

7.1: Aliasing due to Undersampling

This exercise covers the effects of aliasing due to sampling on signals reconstructed by bandlimited interpolation. If a continuous-time signal $x(t)$ is sampled every T seconds, then its samples form the discrete-time sequence $x[n] = x(nT)$. The Nyquist sampling theorem states that if $x(t)$ has bandwidth less than $\Omega_s = 2\pi/T$, i.e., $X(j\Omega) = 0$ for $|\Omega| > \Omega_s/2$, then $x(t)$ can be completely reconstructed from its samples $x(nT)$. The bandlimited interpolation or signal reconstruction is most easily visualized by first multiplying $x(t)$ by an impulse train

$$x_p(t) = \sum_{n=-\infty}^{\infty} x(nT)\delta(t - nT).$$

The signal $x(t)$ can be recovered from $x_p(t)$ by filtering $x_p(t)$ with an ideal lowpass filter with cutoff frequency $\Omega_s/2$. Define $x_r(t)$ to be the reconstructed signal given by lowpass filtering $x_p(t)$. If the bandwidth of $x(t)$ is greater than Ω_s , then the samples $x(nT)$ do not completely determine $x(t)$, and $x_r(t)$ will not generally be equal to $x(t)$. In the following problems, you will examine the effects of undersampling a pure sinusoid and a chirp signal.

Basic Problems

Consider the sinusoidal signal

$$x(t) = \sin(\Omega_0 t)$$

If $x(t)$ is sampled with frequency $\Omega_s = 2\pi/T$ rad/sec, then the discrete-time signal $x[n] = x(nT)$ is equal to

$$x[n] = \sin(\Omega_0 nT).$$

Assume the sampling frequency is fixed at $\Omega_s = 2\pi(8192)$ rad/sec.

7.1:Part A

(a). Assume $\Omega_0 = 2\pi(1000)$ rad/sec and define $T=1/8192$. Create the vector $n=[0:8191]$, so that $t = n * T$ contains the 8192 time samples of the interval $0 \leq t < 1$. Create a vector x which contains the samples of $x(t)$ at the time samples in t .

```
1 %Part 1: Project 7.1, parts (a)
2
3 Omega_0 = 2*pi*1000;
4 T= 1/8192;
5 n=0:8191;
6 t=n*T;
7 x = sin(Omega_0*t); % x(t)
```

Code 7.1-1: matlab script for Part A

7.1:Part B

(b). Display the first fifty samples of $x[n]$ versus n using stem. Display the first fifty samples of $x(t)$ versus the sampling times using plot. (use subplot to simultaneously display these two plots.)

```

1  %Part 2: Project 7.1, parts (b)
2
3  %Sampling frequency is Omega_s = 2*pi*8192
4  %Part A
5  Omega_0 = 2*pi*1000;
6  T= 1/8192;
7  n=0:8191;
8  t=n*T;
9  x = sin(Omega_0*t); % x(t)
10 x_discrete = sin(Omega_0*n*T); % x[n]
11
12 %Part B
13 figure(1)
14
15 subplot(211)
16 stem(n,x_discrete)%x[n]
17 xlim([0 49]); %first fifty samples
18 title('Project 7.1, Part(b)')
19 xlabel('time samples')
20 ylabel('x[t] = sin(\Omega_0 nT)')
21
22 subplot(212)
23 plot(n,x)
24 xlim([0 49]); %first fifty samples
25 xlabel('time samples')
26 ylabel('x(t) = sin(\Omega_0 t)')
27
28 if FINALPLOTS
29     print -deps proj71PartB.eps
30 end

```

Code 7.1-2: matlab script for Part B

Note that `plot(t,x)` displays a continuous-time signal given the samples in `x`, using straight lines to interpolate between sample values. While this interpolation is not generally equal to the bandlimited reconstruction which follows from the sampling theorem, it can often be a very good approximation.

To compute samples of the continuous-time Fourier transform of the bandlimited reconstruction $x_r(t)$, use the following function:

```
function [X,f] = ctfts(x,T) N=length(x); X = fftshift(fft(x,N))*(2*pi/N); f = linspace(-1,1-1/N,N)/(2*T);
```

This function uses `fft` to calculate the Fourier transform of the reconstructed signal. The M-file `ctfts.m` is provided in the Computer Explorations Toolbox, and should be placed in your MATLABPATH.

7.1:Part C

(c). Use `[X,f]=ctfts(x,T)` to calculate the continuous-time Fourier transform of the reconstructed signal $x_r(t)$. Plot the magnitude of `X` versus `f`. Is `X` nonzero at the proper frequency values? (Note that almost all the elements in `X` are nonzero, but most are small values due to numerical round-off errors.) Is the phase of `X` correct, assuming that the phase is equal to zero when `X` is nearly zero, I.E., nonzero only due to round-off error.

```

1  %Part 1: Project 7.1, parts (c)
2
3  %Part A
4  Omega_0 = 2*pi*1000;
5  T= 1/8192;

```

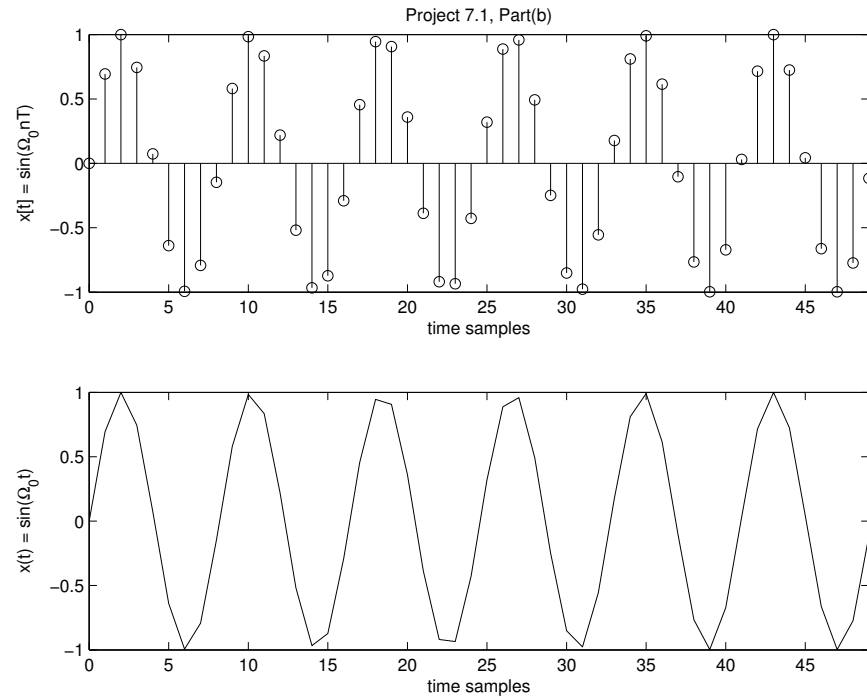


Figure 7.1-1: Output for 7.1 Part B

```

6  n=0:8191;
7  t=n*T;
8  x = sin(Omega_0*t); % x(t)
9
10 %Part C
11 [X,f]=ctfts(x,T);
12
13 figure(1)
14
15 plot(f,abs(X))
16 title('Project 7.1, Part(c)')
17 xlabel('time samples')
18 ylabel('x_r(t) (CTFT)')
19
20
21 if FINALPLOTS
22     print -deps proj71PartC.eps
23 end

```

Code 7.1-3: matlab script for Part C

Output:

Plot the magnitude of X versus f: see figure[!h] for the output

Is X nonzero at the proper frequency values?

Yes, the nonzero points were at 1000 and -1000 which correspond to $\Omega_0 = 2\pi(1000)$ where 1000 is the the bandlimit occurs.

Is the phase of X correct, assuming that the phase is equal to zero when X is nearly zero, I.E., nonzero only due to round-off error.

Yes, the phase of X is correct.

