Block on &

(WIP) Ideas for primitive blocking: from locks to futexes and beyond

Justus Fasse and Bart Jacobs

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Agenda

Problem: classic deadlock-freedom specs are too restrictive

Solution: Parameterize modules by client-specific deadlock-freedom

argument

Application: Futexes (Compare-and-sleep)

Outlook

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Problem: classic deadlock-freedom specs are too restrictive

Solution: Parameterize modules by client-specific deadlock-freedom argument

Application: Futexes (Compare-and-sleep)

Outlook

Primitive blocking

Operational semantics (stuttering)

Acq-Succ
$$\sigma.\text{Heap}(lk) = \textbf{false}$$

$$(\textbf{Acq}\ lk, \sigma) \rightarrow_{\text{h}} ((), \sigma: \text{Heap}[lk \leftarrow \textbf{true}], \epsilon)$$

Primitive blocking

Operational semantics (stuttering)

$$\begin{array}{c} \text{Acq-Succ} \\ \sigma.\text{Heap}(\mathit{lk}) = \mathsf{false} \\ \hline (\mathsf{Acq}\;\mathit{lk},\sigma) \to_\mathsf{h} ((),\sigma:\text{Heap}[\mathit{lk} \leftarrow \mathsf{true}],\epsilon) \end{array} \qquad \begin{array}{c} \mathsf{Acq\text{-Block}} \\ \sigma.\text{Heap}(\mathit{lk}) = \mathsf{true} \\ \hline (\mathsf{Acq}\;\mathit{lk},\sigma) \to_\mathsf{h} (\mathsf{Acq}\;\mathit{lk},\sigma,\epsilon) \end{array}$$

Primitive blocking

Operational semantics (stuttering)

Acq-Succ
$$\sigma.\text{Heap}(lk) = \textbf{false} \qquad \qquad \sigma.\text{Heap}(lk) = \textbf{true}$$

$$(\textbf{Acq}\ lk, \sigma) \rightarrow_{\text{h}} ((), \sigma: \text{Heap}[lk \leftarrow \textbf{true}], \epsilon) \qquad \qquad (\textbf{Acq}\ lk, \sigma) \rightarrow_{\text{h}} (\textbf{Acq}\ lk, \sigma, \epsilon)$$

$$\frac{\text{Rel}}{(\textbf{Rel}\ lk, \sigma) \rightarrow_{\text{h}} ((), \sigma: \text{Heap}[lk \leftarrow \textbf{false}], \epsilon)}$$

$$\frac{lk \notin \mathrm{dom}(\sigma.\mathrm{Locks})}{(\mathsf{NewLock}\ \lambda, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} (lk, \sigma: \mathrm{Locks}[lk \leftarrow (\mathsf{false}, \lambda)], \epsilon)}$$

$$\begin{array}{c} lk \notin \mathrm{dom}(\sigma.\mathrm{Locks}) \\ \hline (\mathsf{NewLock}\; \lambda, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}}\; (lk, \sigma: \mathrm{Locks}[\mathit{lk} \leftarrow (\mathsf{false}, \lambda)], \epsilon) \\ \\ \mathrm{Acq\text{-}Succ} \\ \hline (\mathsf{Acq}\; \mathit{lk}, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}}\; ((), \sigma: \mathrm{Locks}[\mathit{lk} \leftarrow (\mathsf{true}, \lambda)]: \mathrm{Obs}(\theta) \uplus \hookrightarrow \{\lambda\}, \epsilon) \end{array}$$

$$\frac{lk \notin \text{dom}(\sigma.\text{Locks})}{(\text{NewLock }\lambda,\sigma) \underset{\theta}{\longrightarrow}_{\text{h}} (lk,\sigma:\text{Locks}[lk \leftarrow (\text{false},\lambda)],\epsilon)}$$
 Acq-Succ
$$\sigma.\text{Locks}(lk) = (\text{false},\lambda) \\ \hline (\text{Acq }lk,\sigma) \underset{\theta}{\longrightarrow}_{\text{h}} ((),\sigma:\text{Locks}[lk \leftarrow (\text{true},\lambda)]:\text{Obs}(\theta) \uplus \longleftrightarrow \{\lambda\}\,,\epsilon)}$$

$$\frac{\sigma. \text{Locks}(\textit{lk}) = (\textbf{true}, \lambda)}{(\textbf{Rel}\;\textit{lk}, \sigma) \underset{\theta}{\longrightarrow}_{\text{h}} ((), \sigma: \text{Locks}[\textit{lk} \leftarrow (\textbf{false}, \lambda)]: \text{Obs}(\theta) \setminus \hookrightarrow \{\lambda\}, \epsilon)}$$

