

# Stock recruitment relationships

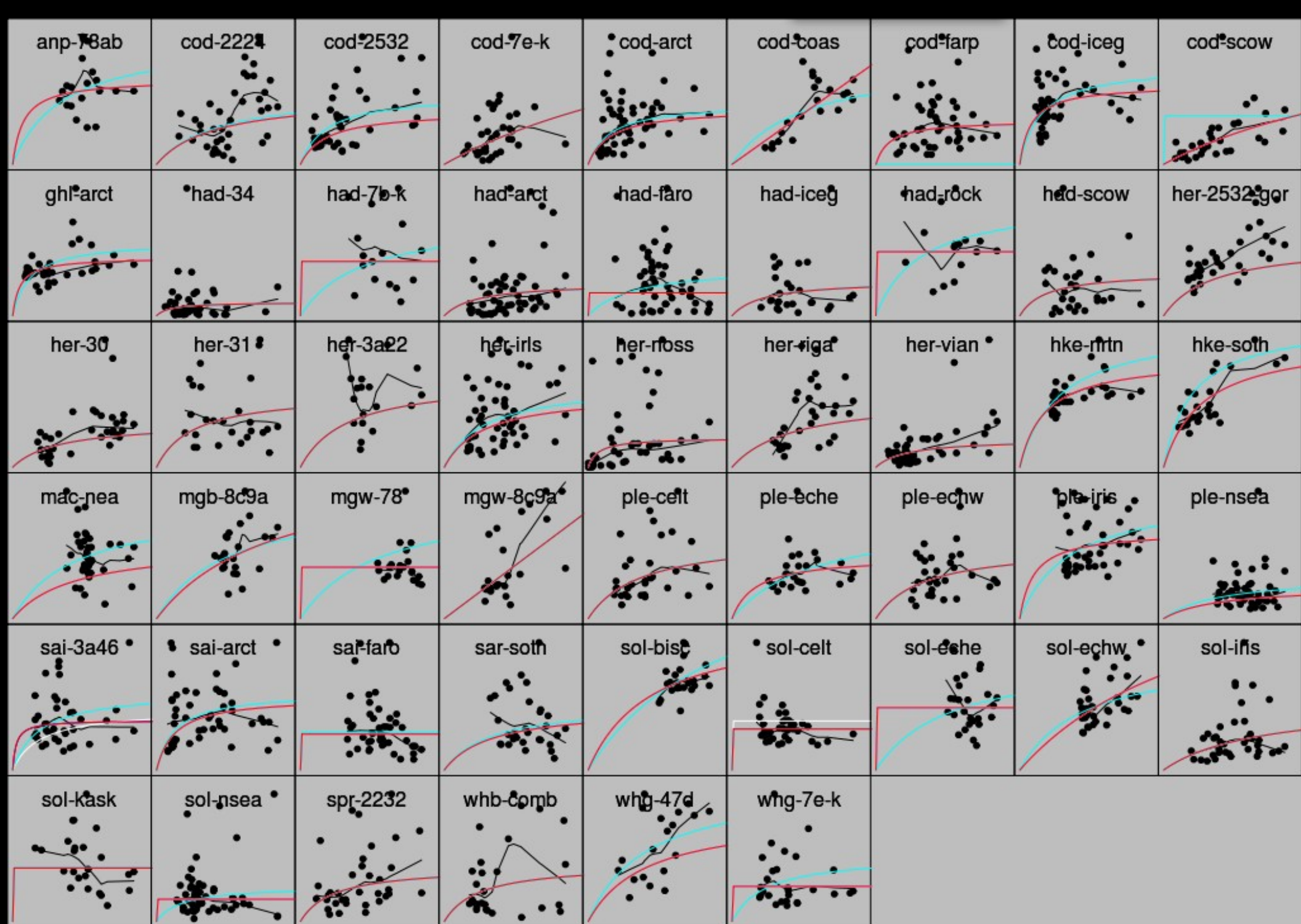
Iago Mosqueira  
Cefas, UK

# Stock-recruitment

- “The most important and generally most difficult problem in biological assessment of fisheries” - Hilborn & Walters, 1991.
- How much can the stock drop before recruitment is affected.
- Simplifies life history up to recruits: management

