} > \\ < \text{log not like g$$

$$P(I | ~~) = \frac{2}{3} = .67~~$$
  $P(Sam | ~~) = \frac{1}{3} = .33~~$   $P(am | I) = \frac{2}{3} = .67$   $P( | Sam) = \frac{1}{2} = 0.5$   $P(Sam | am) = \frac{1}{2} = .5$   $P(do | I) = \frac{1}{3} = .33$ 

#### n-gram Language Models: Example

Suppose we are learning a 4-gram Language Model.

$$P(\boldsymbol{w}|\text{students opened their}) = \frac{\text{count}(\text{students opened their }\boldsymbol{w})}{\text{count}(\text{students opened their})}$$

For example, suppose that in the corpus:

- "students opened their" occurred 1000 times
- "students opened their books" occurred 400 times
  - $\rightarrow$  P(books | students opened their) = 0.4
- "students opened their exams" occurred 100 times
  - → P(exams | students opened their) = 0.1

Should we have discarded the "proctor" context?

#### Practical Issues

- We do everything in log space
  - Avoid underflow
  - (also adding is faster than multiplying)

$$\log(p_1 \times p_2 \times p_3 \times p_4) = \log p_1 + \log p_2 + \log p_3 + \log p_4$$

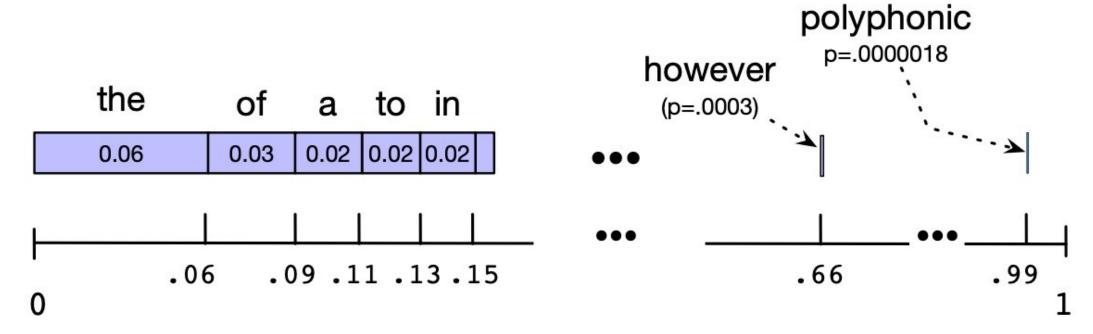
# Generating from a language model

### Generating from a language model

Given a bigram language model, how to generate a sequence?

$$P(x^1, x^2,...x^t) = \prod_{i=1}^t P(x^i | x^i - 1)$$

- Generate the first word  $x_1 \sim P(x)$
- Generate the second word  $x^2 \sim P(x \mid x^1)$
- Generate the third word  $x^3 \sim P(x \mid x^2)$



## Generating from a language model

• Given a bigram language model, how to generate a sequence?

$$P(x^1, x^2,...x^t) = \prod_{i=1}^t P(x^i | x^i - x^i - 1)$$

- Generate the first word  $x_1 \sim P(x)$
- Generate the second word  $x^2 \sim P(x \mid x^1)$
- Generate the third word  $x^3 \sim P(x \mid x^1, x^2)$
- Generate the fourth word  $x^4 \sim P(x \mid x^2, x^3)$

#### n-gram Language Models in practice

You can build a simple trigram Language Model over a
 1.7 million word corpus (Reuters) in a few seconds on your laptop\*

