

1.

```
2A = 2 * Matrix A  
= 2 * [  
12 -3  
-5 4 2  
]  
=[  
2 4 -6  
-10 8 4  
]
```

```
5B = 5 * Matrix B  
= 5 * [  
-2 6 4  
-1 -2 3  
]  
=[  
-10 30 20  
-5 -10 15  
]
```

```
2A + 5B = [  
2 4 -6  
-10 8 4  
] + [  
-10 30 20  
-5 -10 15  
]  
=[  
(2 + -10) (4 + 30) (-6 + 20)  
(-10 + -5) (8 + -10) (4 + 15)  
]  
=[  
-8 34 14  
-15 -2 19  
]
```

Therefore, $2A + 5B$ is equal to the matrix:

```
[  
-8 34 14  
-15 -2 19  
]
```

2.

$$\begin{aligned}3A &= 3 * \text{Matrix A} \\&= 3 * [\\&\quad -3\ 1 \\&\quad -2\ 4 \\&\quad 5\ -1 \\&\quad] \\&= [\\&\quad -9\ 3 \\&\quad -6\ 12 \\&\quad 15\ -3 \\&\quad]\end{aligned}$$

$$\begin{aligned}2B &= 2 * \text{Matrix B} \\&= 2 * [\\&\quad 4\ -2 \\&\quad 0\ -2 \\&\quad -2\ 4 \\&\quad] \\&= [\\&\quad 8\ -4 \\&\quad 0\ -4 \\&\quad -4\ 8 \\&\quad]\end{aligned}$$

$$\begin{aligned}3A - 2B &= [\\&\quad -9\ 3 \\&\quad -6\ 12 \\&\quad 15\ -3 \\&\quad] - [\\&\quad 8\ -4 \\&\quad 0\ -4 \\&\quad -4\ 8 \\&\quad] \\&= [\\&\quad (-9 - 8)\ (3 - -4) \\&\quad (-6 - 0)\ (12 - -4) \\&\quad (15 - -4)\ (-3 - 8) \\&\quad] \\&= [\\&\quad -17\ 7 \\&\quad -6\ 16 \\&\quad 19\ -11 \\&\quad]\end{aligned}$$

Therefore, $3A - 2B$ is equal to the matrix:

$$\begin{bmatrix} -17 & 7 \\ -6 & 16 \\ 19 & -11 \end{bmatrix}$$

3.

$$\text{Matrix A} = [\begin{matrix} 3 & -2 & 5 \\ 0 & -1 & 6 \\ -4 & 2 & -1 \\ \end{matrix}]$$

$$\text{Matrix B} = [\begin{matrix} 2 & -1 & 0 \\ 3 & -5 & 2 \\ 1 & 4 & -2 \\ \end{matrix}]$$

$$\begin{aligned} BA = & [\\ & (2 * 3 + -1 * 0 + 0 * -4) (2 * -2 + -1 * -1 + 0 * 2) (2 * 5 + -1 * 6 + 0 * -1) \\ & (3 * 3 + -5 * 0 + 2 * -4) (3 * -2 + -5 * -1 + 2 * 2) (3 * 5 + -5 * 6 + 2 * -1) \\ & (1 * 3 + 4 * 0 + -2 * -4) (1 * -2 + 4 * -1 + -2 * 2) (1 * 5 + 4 * 6 + -2 * -1) \\ &] \end{aligned}$$

Therefore, BA is equal to the matrix:

$$BA = [\begin{matrix} 6 & 3 & 7 \\ 13 & -19 & \\ 17 & -6 & 29 \\ \end{matrix}]$$

4.

Matrix A = [
1 -2
4 -3
]
]

Matrix B = [
-14
6 -2
]
]

First, let's calculate the transpose of Matrix A:

AT = Transpose of Matrix A
=[
14
-2 -3
]
]

Now, let's calculate the transpose of Matrix B:

BT = Transpose of Matrix B
=[
-16
4 -2
]
]

Therefore, $3AT - 2BT$ is equal to the matrix:

[
5 0
-14 -5
]
]

$3AT - 2BT = 3 * AT - 2 * BT$
= $3 * [$
14
-2 -3
] $- 2 * [$
-16
4 -2
]
=[
3 12
-6 -9
] $- [$
-2 12
8 -4
]
=[
 $(3 - -2)(12 - 12)$
 $(-6 - 8)(-9 - -4)$
]
=[
5 0
-14 -5
]
]