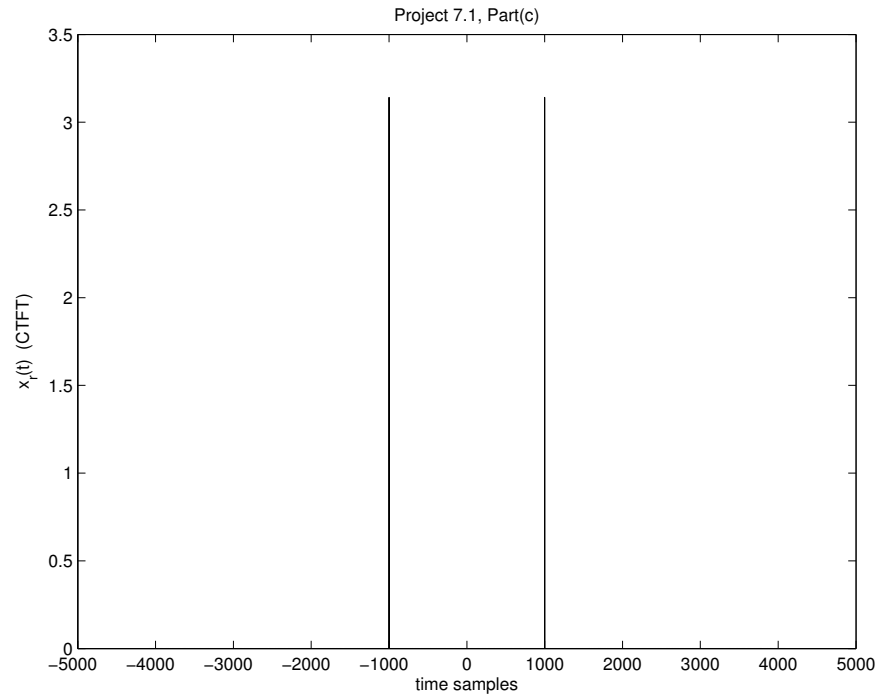


Figure 7.1-2: Output for 7.1 Part C

Intermediate Problems

you will now consider the effect of aliasing on the reconstructed signal $x_r(t)$.

7.1:Part D

(d). Repeat. Parts (a)-(c) for the sinusoidal frequencies $\Omega_0 = 2\pi(1500)$ and $2\pi(2000)$ rad/sec. Again, is the magnitude of X nonzero for the expected frequencies? Is the phase of X correct?

```

1  %Part 1: Project 7.1, parts (d)
2
3  %=====
4  %Repeat (a)-(c) for omega_0 = 2pi(1500)
5  %=====
6
7  Omega_0 = 2*pi*1500;
8  T= 1/8192;
9  n=0:8191;
10 t=n*T;
11 x = sin(Omega_0*t); % x(t)
12 x_discrete = sin(Omega_0*n*T); % x[n]
13
14
15 figure(1)
16 subplot(211)
17 stem(n,x_discrete)%x[n]
18 title('Project 7.1, Part(d) : \Omega_0 = 2 \pi (1500)')
19 xlim([0 49]); %first fifty samples
20 xlabel('time samples')

```

```
21 ylabel('x[t] = sin(\Omega_0 nT)')
22
23 subplot(212)
24 plot(n,x)
25 xlim([0 49]); %first fifty samples
26 xlabel('time samples')
27 ylabel('x(t) = sin(\Omega_0 t)')
28
29 if FINALPLOTS
30     print -deps proj71PartD1.eps
31 end
32
33 [X,f]=ctfts(x,T);
34
35 figure(2)
36 plot(f,abs(X))
37 title('Project 7.1, Part(d): \Omega_0 = 2 \pi (1500)')
38 xlabel('time samples')
39 ylabel('x_r(t) (CTFT)')
40
41
42 if FINALPLOTS
43     print -deps proj71PartD2.eps
44 end
45
46 %=====
47 %Repeat (a)-(c) for omega_0 = 2pi(2000)
48 %=====
49
50 Omega_0 = 2*pi*2000;
51 x = sin(Omega_0*t); % x(t)
52 x_discrete = sin(Omega_0*n*T); % x[n]
53
54
55 figure(3)
56 subplot(211)
57 stem(n,x_discrete)%x[n]
58 title('Project 7.1, Part(d) : \Omega_0 = 2 \pi (2000)')
59 xlim([0 49]); %first fifty samples
60 xlabel('time samples')
61 ylabel('x[t] = sin(\Omega_0 nT)')
62
63 subplot(212)
64 plot(n,x)
65 xlim([0 49]); %first fifty samples
66 xlabel('time samples')
67 ylabel('x(t) = sin(\Omega_0 t)')
68
69 if FINALPLOTS
70     print -deps proj71PartD3.eps
71 end
72
73 [X,f]=ctfts(x,T);
74
75 figure(4)
76 plot(f,abs(X))
77 title('Project 7.1, Part(d): \Omega_0 = 2 \pi (2000)')
78 xlabel('time samples')
79 ylabel('x_r(t) (CTFT)')
80
81
82 if FINALPLOTS
```

```

83     print -deps proj71PartD4.eps
84 end

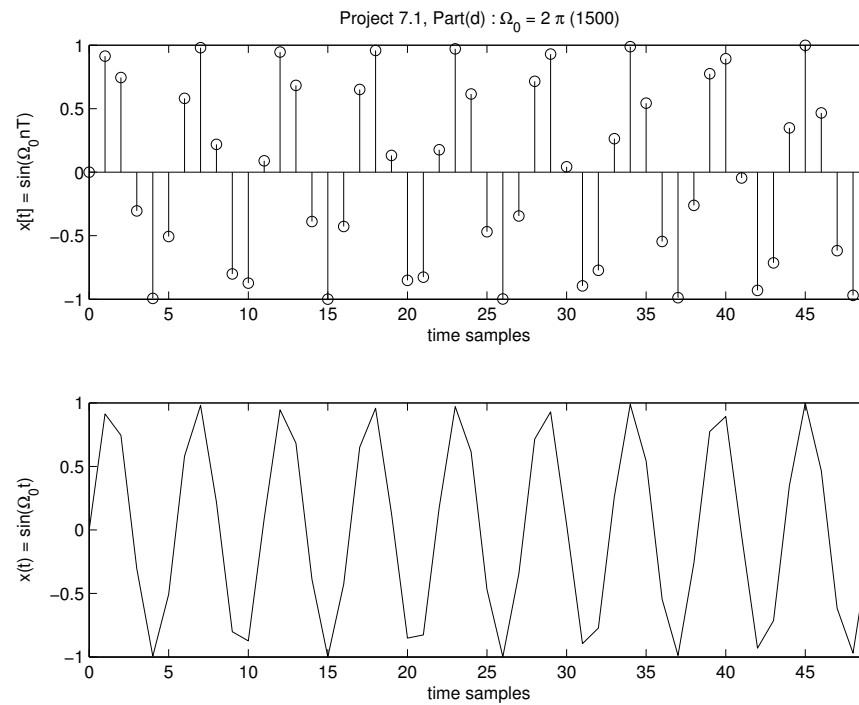
```