$$\begin{array}{l} \operatorname{NewLock} \\ lk \notin \operatorname{dom}(\sigma.\operatorname{Locks}) \\ \hline (\operatorname{NewLock} \lambda, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} (lk, \sigma : \operatorname{Locks}[lk \leftarrow (\operatorname{false}, \lambda)], \epsilon) \\ \\ \operatorname{Acq-Succ} \\ \hline (\operatorname{Acq-Succ} \\ \hline (\operatorname{Acq} lk, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} ((), \sigma : \operatorname{Locks}[lk \leftarrow (\operatorname{true}, \lambda)] : \operatorname{Obs}(\theta) \uplus \longleftrightarrow \{\lambda\}, \epsilon) \\ \\ \overline{(\operatorname{Acq} lk, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} (\operatorname{Acq} lk, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} (\operatorname{Acq} lk, \sigma, \epsilon)} \\ \\ \operatorname{Rel} \\ \hline (\operatorname{Rel} lk, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} ((), \sigma : \operatorname{Locks}[lk \leftarrow (\operatorname{false}, \lambda)] : \operatorname{Obs}(\theta) \setminus \longleftrightarrow \{\lambda\}, \epsilon) \\ \hline \\ (\operatorname{Rel} lk, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} ((), \sigma : \operatorname{Locks}[lk \leftarrow (\operatorname{false}, \lambda)] : \operatorname{Obs}(\theta) \setminus \longleftrightarrow \{\lambda\}, \epsilon) \\ \hline \end{array}$$

```
NewLock
                                                    lk \notin dom(\sigma.Locks)
               (NewLock \lambda, \sigma) \rightarrow_{\theta} (lk, \sigma : Locks[lk \leftarrow (false, \lambda)], \epsilon)
Acq-Succ
                                             \sigma.Locks(lk) = (false, \lambda)
 (\text{Acq } lk, \sigma) \xrightarrow{\theta} ((), \sigma : \text{Locks}[lk \leftarrow (\text{true}, \lambda)] : \text{Obs}(\theta) \uplus \leftarrow \{\lambda\}, \epsilon)
                           Acq-Block
                           \sigma.Heap(lk) = (true, \lambda) \lambda \prec \sigma.Obs(\theta)
                                          (\operatorname{Acq} lk, \sigma) \xrightarrow{\theta} (\operatorname{Acq} lk, \sigma, \epsilon)
Rel
                                              \sigma.Locks(lk) = (true, \lambda)
(\text{Rel } lk, \sigma) \underset{\theta}{\longrightarrow}_{\mathsf{h}} ((), \sigma : \text{Locks}[lk \leftarrow (\text{false}, \lambda)] : \text{Obs}(\theta) \setminus \leftarrow \{\lambda\}, \epsilon)
```

Operational semantics

FORK
$$\theta' \notin \text{dom}(\Theta)$$

$$(\textbf{fork} \ e \ obs, \sigma) \xrightarrow{\theta}_{h} ((), \sigma : \text{Obs}(\theta) \setminus \longleftrightarrow obs : \text{Obs}(\theta') \uplus \longleftrightarrow obs, (\theta', (e; \textbf{Finish}))$$

$$FINISH$$

$$\sigma.\text{Obs}(\theta) = \emptyset$$

$$(\textbf{Finish}, \sigma) \xrightarrow{\theta}_{h} ((), \sigma, \epsilon)$$

À la Kobayashi 2006, Leino et al. 2010, Boström and Müller 2015, Jacobs et al. 2018, Reinhard and Jacobs 2021

A deadlock-free language, restrictive language

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

A deadlock-free language, restrictive language

```
// obs(Ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(Ø)
```

Finish

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

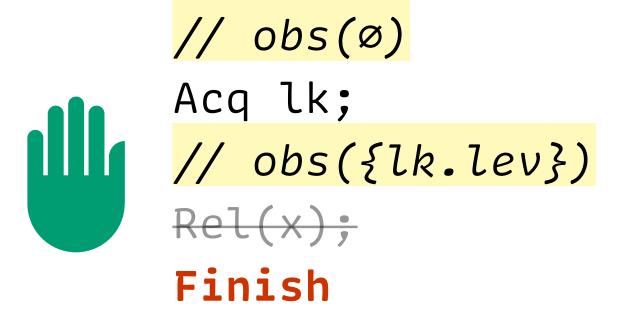
```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel(x);
Finish
```