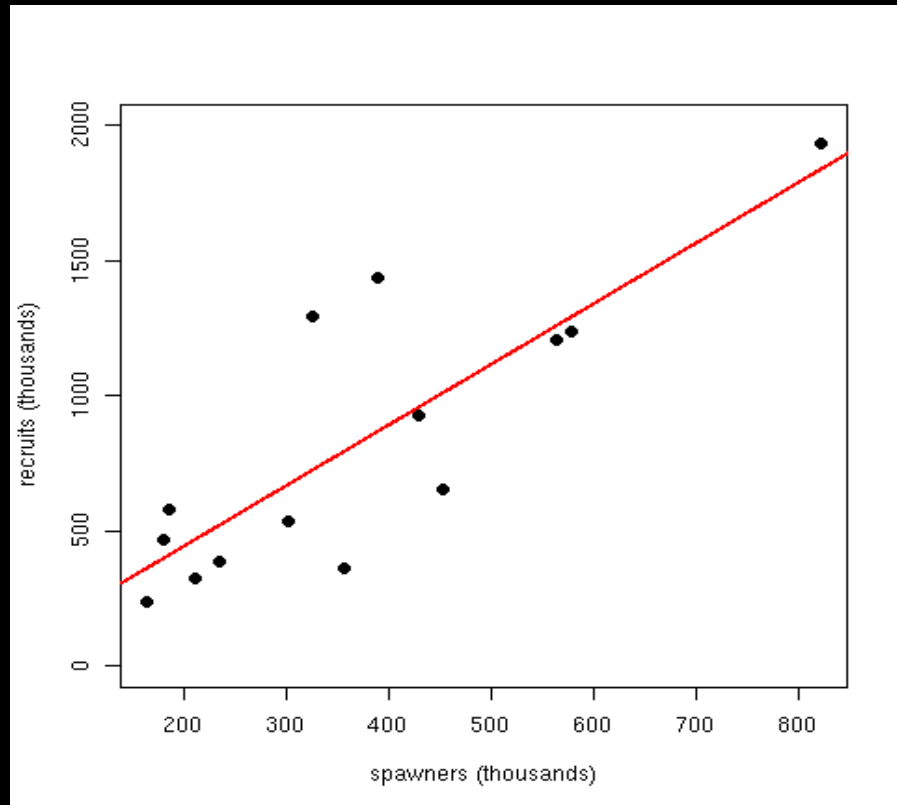
# What are stock and recruits?

- Stock (SSB) = reproductive potential
- Recruits: individuals reaching a certain stage
  - Larvae settlement
  - Fishery
- Recruits (N at age 1) = realized reproduction
- SSB<sub>y</sub> & rec<sub>y+1</sub>



# Biological processes

- Density independence: predation, starvation and environmental impacts
- Must have limits



# Biological processes

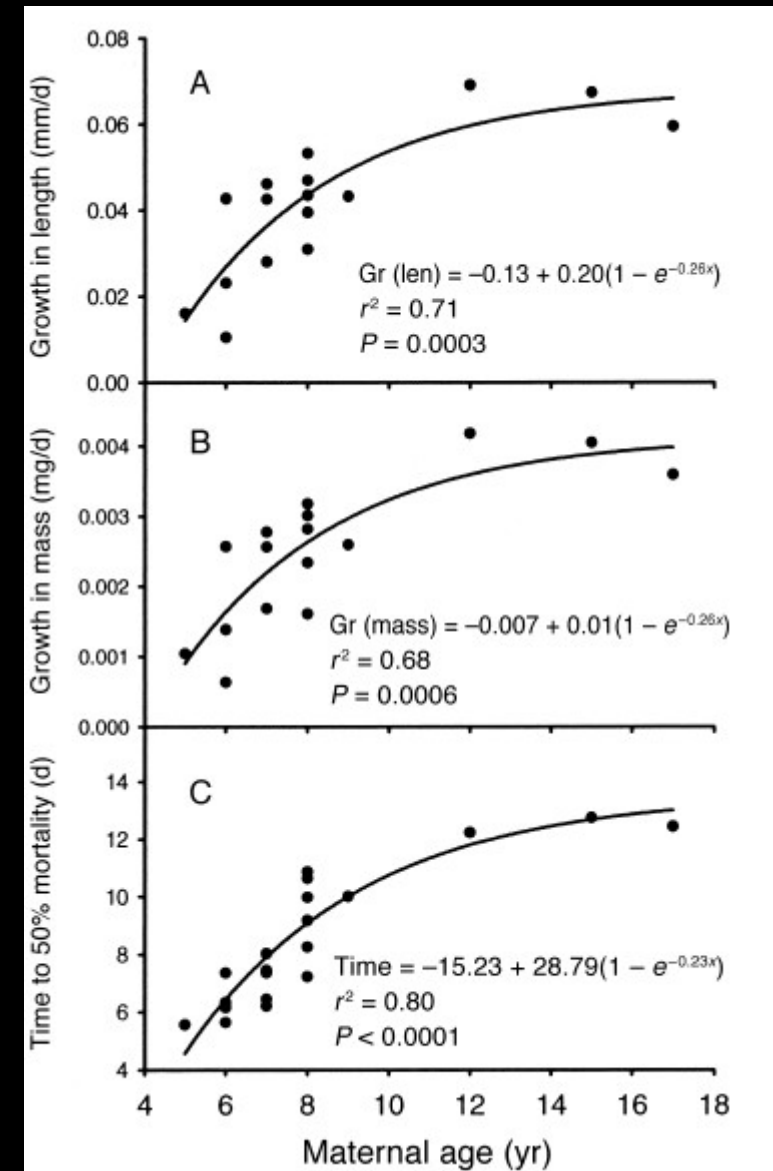
- Compensation: recruitment becomes independent of spawners
- Recruits-per-spawner decreases
- Competition for food or space, cannibalism