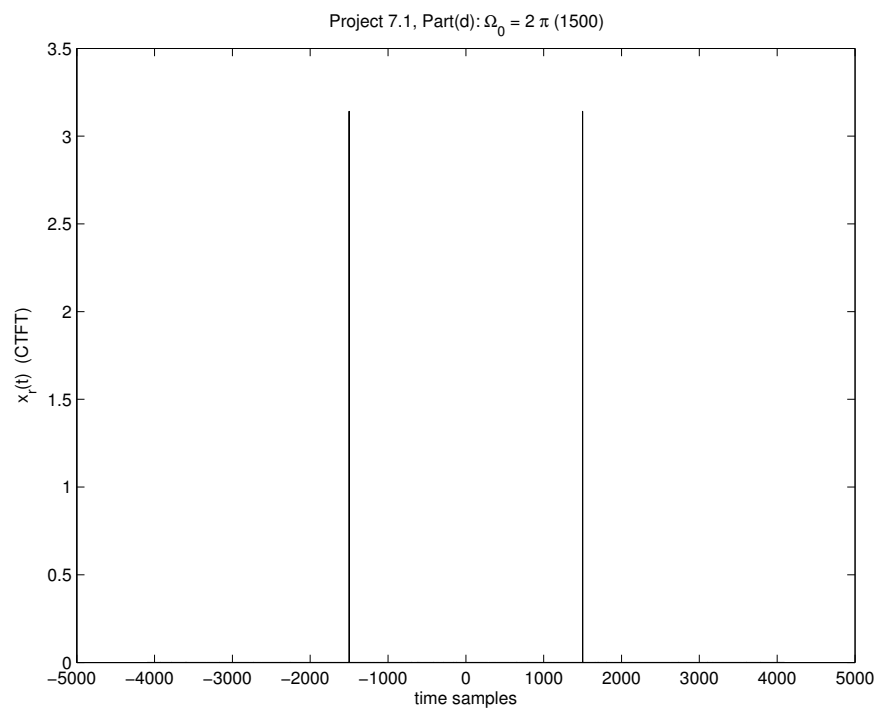
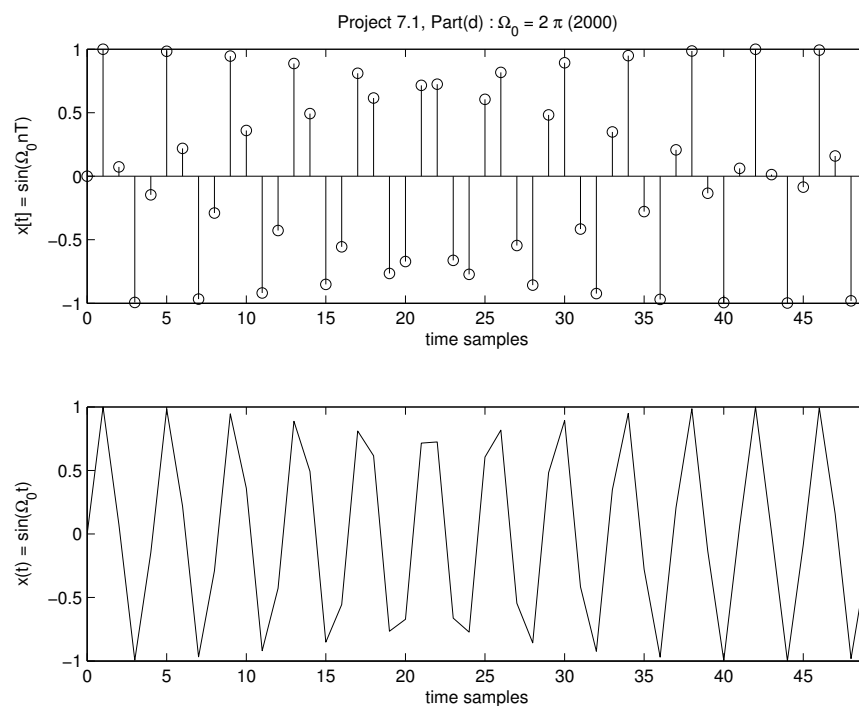
Code 7.1-4: matlab script for Part D

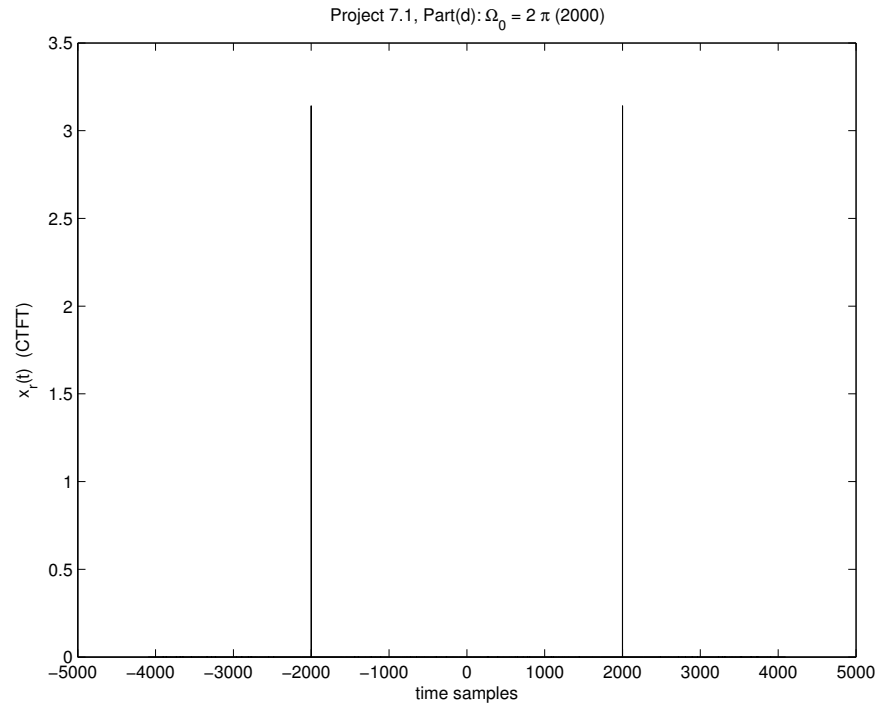
Output:

Again, is the magnitude of X nonzero for the expected frequencies? Is the phase of X correct?

Yes, It matched the expectations I Stated from previous(part C)

Figure 7.1-3: Output for 7.1 Part D —Part B for $\Omega_0 = 2\pi(1500)$

Figure 7.1-4: Output for 7.1 Part D —Part C for $\Omega_0 = 2\pi(1500)$ Figure 7.1-5: Output for 7.1 Part D —Part B for $\Omega_0 = 2\pi(2000)$

Figure 7.1-6: Output for 7.1 Part D —Part C for $\Omega_0 = 2\pi(2000)$

7.1:Part E

(e). Play each of the sampled signals created in Part(d) using `sound(x,1/T)`. Does the pitch of the tone that you hear increase with increasing frequency Ω_0 ? Note that, like `plot`, the function `sound` performs interpolation. In essence, your computer converts the discrete-time signal in MATLAB into a continuous-time signal using a digital-to-analog converter, and then plays this continuous-time signal on its speaker.

```

1 %Part 1: Project 7.1, parts (e)
2
3 Omega_0_1 = 2*pi*1500;
4 Omega_0_2 = 2*pi*2000;
5 T= 1/8192;
6 n=0:8191;
7 t=n*T;
8 x1 = sin(Omega_0_1*t); % x1(t)
9 x2 = sin(Omega_0_2*t); % x2(t)
10
11 sound(x1,1/T)
12 sound(x2,1/T)

```

Code 7.1-5: matlab script for Part E

Output:

Does the pitch of the tone that you hear increase with increasing frequency Ω_0 ? Note that, like `plot`, the function `sound` performs interpolation.

Yes, as Ω_0 increased so does the pitch. This can be observed when running the matlab script (Code 7.1-5)

7.1:Part F

(f). Now repeat Parts (a) and (c) - do not repeat Part (b) - for the sinusoidal frequencies $\Omega_0 = 2\pi(3500)$, $2\pi(4000)$, $2\pi(4500)$, $2\pi(5000)$, and $2\pi(5500)$ rad/sec. Also play each sample signal using sound. Does the pitch of the tone that you hear increase with each increase in the frequency Ω_0 ? If not, can you explain this behavior?

```

1  %Part 1: Project 7.1, parts (f)
2  function Part1Code_F(freq, FINALPLOTS)
3  %
4  % This will do both Part A and C for Part F
5  % freq: what frequency will Omega_0 be based on 2*pi*freq
6  % FINALPLOTS: bool wheter to print out the graphs
7  %
8
9  %Part A
10 Omega_0 = 2*pi*freq;
11 T= 1/8192;
12 n=0:8191;
13 t=n*T;
14 x = sin(Omega_0*t); % x(t)
15
16 %Part C
17 [X,f]=ctfts(x,T);
18
19 figure(1)
20
21 plot(f,abs(X))
22 title(['Project 7.1, Part(F) | \Omega_o = 2\pi*( ' num2str(freq) ' )'])
23 xlabel('time samples')
24 ylabel('x_r(t) (CTFT)')
25
26 output = sprintf('proj71PartF-%i.eps', freq);
27
28 if FINALPLOTS
29     print('-deps', output)
30 end
31
32 %play the freq
33 sound(x,1/T)

```

Code 7.1-6: matlab script for Part F

Output:

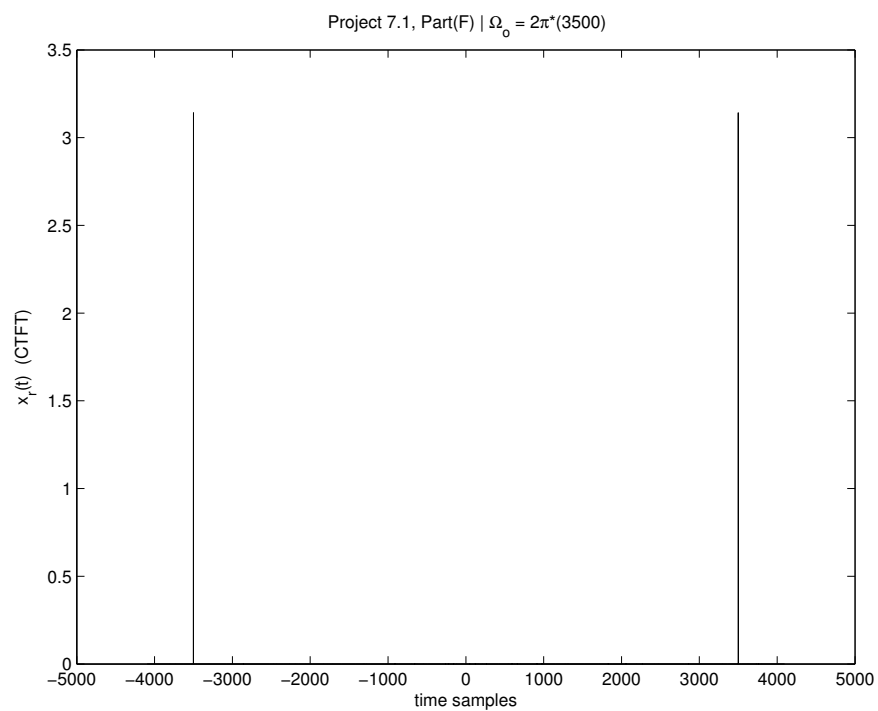
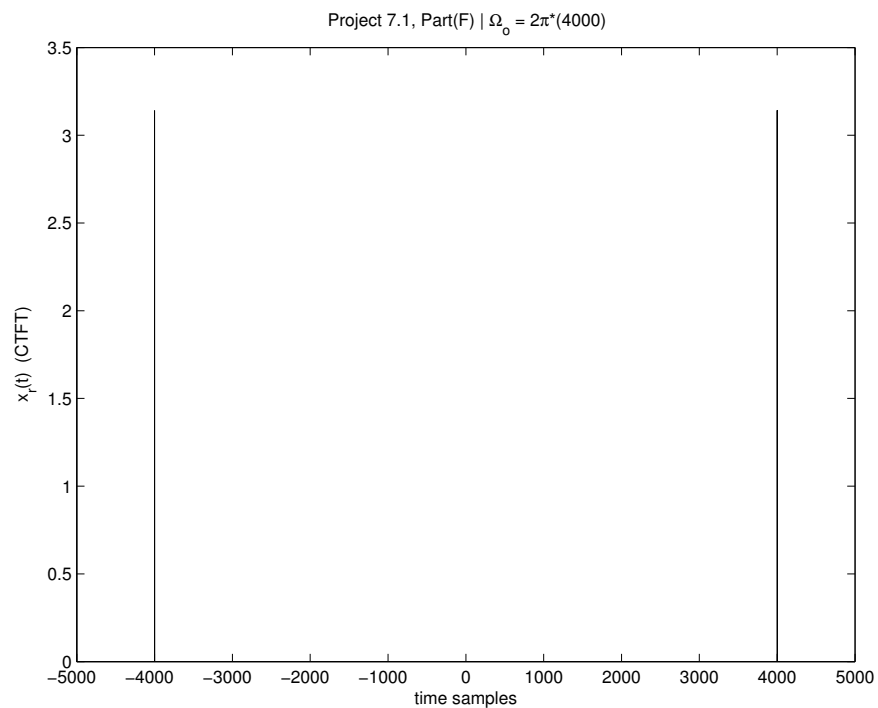
Does the pitch of the tone that you hear increase with each increase in the frequency Ω_0 ? If not, can you explain this behavior?

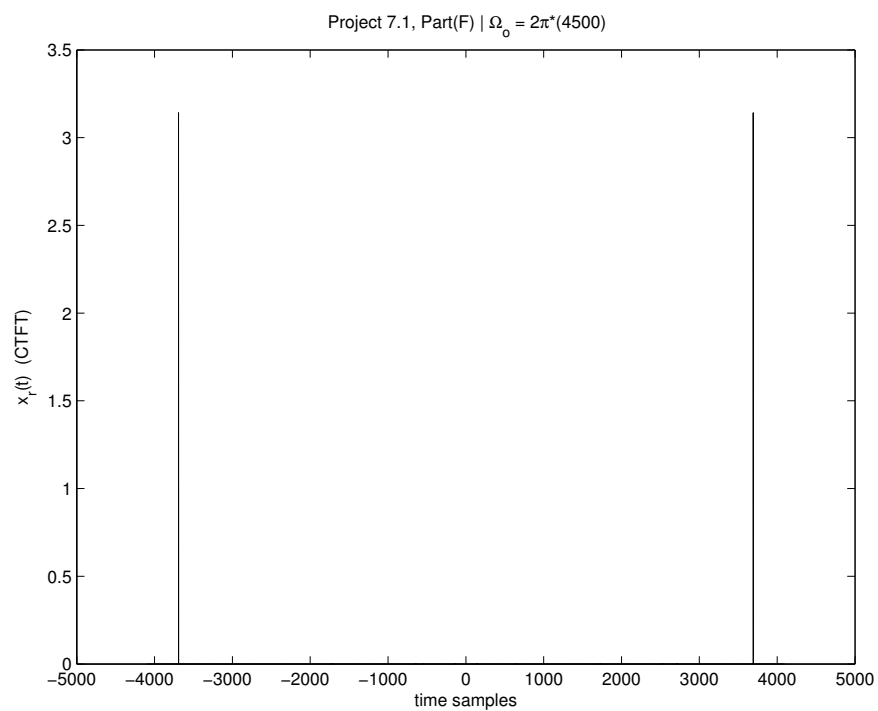
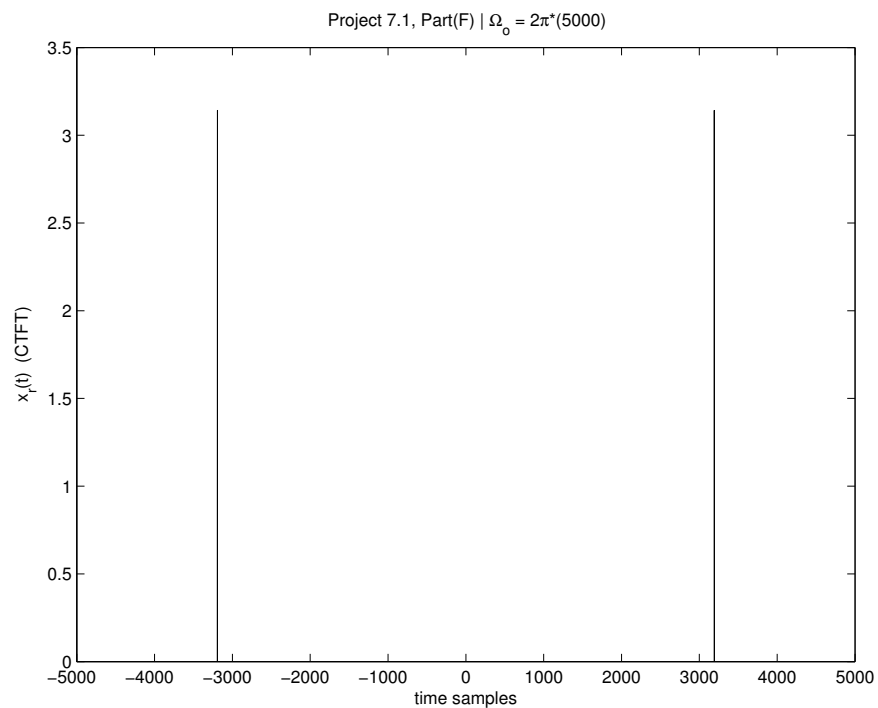
The Pitch of the tone increase to the highest frequency at $\omega_0 = 4000$ and then it decreases in pitch. This Can be observed with the Matlab script which was created as a function(Code 7.1-6).

