

CSE340: Computer Architecture

Chapter 3 Practice Problems

1. Consider $A = 5ED8$ and $B = 3C91$ as signed 16-bit hexadecimal numbers. **Determine** whether $A - B$ causes overflow or not. Show all the necessary work.
2. **Calculate** the product of the two hexadecimal unsigned 4-bit integers C and A using the long-multiplication approach (using the hardware with one 4-bit register and two 8-bit registers). Consider C as multiplicand and A as multiplier in the calculation. You have to show the contents of each register on each step in an iteration.
Hint: The values of C and A in decimal are 12 and 10 respectively.
3. **Calculate** the product of the two hexadecimal unsigned 4-bit integers C and A using the optimized-multiplication approach (using the hardware with one 4-bit register and one 8-bit register). Consider C as the multiplicand and A as the multiplier in the calculation. You have to show the contents of each register on each step in an iteration.
Hint: The values of C and A in decimal are 12 and 10 respectively.

Solutions:

- $A = 0101\ 1110\ 1101\ 1000 = (24280)_{\text{decimal}}$
 $B = 0011\ 1100\ 1001\ 0001 = (15505)_{\text{decimal}}$
 $A - B = 24280 - 15505 = 8775$

2's complement of B = 1100 0011 0110 1111

$$\begin{array}{r}
 A - B = A + (2\text{'s complement of } B) = 0101\ 1110\ 1101\ 1000 \\
 \phantom{A - B = A + (2\text{'s complement of } B) = } 1100\ 0011\ 0110\ 1111 \\
 \hline
 0010\ 0010\ 0100\ 0111
 \end{array}$$

No overflow because subtraction of two positive numbers will not cause overflow.
 Moreover, subtracting B from A should result in a positive number and MSB bit 0 of the result shows it is a positive number.

- $(C)_{16} \times (A)_{16} = (12)_{10} \times (10)_{10} = (120)_{10} \text{ OR } (1100)_2 \times (1010)_2 = (0111\ 1000)_2$

Iteration	Step	Multiplicand (8bits) (M1)	Multiplier (4bits) (M2)	Product (8bits)
0	init	0000 1100	1010	0000 0000
1	No opt	0000 1100	1010	0000 0000
	$M_1 \leftarrow$	0001 1000	1010	0000 0000
	$M_2 \rightarrow$	0001 1000	0101	0000 0000
	Add	0001 1000	0101	0001 1000
2	$M_1 \leftarrow$	0011 0000	0101	0001 1000
	$M_2 \rightarrow$	0011 0000	0010	0001 1000
	No opt	0011 0000	0010	0001 1000
	$M_1 \leftarrow$	0110 0000	0010	0001 1000
3	$M_2 \rightarrow$	0110 0000	0001	0001 1000
	Add	0110 0000	0001	0111 1000
	$M_1 \leftarrow$	1100 0000	0001	0111 1000
	$M_2 \rightarrow$	1100 0000	0000	0111 1000 (Ans.)

$$3. (C)_{16} \times (A)_{16} = (12)_{10} \times (10)_{10} = (120)_{10} \text{ OR } (1100)_2 \times (1010)_2 = (0111\ 1000)_2$$

Iteration	Step	Multiplicand (4bits) (Mult)	Product (8bits) (Prod)
0	Initialization	1100	0000 1010
1	No Opt.	1100	0000 1010
	Prod >> 1	1100	0000 0101
2	Addition	1101	1100 0101
	Prod >> 1	1101	0110 0010
3	No Opt.	1100	0110 0010
	Prod >> 1	1100	0011 0001
4	Addition	1100	1111 0001
	Prod >> 1	1100	0111 1000 (Ans.)