today the \_\_\_\_\_

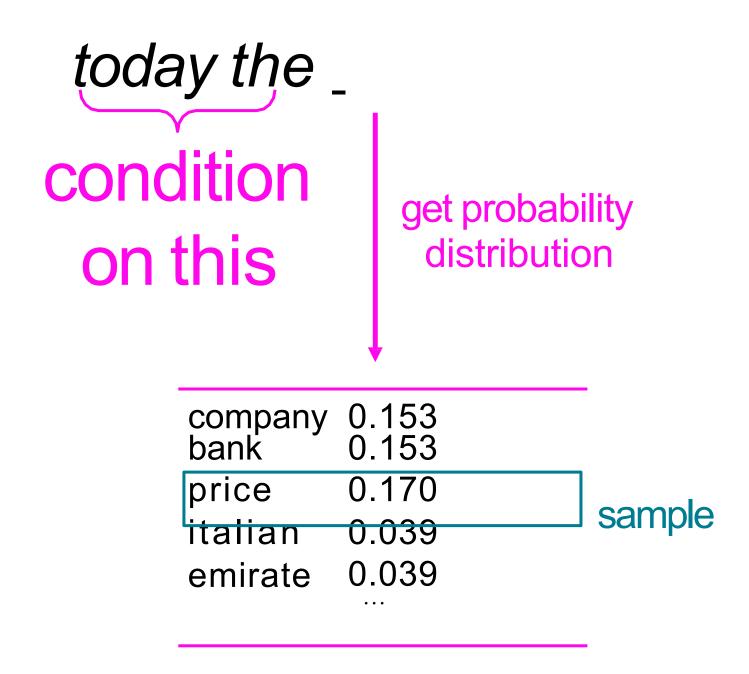
Business and financial news

get probability distribution

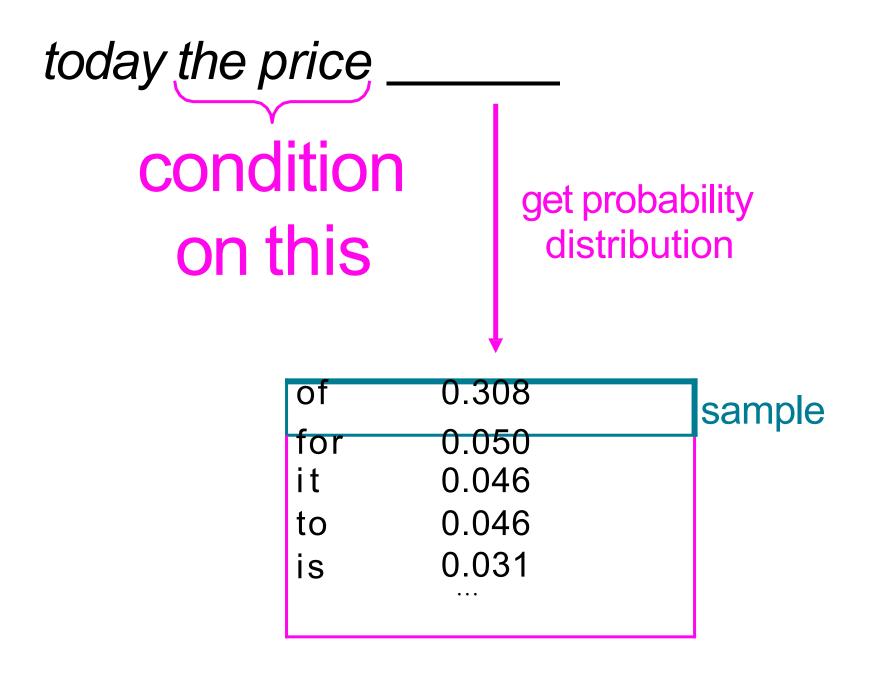
```
company 0.153
bank 0.153
price 0.170
italian 0.039
emirate 0.039
```

<sup>\*</sup> Try for yourself: <a href="https://nlpforhackers.io/language-models/">https://nlpforhackers.io/language-models/</a>

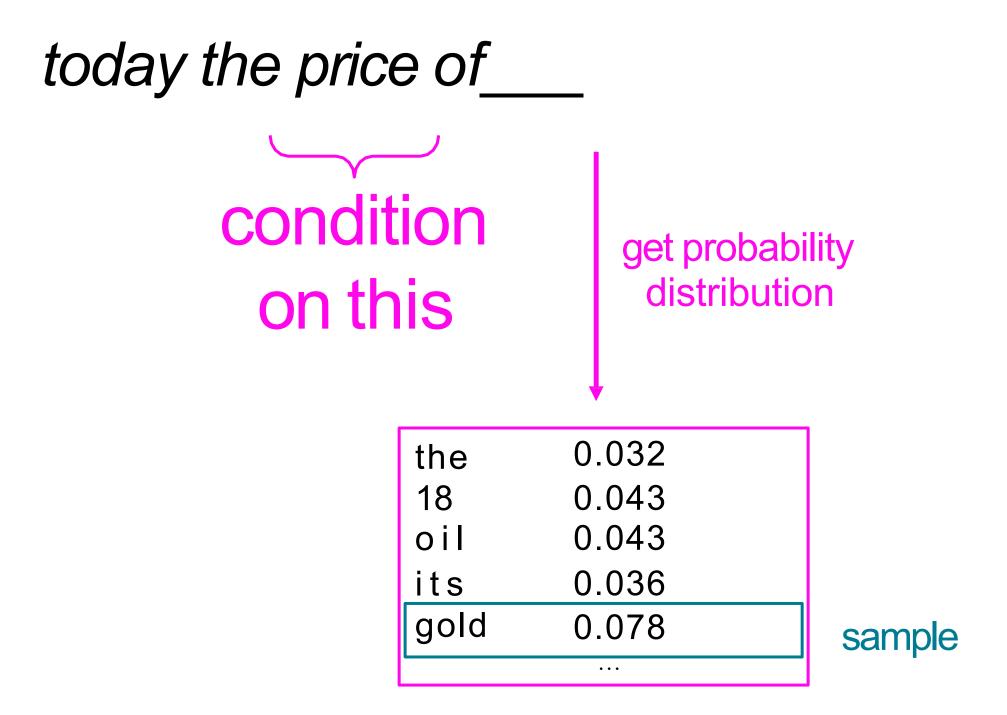
You can also use a Language Model to generate text



You can also use a Language Model to generate text



You can also use a Language Model to generate text



You can also use a Language Model to generate text

today the price of gold per ton, while production of shoe lasts and shoe industry, the bank intervened just after it considered and rejected an imf demand to rebuild depleted european stocks, sept 30 end primary 76 cts a share.

Surprisingly grammatical!