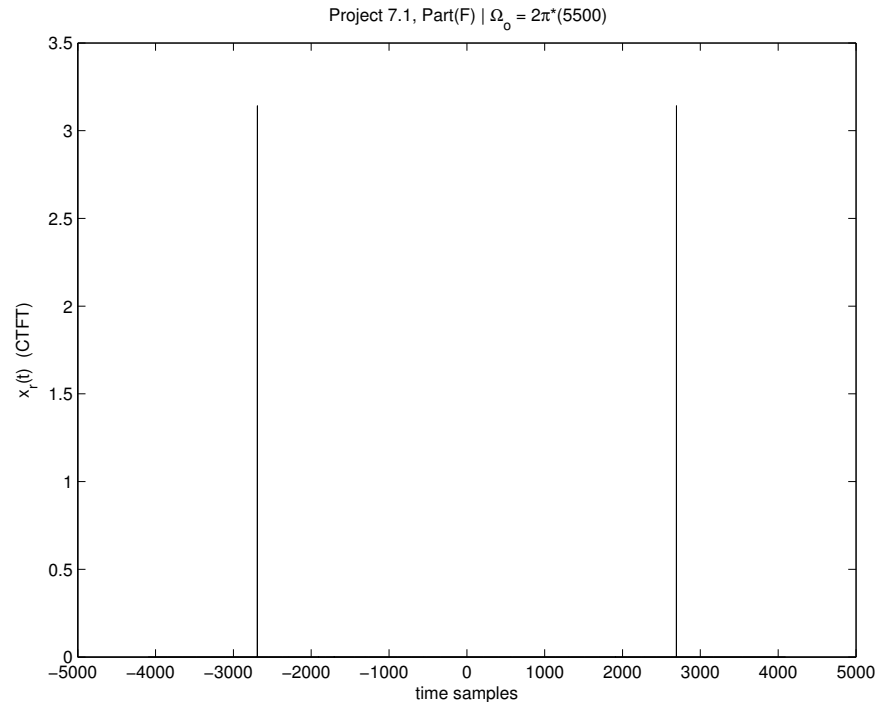
```

>> Part1Code_F(3500,0)
>> Part1Code_F(4000,0)
>> Part1Code_F(4500,0)
>> Part1Code_F(5000,0)
>> Part1Code_F(5500,0)

```

Figure 7.1-7: Output for 7.1 Part F — $\Omega_0 = 2\pi(3500)$ Figure 7.1-8: Output for 7.1 Part F — $\Omega_0 = 2\pi(4000)$

Figure 7.1-9: Output for 7.1 Part F — $\Omega_0 = 2\pi(4500)$ Figure 7.1-10: Output for 7.1 Part F — $\Omega_0 = 2\pi(5000)$

Figure 7.1-11: Output for 7.1 Part F — $\Omega_0 = 2\pi(5500)$

Advanced Problems

Now consider the signal

$$x(t) = \sin(\Omega_0 t + \tfrac{1}{2}\beta t^2).$$

which is often called a chirp signal due to the sound it makes when played through a loudspeaker. The "chirp" sound is due to the increasing instantaneous frequency of the signal over time. The instantaneous frequency of a sinusoidal signal is given by the derivatives of its phase, i.e., the argument of $\sin(\cdot)$. For the chirp signal, the instantaneous frequency is

$$\begin{aligned}\Omega_{inst}(t) &= \frac{d}{dt} \left(\Omega_0 t + \tfrac{1}{2}\beta t^2 \right) \\ &= \Omega_0 + \beta t\end{aligned}$$

Assume for the following problems that $\Omega_s = 2\pi(8192)$ rad/sec:

[Note: Use $\beta = 2\pi(2000)$ for (g)-(j), not $\beta = 2000$ as in the book.]

7.1:Part G

(g). Set $\Omega_0 = 2\pi(3000)$ rad/sec and $\beta = 2000\text{rad/sec}^2$. Store in the vector x the samples of the chirp signal on the interval $0 \leq t < 1$.

```
1 %Part 1: Project 7.1, parts (g)
2
```

```
3  Omega_0 = 2*pi*(3000);
4
5  %Based on matlab3.pdf infomation
6  beta = 2*pi*(2000);
7
8  %Omega_s=2*pi*(8192)
9  T= 1/8192;
10 n=0:8191;
11 t=n*T;
12
13 x = sin(Omega_0*t + (1/2)*beta*t.^2);
```

Code 7.1-7: matlab script for Part G

7.1:Part H

(h). Use sound to play the chirp signal contained in x. Can you explain what you just heard?

```
1  %Part 1: Project 7.1, parts (h)
2
3  Omega_0 = 2*pi*(5500);
4
5  %Based on matlab3.pdf infomation
6  beta = 2*pi*(2000);
7
8  %Omega_s=2*pi*(8192)
9  T= 1/8192;
10 n=0:8191;
11 t=n*T;
12
13 x = sin(Omega_0*t + (1/2)*beta*t.^2);
14
15 sound(x,1/T)
```

Code 7.1-8: matlab script for Part H

Output:

Can you explain what you just heard?

I Heard the sound of a mild high pitch which went higher then drop the pitch a little. This is what a chirp sounds like.

7.1:Part I

(i). Determine the approximate time sample at which the chirp signal has its maximum pitch. Given the linear equation for instantaneous frequency and your understanding of aliasing, explain how you could have predicted this time sample.

Output:

explain how you could have predicted this time sample.

Since the sample frequency $\omega_s = 2\pi * (8192)$ the sample frequency is 8192 which means $T = 1/8192$. In order of the highest frequency for the sinusoidal $\Omega_{inst}(t) = \frac{d}{dx}(\Omega_0 t + \frac{1}{2}\beta t^2)$.

7.1:Part J

(j). Store in x the samples for the first 10 seconds of the chirp signal. Play the signal using sound. Explain how you could have predicted the times at which the played signal has zero (or very low) frequency.

```
1  %Part 1: Project 7.1, parts (j)
2
3  Omega_0 = 2*pi*(3000);
4
5  %Based on matlab3.pdf infomation
6  beta = 2*pi*(2000);
7
8  %Omega_s=2*pi*(8192)
9  T= 1/8192;
10 n=0:8191*10;%increase the capture length by 10 seconds
11 t=n*T;
12
13 x = sin(Omega_0*t + (1/2)*beta*t.^2);
14
15 sound(x,1/T)
```

Code 7.1-8: matlab script for Part J

Output:

Explain how you could have predicted the times at which the played signal has zero (or very low) frequency. Upon Listening to the chirp sound, I noticed that it fluctuates the pitch 2.5 times in the entire sound. This means that it alternates a pi means 2 seconds.

The pattenen for the chirp went:

[mid|start|0] - > [high|1] - > [mid|2] - > [low|3] - > [mid|4] - > [high|5] - > [mid|6] - > [low|7] - > [mid|8] - > [high|9] - > [mid|end|10]

So therefore the lowest is at 3,7 seconds in the chirp

Part 2: New project below

You are secret agent Melbourne Wrist-toe, a member of the top-secret SD-320 organization. Your friends all believe your cover story that you are a UMassD ECE student. Working with your partner Mason, you acquired one of the coveted Ravioli manuscripts drawn by the 15th century genius and architect Manicotti Ravioli. This particular manuscript includes a diagram for a speech scrambling system, shown below in Figure 1, which was used to encode a secret message from Ravioli. Some of the important parts of the diagram in the Ravioli manuscript were damaged when you recovered it from your rival organization, ej-Directorate. Working with the SD-320 technology guru Fender, you need to use the diagram from the manuscript to write a Matlab program that will unscramble the speech and recover the secret message.