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

A deadlock-free language, restrictive language

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```



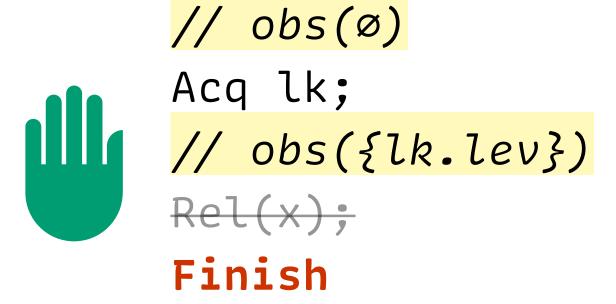
```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

A deadlock-free language, restrictive language

```
// obs(Ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(Ø)
Finish
```

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

```
// obs({x.lev})
Acq y;
Rel x;
Finish
// obs({y.lev})
Acq x;
Rel y;
Finish
```

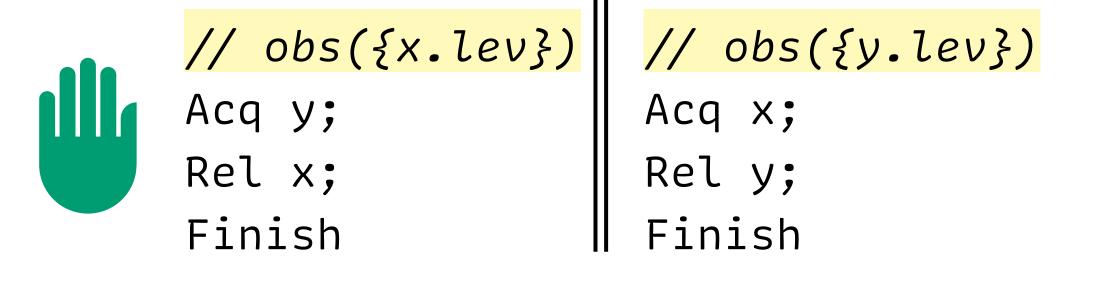


```
// obs(Ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(Ø)
Finish
```

A deadlock-free language, restrictive language

```
// obs(Ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(Ø)
Finish
```

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```



Failing level check

```
// obs(Ø)
Acq lk;
// obs({lk.lev})
Rel(x);
Finish
```

```
// obs(ø)
Acq lk;
// obs({lk.lev})
Rel lk;
// obs(ø)
Finish
```

Classic lock specifications

External knowledge of deadlock-freedom

```
// obs(Ø)
Acq x;
// obs({lk.lev})
Finish;
```

External knowledge of deadlock-freedom

```
// obs(Ø)
Acq x;
// obs({lk.lev})
Finish;
```

```
let x = NewLock () in
let f = ref true in

// obs({ø})
if !f then exit 0;
// obs({ø})
Rel x;
Finish;
```

```
let x = NewLock () in
let f = ref true in

// obs({ø})
Acq x;
// obs({lk.lev})
f := false;
Finish;
// obs({ø})
Rel x;
Finish;
```

```
let x = NewLock () in
let f = ref true in

// obs({ø})
Acq x;
// obs({lk.lev})
f := false;
Finish;
// obs({ø})
Rel x;
Finish;
```

```
let x = NewLock () in
let f = ref true in

// obs({ø})
Acq x;
// obs({lk.lev})
f := false;
Finish;

// obs({ø})
Rel x;
Finish;

// obs({ø})
Rel x;
Finish;