# Biological processes

- Depensation: recruits-per-spawner increases
- (1) Predation constant, smaller % as SSB increases
- (2) Reduced fertilization success (Allee effect)

# Reproductive potential and SSB

- SSB is a proxy of reproductive potential
- But egg production not linearly related to SSB
  - eggs/g body weight
  - Maternal effects
  - Egg size vs. age
  - BOFFFFF hypothesis





# Beverton & Holt

- Mortality rate linearly dependent upon fish in cohort due to juvenile competition

$$R = \frac{a * S}{1 + b * S}$$

- $a$  changes the height of the asymptote
- $b$  increases the rate of approach to it

$$R = \frac{\alpha * S}{\beta * S}$$

- $\alpha$  max number of recruits
- $\beta$  SSB that gives mean rec of  $\alpha/2$

# Ricker

- Mortality rate linearly dependent to initial cohort size

$$R = a * S e^{-b * S}$$

- $a$  is the density-independent parameter
- $b$  is the density-dependent parameter
- Maximum mean rec at  $S = 1/b$

Google maps

ricker's curve, nanaimo

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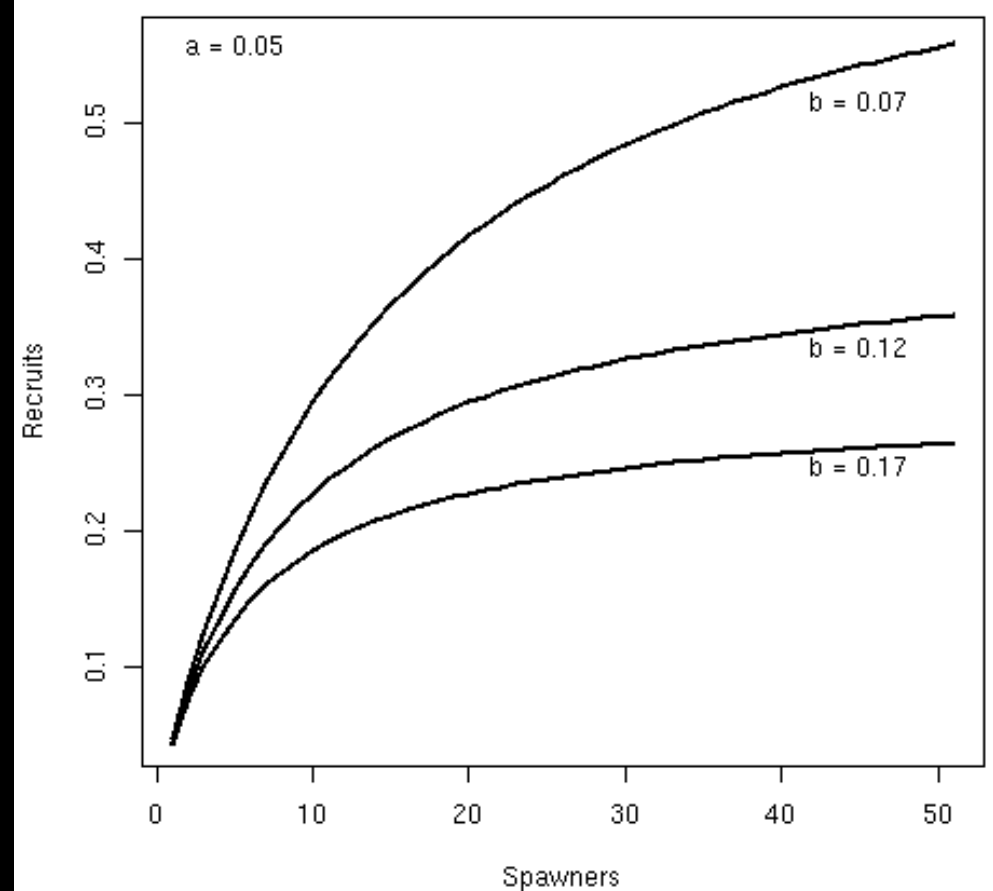
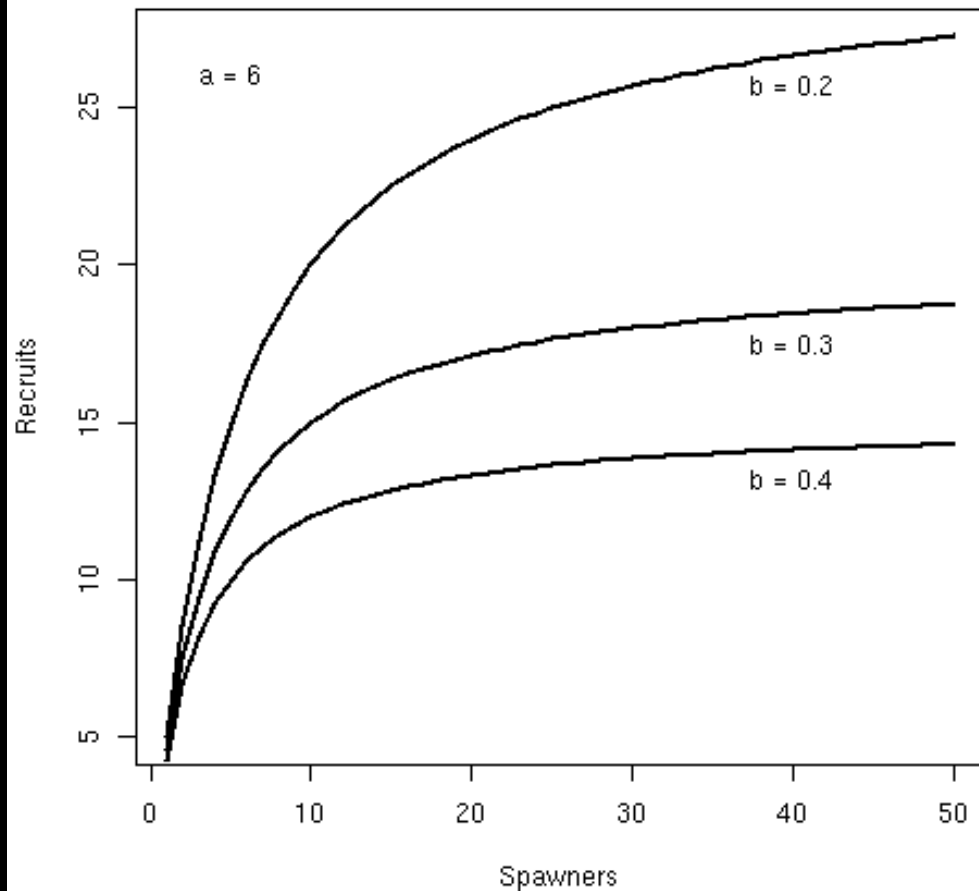


# Exercise: Beverton & Holt

- Plot B&H model changes with  $\alpha$ ,  $\beta$