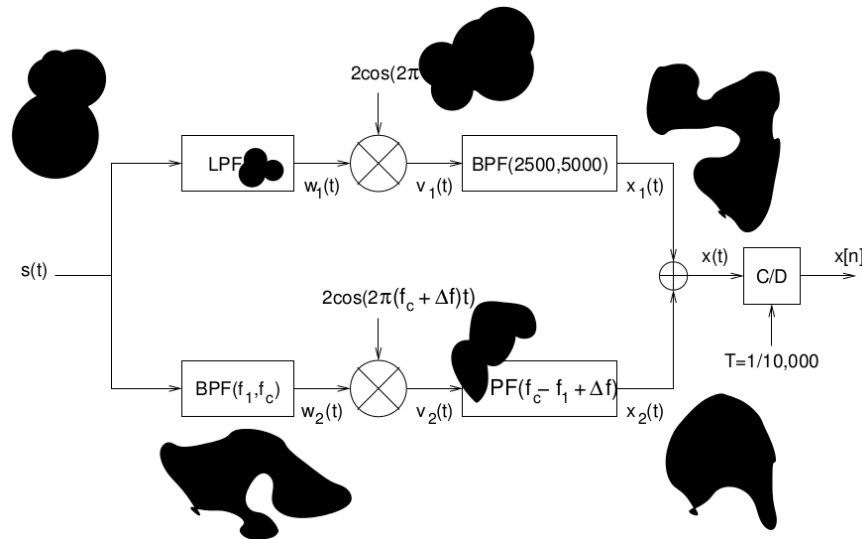


Figure Part 2-12: Secret speech scrambler from the Ravioli manuscript

Part 2: A

(a). Download the scrambled speech .wav file for your group from the course web site under Matlab Projects. You are looking for a Matlab file named groupx.wav, where x is your group number. This file contains the output of the speech scrambler sampled at 10 kHz. Listen to the file to confirm that it is truly scrambled.

```
1 %Proj 3 - Part 2 - Section (a)
2 [s] = wavread('group4.wav');
3 soundsc(s, 10000) %plays sound at 10KHz
```

Part 2: matlab script for Part A

Part 2: B

(b). Using what you learned on Project 5.1, plot the magnitude spectrum $|X(e^{j\omega})|$ for the scrambled data file you loaded from the web site. You'll need to use the wavread command to read your file into Matlab. Which parts of the spectrum look like speech? Instead of labeling your plot in DT frequencies (radians), work out the correct x-axis to label it in Hz (or kHz).


```

1  %Proj 3 - Part 2 - Section (b)
2  Nfft = 10000; % 10 kHz
3  S = fft(s,Nfft);
4  omega = (0:(Nfft-1));
5
6  figure(1)
7  clf
8
9  plot(omega,fftshift(abs(S)));
10
11 grid on
12 xlabel('Frequency (Hz)')
13 ylabel('X(e^{j\omega})')
14 title('Project 3, Part 2, Section (b): Scrambled signal spectrum |X(e^{j\omega})|')
15
16
17 if FINALPLOTS
18     print -deps Part2B.eps
19 end

```

Part 2: matlab script for Part B

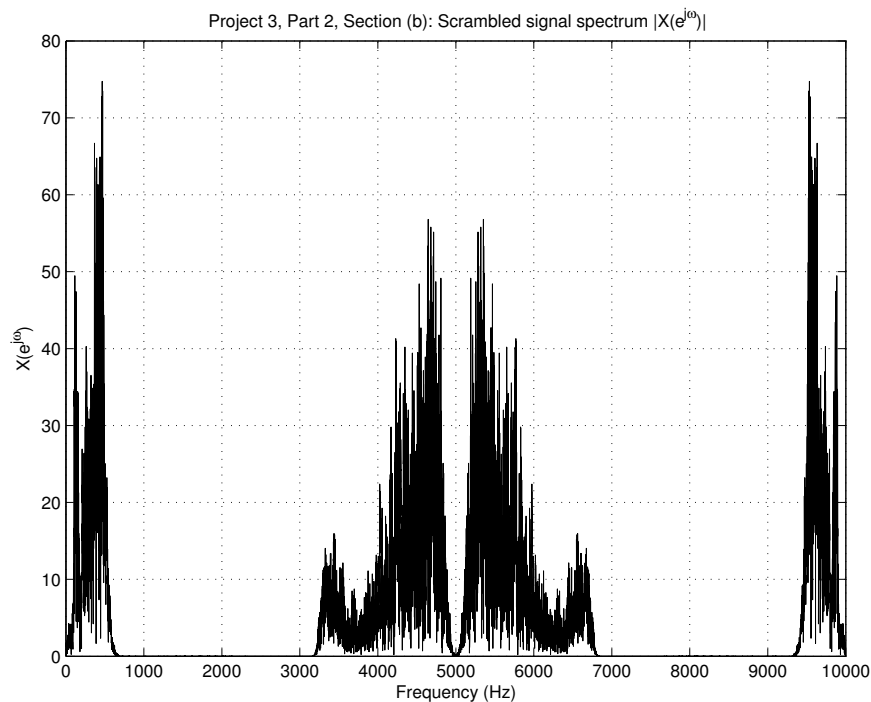


Figure Part 2-13: Output For B in Part 2

Part 2: C

(c). As a first start towards unscrambling the speech, work through graphically what the output of the system will be when the input is

$$x_c(t) = \left(\frac{\sin(2\pi(1000)t)}{\pi t} \right)^2.$$

Compare your results with the scrambled speech spectrum in part (b) to make your best guess at what the missing values are in the diagram. State clearly any assumptions you make in this process. Hand in sketches of the spectrum you get for each step in the process with all important frequencies labeled clearly.

Part 2: D

(d). Based on your work in part (c), design a DT descrambling system. You will need to be careful to convert all of the important frequencies into DT frequencies. Demonstrate that your system would correctly unscramble the test waveform in part (c) if it were sampled at 10 kHz to obtain $x[n]$.

Part 2: E

(e). Implement your unscrambling system in Matlab and decode the secret message. Use FIR filters designed with `fir1` to approximate the ideal filters in your design in part (d). Make sure all of the FIR filters you use in your system have the same length. Agent Wrist-toe, what is the secret message?

```
1  %Matlab # 3 : Part 2: parts (e)
2  %Group 4
3
4  [s] = wavread('group4.wav');
5  %soundsc(s, Freq) %10KHz
6
7  Freq = 10000;%10KHz
8
9  s=s';
10 x=s.*Freq;
11
12
13 T=1/Freq;
14 xlen=[0:(length(x)-1)];
15 N=2^nextpow2(length(x));
16 X=fftshift(fft(x,N));
17
18 %x[n]
19 figure(1)
20 plot(xlen/Freq,x)
21 grid on
22 xlabel('samples (s)')
23 ylabel('x[n]')
24 title('Project 3, Part 2, Section (e): x[n]')
25
26 if FINALPLOTS
27     print -deps Part2E-1.eps
28 end
29
30
31 %=====
32 %Top Branch
33 %=====
34
35 Wn=[0.5 0.9];
36 n = 2048;
37
38 b = fir1(n, Wn);
39 BPF=fftshift(fft(b,N));
40
```

```
41 V1=X.*BPF;
42 v1=ifft(V1,N);
43
44 k=0:N-1;
45 whz=((2*pi*k/N)-pi)./T.*(10/(2*pi));
46
47 %V1(t)
48 figure(2)
49 plot(whz.*T,abs(V1))
50 grid on
51 xlabel('freq (Khz)')
52 ylabel('|V_1(t)|')
53 title('Project 3, Part 2, Section (e): V_1(t)')
54
55 if FINALPLOTS
56     print -deps Part2E-2.eps
57 end
58
59
60 w1=v1.*(2*cos(2*pi*2000.*whz));
61 W1=fft(w1,N);
62
63 %W1(t)
64 figure(3)
65 plot(whz.*T,abs(W1))
66 grid on
67 xlabel('freq (Khz)')
68 ylabel('|W_1(t)|')
69 title('Project 3, Part 2, Section (e): W_1(t)')
70
71 if FINALPLOTS
72     print -deps Part2E-3.eps
73 end
74
75
76 wlpf=2000/5000;
77 b = fir1(n, wlpf);
78 LPF=fftshift(fft(b,N));
79
80 S1 = LPF.*W1;
81
82 %s1(t)
83 figure(4)
84 plot(whz.*T,abs(S1))
85 grid on
86 xlabel('freq (Khz)')
87 ylabel('|S_1(t)|')
88 title('Project 3, Part 2, Section (e): S_1(t)')
89
90 if FINALPLOTS
91     print -deps Part2E-4.eps
92 end
93
94
95 %=====
96 %Bot Branch
97 %=====
98
99 b = fir1(n, wlpf);
100 LPF2 = fftshift(fft(b,N));
101
102 V2 = X.*LPF2;
```

```
103 v2=ifft(V2,N);
104
105 %V2(t)
106 figure(5)
107 plot(whz.*T,abs(V2))
108 grid on
109 xlabel('freq (Khz)')
110 ylabel('|V_2(t)|')
111 title('Project 3, Part 2, Section (e): V_2(t)')
112
113 if FINALPLOTS
114     print -deps Part2E-5.eps
115 end
116
117
118 w2 = v2.*(2*cos(2*pi*2000.*whz));
119 W2 = fft(w2,N);
120
121
122 %W2(t)
123 figure(6)
124 plot(whz.*T,abs(W2))
125 grid on
126 xlabel('freq (Khz)')
127 ylabel('|W_2(t)|')
128 title('Project 3, Part 2, Section (e): W_2(t)')
129
130 if FINALPLOTS
131     print -deps Part2E-6.eps
132 end
133
134
135 Wn2 = [1000/5000 4000/5000];%need to change
136 b = fir1(n, Wn2);
137 BPF2=fftshift(fft(b,N));
138
139
140 S2=W2.*BPF2;
141
142 %s2(t)
143 figure(7)
144 plot(whz.*T,abs(S2))
145 grid on
146 xlabel('freq (Khz)')
147 ylabel('|S_2(t)|')
148 title('Project 3, Part 2, Section (e): S_2(t)')
149
150 if FINALPLOTS
151     print -deps Part2E-7.eps
152 end
153
154
155 Y=S1+S2;
156
157 y = ifft(Y,N);
158 yy=0:length(y)-1;
159 %Y(t)
160 figure(7)
161 plot(whz.*T,Y)
162 grid on
163 xlabel('freq (Khz)')
164 ylabel('Y(t)')
```

```
165 title('Project 3, Part 2, Section (e): Y(t)')
166
167 if FINALPLOTS
168     print -deps Part2E-7.eps
169 end
170
171
172
173 y=ifft(Y,N);
174 soundsc(y,10000)
```