// obs({ø})
Finish;
// obs({ø})
Finish;
```

```
let x = NewLock () in
let f = ref true in

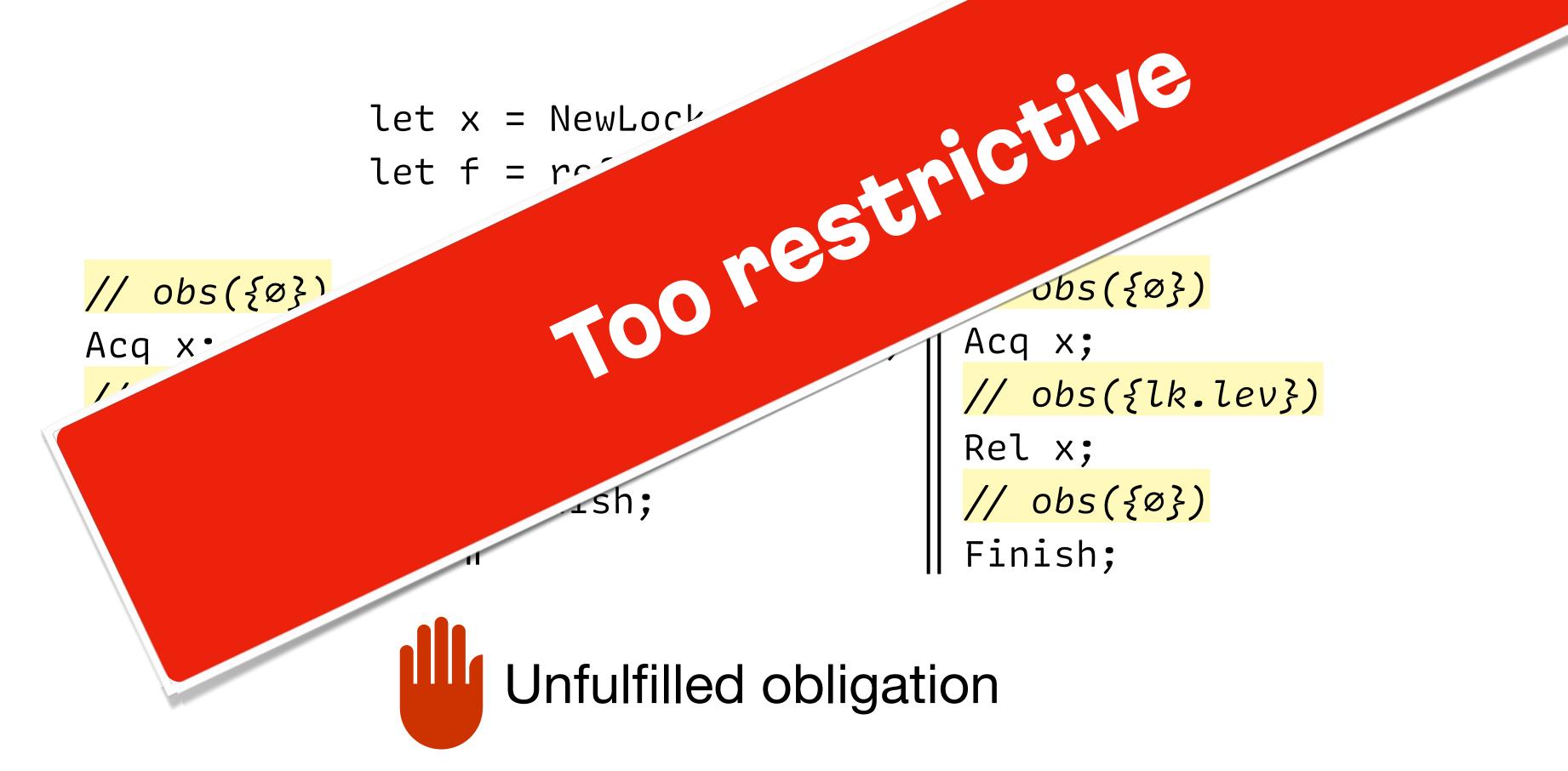
// obs({ø})
Acq x;
// obs({lk.lev})
f := false;
Finish;

// obs({ø})
Rel x;
Finish;

// obs({ø})
Rel x;
Finish;

// obs({ø})
Finish;
// obs({ø})
Finish;
```





Deadlocked?

```
let x = NewLock () in
let f = ref true in
```

```
Acq x;

// Critical section
f := false;
Finish;

if !f then exit 0;
// Critical section
Rel x;
Finish;

Acq x;
// Critical section
Rel x;
Finish;
```

```
FORK

(fork e, \sigma) \rightarrow_h ((), \sigma : \#ALIVE++, (e; Finish))
```

```
FORK

(fork e, \sigma) \rightarrow_h ((), \sigma : \#ALIVE++, (e; Finish))
```

FINISH
$$\sigma.\#\text{WAITING} = 0 \lor \sigma.\#\text{ALIVE} - 1 > \sigma.\#\text{WAITING}$$

$$(\textbf{Finish}, \sigma) \rightarrow_{\text{h}} ((), \sigma: \#\text{ALIVE} - -, \epsilon)$$

FORK
$$(\textbf{fork}\,e,\sigma) \rightarrow_{\mathsf{h}} ((),\sigma: \#\texttt{ALIVE}++,(e;\textbf{Finish})) \qquad \frac{\sigma.\texttt{HEAP}(\mathit{lk}) = \textbf{false}}{(\texttt{Acq}\,\mathit{lk},\sigma) \rightarrow_{\mathsf{h}} ((),\sigma: \texttt{HEAP}[\mathit{lk} \leftarrow \texttt{true}],\epsilon)}$$

FINISH
$$\sigma.\#\text{WAITING} = 0 \lor \sigma.\#\text{ALIVE} - 1 > \sigma.\#\text{WAITING}$$

$$(\textbf{Finish}, \sigma) \rightarrow_{\text{h}} ((), \sigma: \#\text{ALIVE} - -, \epsilon)$$