- `spawn <- seq(1,50)`
- `a=6, b=seq(0.2, 0.4, by=0.1)`
- `b=0.2, a=c(2,4,6)`
- EXTRA: Do the same for Ricker
- `a=0.05, b=c(0.05, 0.10, 0.15)`
- `B=0.07, b=seq(1,5)`

$$R = a * S e^{-b * S}$$

# Exercise: Beverton & Holt



# Shepherd

$$R = \frac{a * S}{1 + (b * S)^c}$$

- a slope at low stock sizes
- b is the density-dependent parameter
- c shape parameter
  - $c < 1$  curve rises
  - $c = 1$  B&H
  - $c > 1$  Ricker
- Usually no information to estimate c, but worth trying!

# Depensatory models

- Potential recruits are then subject to predation
- Models are added a depensatory parameter

$$R = a * S^m e^{-b * S}$$

- M is greater than 1
- Estimated from data, should be much greater than 1



# Model fitting: good, bad and ugly

- Some models can be linearized in log scale (Ricker)
- Error structure given by lm, and inputs assumed without error
- Non-linear regression, error structure chosen
- Non-linear models, solved by numerical methods.
- State-space for observation & model error
- Bayesian models

# Model fitting: maximum likelihood

- Alternative to SS
- Minimize the  $-\log(\text{likelihood})$  of the model given the data
- Explicit formulation of error structure