Part 2: matlab script for Part E

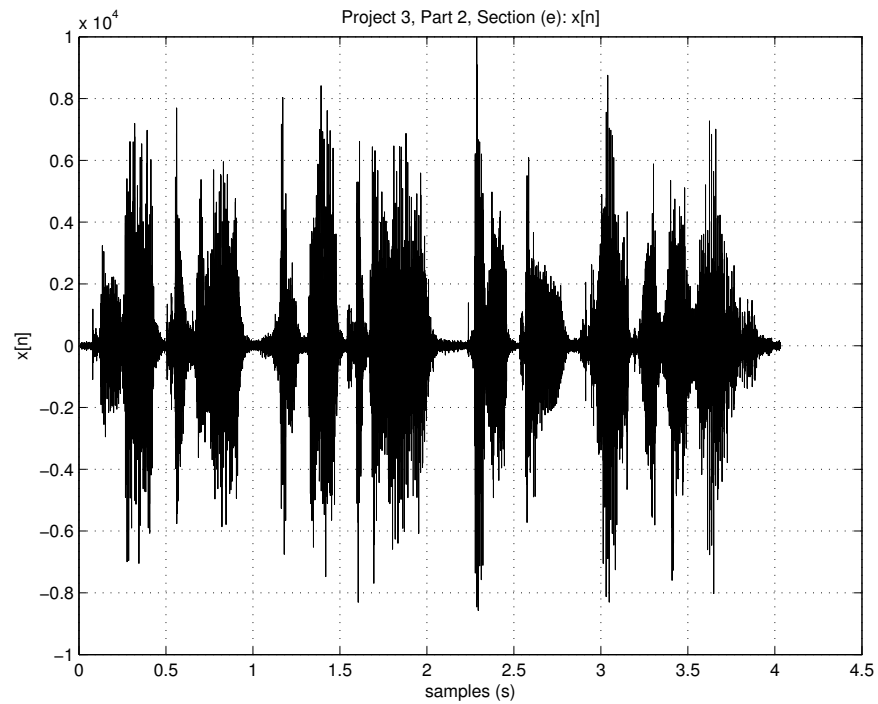


Figure Part 2-14: Output For E in Part 2

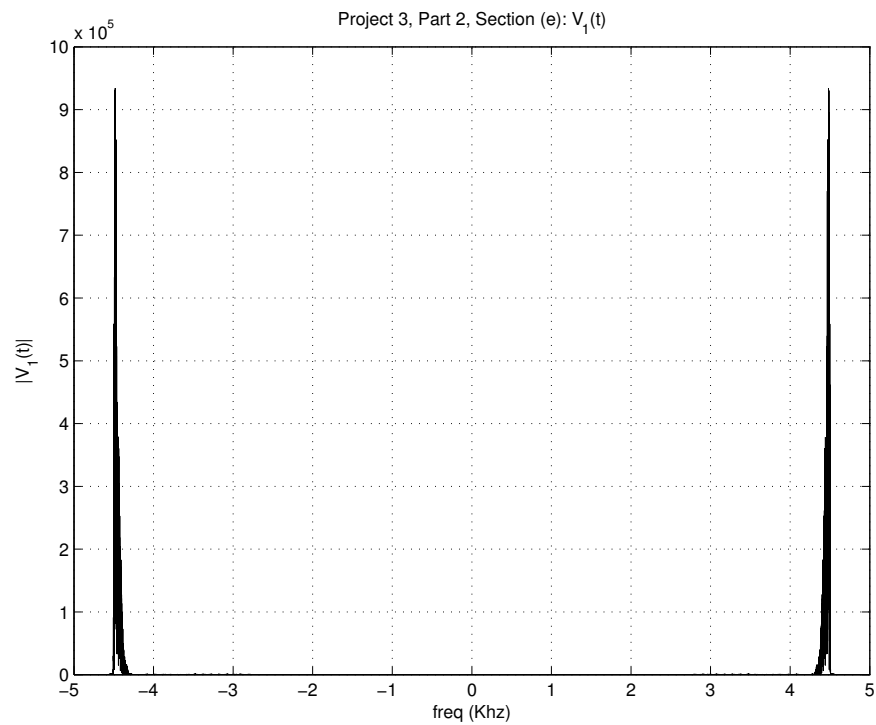


Figure Part 2-15: Output For E in Part 2

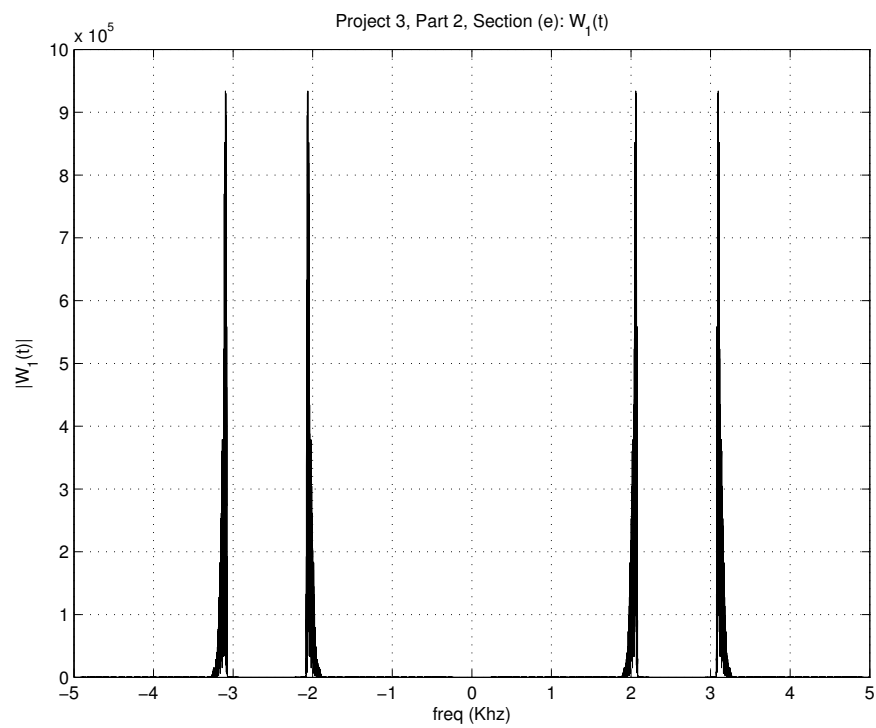


Figure Part 2-16: Output For E in Part 2

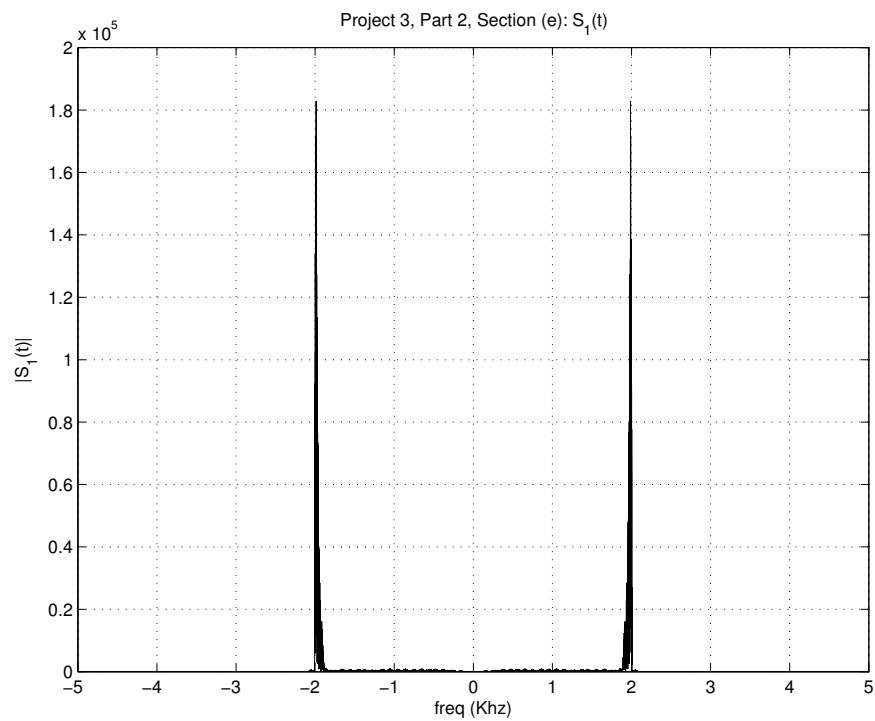