```
FORK (\operatorname{fork} e, \sigma) \rightarrow_{h} ((), \sigma : \#\operatorname{ALIVE} + +, (e; \operatorname{Finish})) \frac{\sigma.\operatorname{Heap}(lk) = \operatorname{false}}{(\operatorname{Acq} lk, \sigma) \rightarrow_{h} ((), \sigma : \operatorname{Heap}[lk \leftarrow \operatorname{true}], \epsilon)} \frac{\sigma.\operatorname{Heap}(lk) = \operatorname{true}}{\sigma.\operatorname{Heap}(lk) = \operatorname{true}} \quad \sigma.\#\operatorname{ALIVE} > \sigma.\#\operatorname{Waiting} + 1 \frac{\sigma.\operatorname{Heap}(lk) = \operatorname{true}}{(\operatorname{Acq} lk, \sigma) \rightarrow_{h} (\operatorname{WAIT} lk, \sigma : \#\operatorname{Waiting} + +, \epsilon)}
```

Finish
$$\frac{\sigma.\#\text{Waiting} = 0 \lor \sigma.\#\text{Alive} - 1 > \sigma.\#\text{Waiting}}{(\text{Finish}, \sigma) \rightarrow_{\text{h}} ((), \sigma: \#\text{Alive} - -, \epsilon)}$$

Acq-Succ

```
FORK
(\mathbf{fork}\,e,\sigma) \rightarrow_{\mathsf{h}} ((),\sigma: \#\mathsf{ALIVE} + +, (e; \mathbf{Finish})) \qquad \frac{\sigma.\mathsf{HEAP}(lk) = \mathbf{false}}{(\mathsf{Acq}\,lk,\sigma) \rightarrow_{\mathsf{h}} ((),\sigma: \mathsf{HEAP}[lk \leftarrow \mathsf{true}],\epsilon)}
\frac{\mathsf{Acg\text{-Wait}}}{\sigma.\mathsf{HEAP}(lk) = \mathsf{true}} \qquad \frac{\sigma.\#\mathsf{ALIVE} > \sigma.\#\mathsf{WaitIng} + 1}{(\mathsf{Acq}\,lk,\sigma) \rightarrow_{\mathsf{h}} (\mathsf{WAIT}\,lk,\sigma: \#\mathsf{WaitIng} + +,\epsilon)} \qquad \frac{\sigma.\mathsf{HEAP}(lk) = \mathsf{true}}{(\mathsf{WAIT}\,lk,\sigma) \rightarrow_{\mathsf{h}} (\mathsf{WAIT}\,lk,\sigma,\epsilon)}
```

FINISH
$$\sigma.\#\text{WAITING} = 0 \lor \sigma.\#\text{ALIVE} - 1 > \sigma.\#\text{WAITING}$$

$$(\textbf{Finish}, \sigma) \rightarrow_{\text{h}} ((), \sigma: \#\text{ALIVE} - -, \epsilon)$$

Fork

```
\sigma.Heap(lk) = false
(fork e, \sigma) \rightarrow_h ((), \sigma: #ALIVE++, (e; Finish))
                                                                              (Acq lk, \sigma) \rightarrow_h ((), \sigma: Heap[lk \leftarrow \text{true}], \epsilon)
Acq-Wait
                                                                                               WAIT-BLOCK
\sigma.\text{Heap}(lk) = \text{true} \sigma.\#\text{Alive} > \sigma.\#\text{Waiting} + 1
                                                                                                        \sigma.Heap(lk) = true
       (Acq lk, \sigma) \rightarrow_h (WAIT lk, \sigma: #WAITING++, \epsilon)
                                                                                                (WAIT lk, \sigma) \rightarrow_h (WAIT lk, \sigma, \epsilon)
Wait-Acq
                                                                                                FINISH
                              \sigma.Heap(lk) = false
                                                                                                 \sigma.#Waiting = 0 \vee \sigma.#Alive - 1 > \sigma.#Waiting
(WAIT lk, \sigma) \rightarrow_h ((), \sigma: Heap[lk \leftarrow true]: #Waiting--, \epsilon)
                                                                                                        (Finish, \sigma) \rightarrow_h ((), \sigma: #ALIVE--, \epsilon)
```

Acq-Succ

Agenda

Problem: classic deadlock-freedom specs are too restrictive

Solution: Parameterize modules by client-specific deadlock-freedom argument

Application: Futexes (Compare-and-sleep)

Outlook

Our solution

Obligations defined on top of the #Alive and #Waiting counters

$$\mathsf{obs}(O) \iff_{\mathcal{N}_{\mathsf{ACQ}}} \mathsf{obs}(O \uplus \{\!\!\{\lambda\}\!\!\}) * \mathsf{ob}(\lambda)$$

- Deadlock-freedom argument is passed by the client to the blocking module
 - Whenever the module has to block, the client has to show $ob(\lambda) < obs(O)$
- Argument phrased in terms of obligations
- Client-managed obligations!

