

Tarea 4-01

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A

Scanned with

Aplicar el método de potencia para encontrar el valor propio dominante de la matriz $A = \begin{pmatrix} 10 & -12 & -6 \\ 5 & -5 & -4 \\ -1 & 0 & 3 \end{pmatrix}$ hasta una tolerancia $|x^{(k)} - x^{(k-1)}| < 0.001$

$$x^{(0)} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

$$x^{(1)} = \begin{pmatrix} 10 & -12 & -6 \\ 5 & -5 & -4 \\ -1 & 0 & 3 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} -8 \\ -4 \\ 2 \end{pmatrix}$$

$$y_{p0}^{(1)} = -8$$

$$\lambda^{(1)} = -8/1 = -8$$

$$u_1^{(1)} = y_{p0}^{(1)} \quad \rho_1 = 1 \quad u^{(1)} = \frac{1}{-8} \begin{pmatrix} -8 \\ -4 \\ 2 \end{pmatrix} = \begin{pmatrix} 1 \\ 1/2 \\ -1/4 \end{pmatrix}$$

$$\begin{pmatrix} 10 & -12 & -6 \\ 5 & -5 & -4 \\ -1 & 0 & 3 \end{pmatrix} \begin{pmatrix} -8 \\ -4 \\ 2 \end{pmatrix} = \begin{pmatrix} -94 \\ -18 \\ 14 \end{pmatrix}$$

$$\lambda^{(2)} = \frac{-44}{-8} = 5.5$$

~~$$A x^{(2)} = \begin{pmatrix} -94.148 \\ -94.776 \\ 14.0406 \end{pmatrix}$$~~

$$\begin{pmatrix} 10 & -12 & -6 \\ 5 & -5 & -4 \\ -1 & 0 & 3 \end{pmatrix} \begin{pmatrix} -44 \\ -18 \\ 14 \end{pmatrix} = \begin{pmatrix} -188 \\ -136 \\ 86 \end{pmatrix}$$

$$\lambda^{(3)} = \frac{-188}{-44} = 4.27$$

~~$$A x^{(3)} = \begin{pmatrix} -44.148 \\ -94.776 \\ 14.0406 \end{pmatrix}$$~~

$$\begin{pmatrix} -188 \\ -136 \\ 86 \end{pmatrix} \cdot \begin{pmatrix} -361 \\ -604 \\ 446 \end{pmatrix}$$

$$\lambda^{(4)} = \frac{-764}{-188} = 4.06$$

$$\lambda^{(6)} = 4.00017$$

$$A x^{(7)} = \begin{pmatrix} -44.609 \\ -94.776 \\ 14.0406 \end{pmatrix}$$

$$\begin{pmatrix} -361 \\ -604 \\ 446 \end{pmatrix} \cdot \begin{pmatrix} -3068 \\ -2884 \\ 12102 \end{pmatrix}$$

$$\lambda^{(9)} = 4.0157$$

$$\lambda^{(7)} = 4.00024$$

$$\begin{pmatrix} -12284 \\ -10828 \\ 4374 \end{pmatrix}$$

$$\lambda^{(10)} = 4.0039$$