Figure Part 2-17: Output For E in Part 2

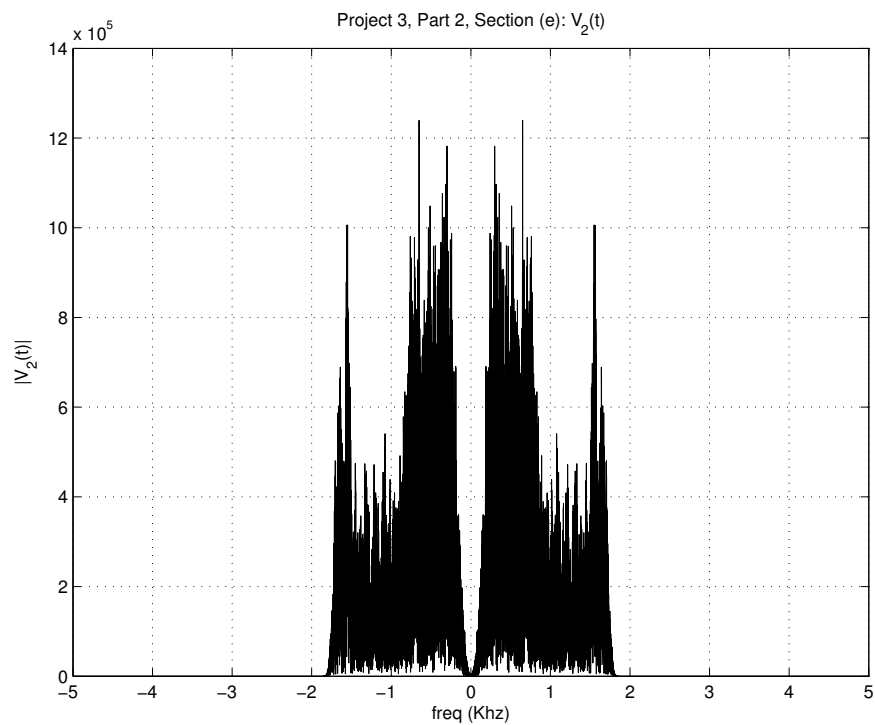


Figure Part 2-18: Output For E in Part 2

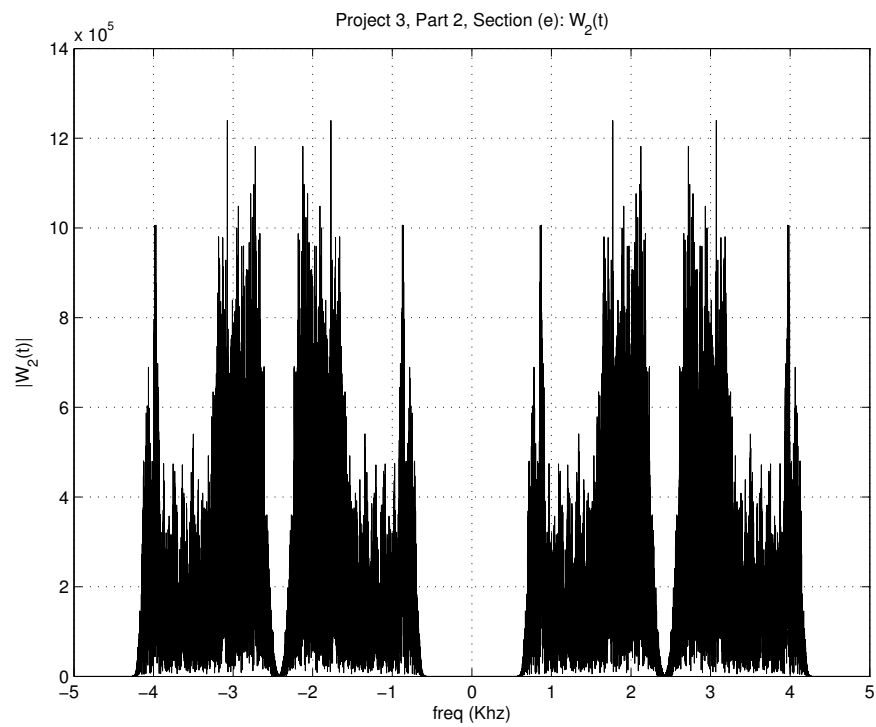


Figure Part 2-19: Output For E in Part 2

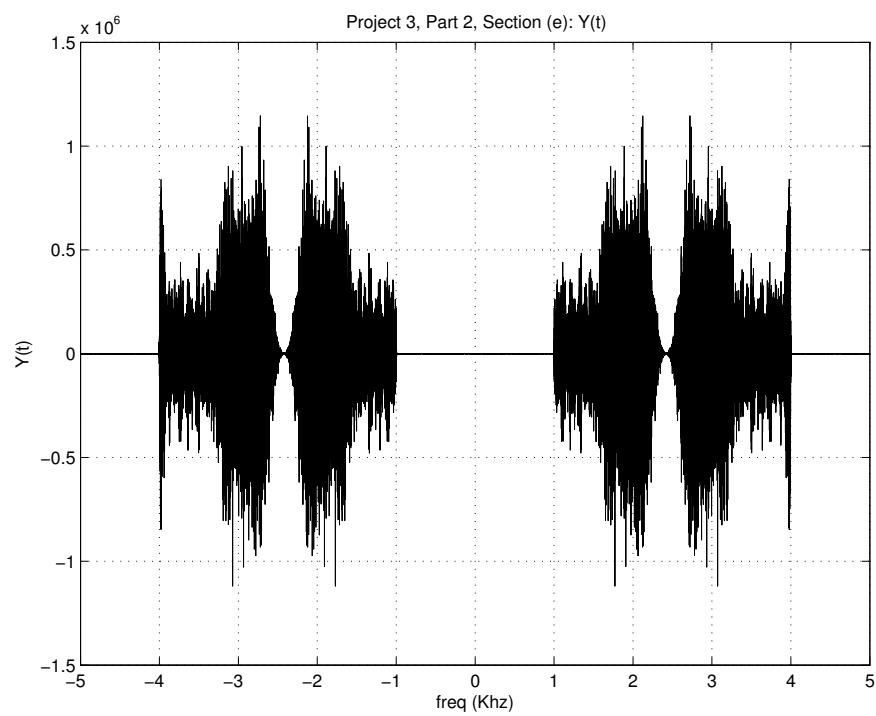


Figure Part 2-20: Output For E in Part 2