```
// obs(Ø)
Acq x
// obs(Ø)
Finish;
```

```
// obs(∅)
Acq x (fun () → assert false);
// obs(∅)
Finish;
```

```
// obs(∅)
Acq x (fun () → assert false) ();
// obs(∅)
Finish;
```

Motivating example

Revisited

```
CreateOblig 0;
lock x = NewLock();
bool* f = Alloc(true);
```

"If x is true, there is an obligation"

```
// obs(Ø)
Acq x ("by inv") ());
// obs(Ø)
f := false;
Finish
// obs(Ø)
// critical section
Rel x (fun () -> DropOblig(Ø));
// obs(Ø)
Finish

// obs(Ø)
Rel x (DropOblig(1));
// obs(Ø)
Finish

Finish
```

Client-provided deadlock-freedom argument

$$P_{\top} \Longrightarrow_{\perp} \exists v. \ell \mapsto \mathsf{true} *$$

$$\begin{pmatrix} (\ell \mapsto \mathsf{true} \ _{\perp} \Longrightarrow_{\top} P) \\ \lor (\ell \mapsto \mathsf{false} \ _{\perp} \Longrightarrow_{\top} Q) \end{pmatrix}$$

$$\{P\} \ \mathsf{Rel}(\ell) \ \{Q\}$$

Cf. logically atomic triples [Jung et al. 2015], (total) atomic triples [D'Osualdo et al. 2021]

Client-provided deadlock-freedom argument