...but **incoherent.** We need to consider more than three words at a time if we want to model language well.

But increasing *n* worsens sparsity problem, and increases model size...

# Evaluating a language model

#### Evaluation: How good is our model?

- Does our language model prefer good sentences to bad ones?
  - Assign higher probability to "real" or "frequently observed" sentences
    - Than "ungrammatical" or "rarely observed" sentences?
- We train parameters of our model on a training set.
- We test the model's performance on data we haven't seen.
  - A test set is an unseen dataset that is different from our training set, totally unused.
  - An evaluation metric tells us how well our model does on the test set.

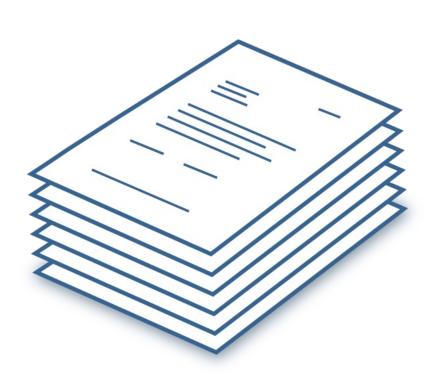
### Extrinsic evaluation of N-gram models

- Best evaluation for comparing models A and B
  - Put each model in a task
    - spelling corrector, speech recognizer, MT system
  - Run the task, get an accuracy for A and for B
    - How many misspelled words corrected properly
    - How many words translated correctly
  - Compare accuracy for A and B
- But Time-consuming; can take days or weeks

### Intrinsic evaluation of language models

#### Research process:

- Train parameters on a suitable training corpus
  - Assumption: observed sentences ~ good sentences
- Test on different, unseen corpus
  - If a language model assigns a higher probability to the test set, it is better
- Evaluation metric perplexity!
  - Measure of how well a LM predicts the next word



#### Evaluating Language Models

The standard evaluation metric for Language Models is perplexity.

$$\text{perplexity} = \prod_{t=1}^T \left( \frac{1}{P_{\text{LM}}(\boldsymbol{x}^{(t+1)}|\ \boldsymbol{x}^{(t)},\dots,\boldsymbol{x}^{(1)})} \right)^{1/T}$$
 Normalized by number of words

Inverse probability of corpus, according to Language Model

• This is equal to the exponential of the cross-entropy loss  $J(\theta)$ :

$$= \prod_{t=1}^{T} \left( \frac{1}{\hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)}} \right)^{1/T} = \exp \left( \frac{1}{T} \sum_{t=1}^{T} -\log \hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)} \right) = \exp(J(\theta))$$

Measure of model's uncertainty about next word : Lower perplexity is better!

# RNNs have greatly improved perplexity

*n*-gram model

Increasingly complex RNNs

Model	Perplexity
Interpolated Kneser-Ney 5-gram (Chelba et al., 2013)	67.6
RNN-1024 + MaxEnt 9-gram (Chelba et al., 2013)	51.3
RNN-2048 + BlackOut sampling (Ji et al., 2015)	68.3
Sparse Non-negative Matrix factorization (Shazeer et al., 2015)	52.9
LSTM-2048 (Jozefowicz et al., 2016)	43.7
2-layer LSTM-8192 (Jozefowicz et al., 2016)	30
Ours small (LSTM-2048)	43.9
Ours large (2-layer LSTM-2048)	39.8

Perplexity improves (lower is better)

Source: <a href="https://research.fb.com/building-an-efficient-neural-language-model-over-a-billion-words/">https://research.fb.com/building-an-efficient-neural-language-model-over-a-billion-words/</a>

# Why should we care about Language Modeling?

- Language Modeling is a benchmark task that helps us measure our progress on understanding language.
- Language Modeling is a subcomponent of many NLP tasks, especially those involving generating text or estimating the probability of text:
  - Predictive typing
  - Speech recognition
  - Handwriting recognition
  - Spelling/grammar correction
  - Authorship identification
  - Machine translation
  - Summarization
  - Dialogue
  - etc.

#### Sparsity Problems with n-gram Language Models

#### **Sparsity Problem 1**

Problem: What if "students opened their w" never occurred in data? Then w has probability 0!

(Partial) Solution: Add small  $\delta$  to the count for every  $w \in V$ . This is called *smoothing*.

 $P(\boldsymbol{w}|\text{students opened their}) = \frac{\text{count}(\text{students opened their }\boldsymbol{w})}{\text{count}(\text{students opened their})}$ 

#### Sparsity Problem 2

Problem: What if "students opened their" never occurred in data? Then we can't calculate probability for any w!

(Partial) Solution: Just condition on "opened their" instead. This is called backoff.

**Note:** Increasing *n* makes sparsity problems *worse*. Typically, we can't have *n* bigger than 5.

#### Storage Problems with n-gram Language Models

Storage: Need to store count for all *n*-grams you saw in the corpus.

$$P(\boldsymbol{w}|\text{students opened their}) = \frac{\text{count}(\text{students opened their }\boldsymbol{w})}{\text{count}(\text{students opened their})}$$

Increasing *n* or increasing corpus increases model size!



# Questions