$$\{\operatorname{obs}(\emptyset)\} \text{ Finish } \{\operatorname{True}\}$$

$$\frac{\{\operatorname{obs}(O') * P\} \text{ e; Finish } \{\operatorname{obs}(\emptyset)\}}{\{\operatorname{obs}(O \uplus O') * P\} \text{ fork}(e) \{\operatorname{obs}(O)\}}$$

$$\frac{P_{\top} \bowtie_{\bot} \exists v. \, \ell \mapsto \operatorname{true} *}{\left(\ell \mapsto \operatorname{true}_{\bot} \bowtie_{\top} P\right)} \\ \vee (\ell \mapsto \operatorname{false}_{\bot} \bowtie_{\top} Q)$$

$$\frac{\{P\} \operatorname{Rel}(\ell) \{Q\}}{\{Q\}}$$

Cf. logically atomic triples [Jung et al. 2015], (total) atomic triples [D'Osualdo et al. 2021]

Client-provided deadlock-freedom argument

Cf. logically atomic triples [Jung et al. 2015], (total) atomic triples [D'Osualdo et al. 2021]

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Futexes: low-level primitive blocking

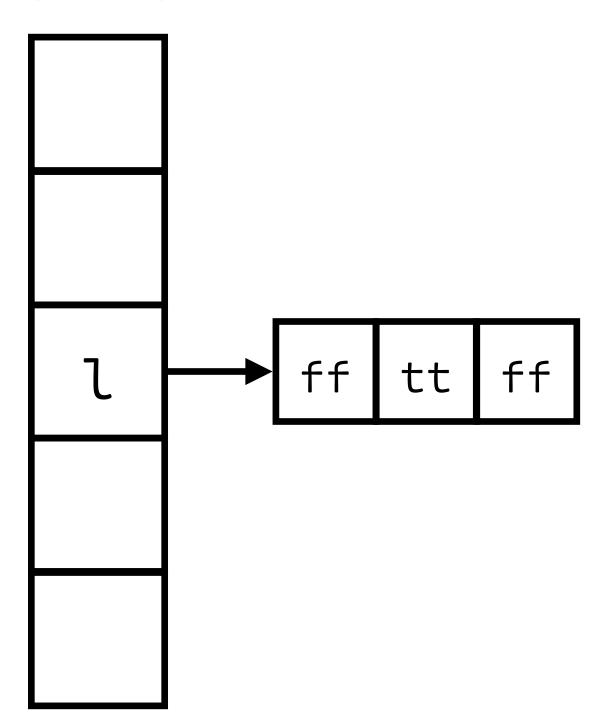
futex_wait, WaitOnAddress, os_sync_wait_on_address

- in-kernel, per-location, list of waiting threads
- futex_wait l v adds current thread to the list if !l = v
- futex_wake l wakes one waiting thread, if there are any
- spurious wakeups are possible

^{*}much simplified: only wake-one, no thread priorities, only same address space, ...

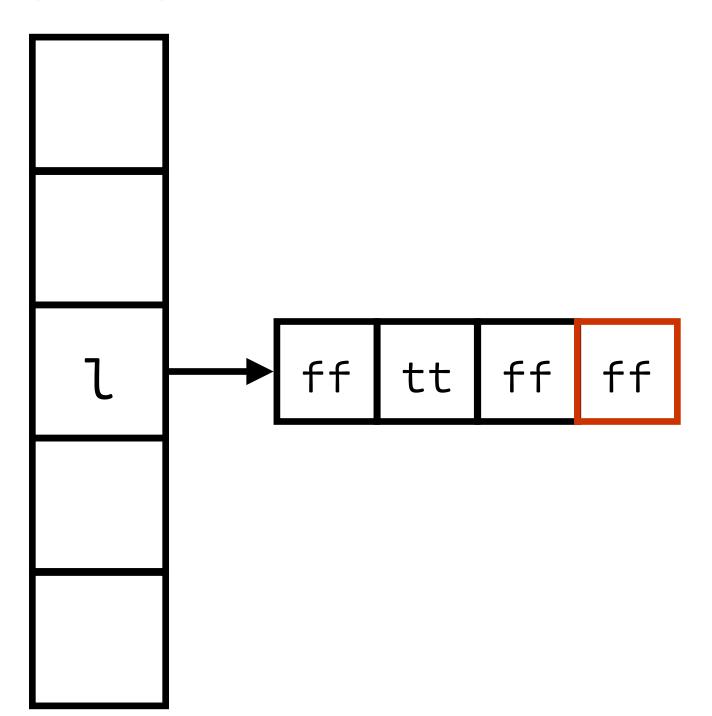
How we model the kernel-side

going to sleep:



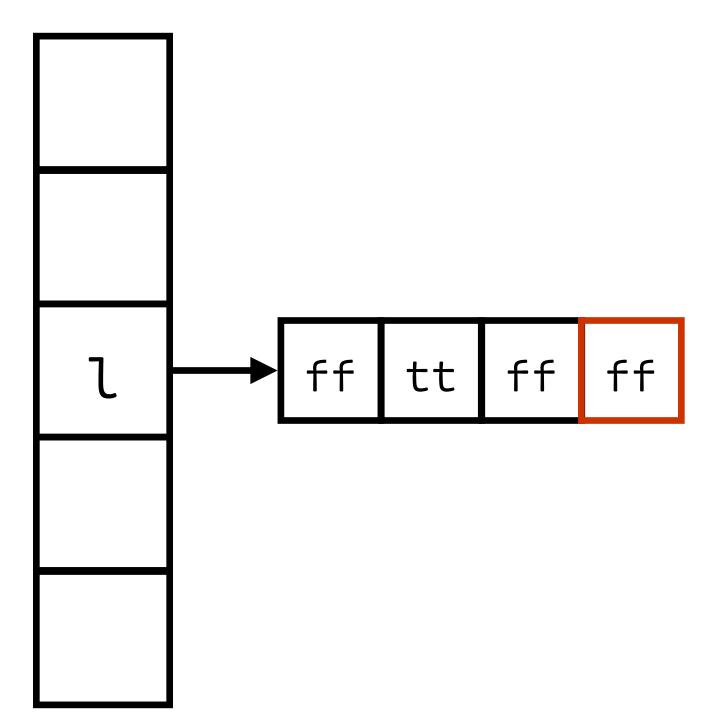
How we model the kernel-side

going to sleep:

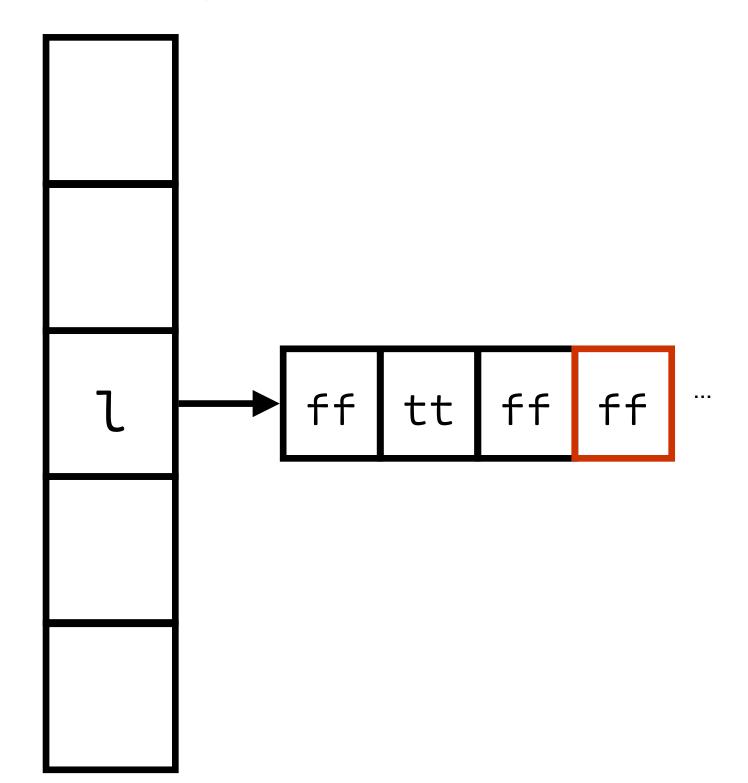


How we model the kernel-side

going to sleep:

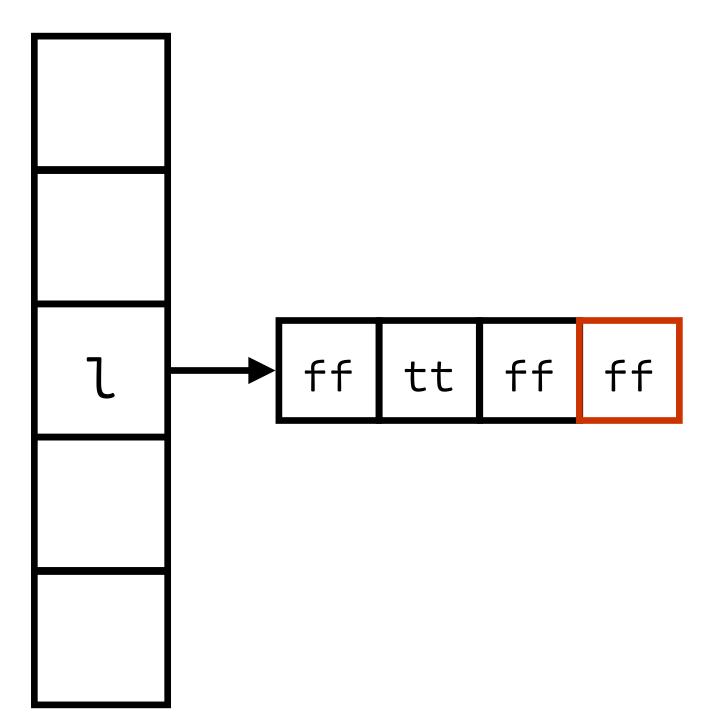


waking up:

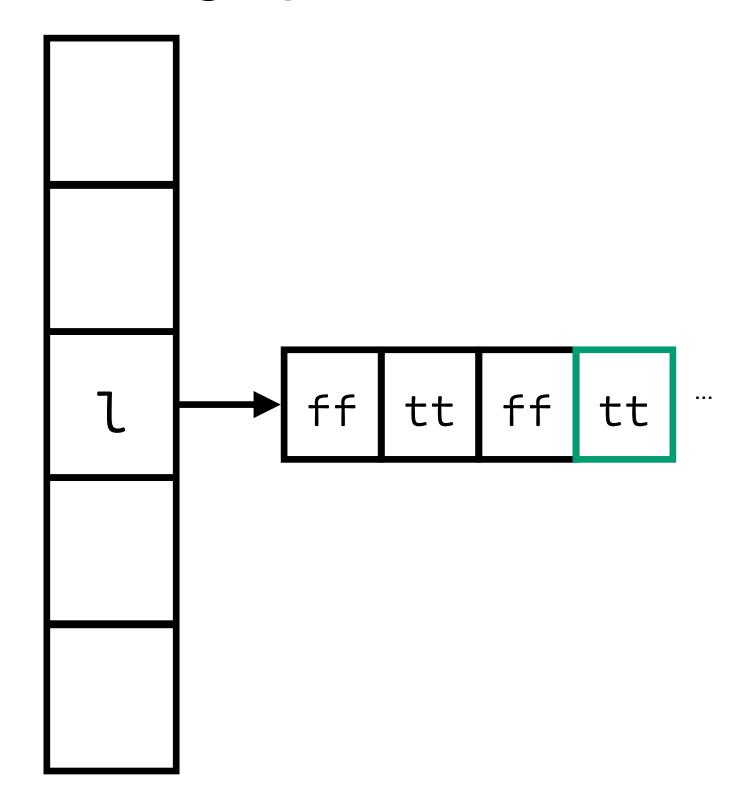


How we model the kernel-side

going to sleep:



waking up:



 $\ell \notin \text{dom}(\sigma.\text{HEAP})$

 $(\mathbf{ref}\,v,\sigma) \to_{\mathsf{h}} (\ell,\sigma: \mathrm{Heap}[\ell\leftarrow v]: \mathrm{FutexM}[\ell\leftarrow[]],\epsilon)$

$$\ell \notin \text{dom}(\sigma.\text{Heap})$$

$$(\mathbf{ref}\,v,\sigma) \to_{\mathsf{h}} (\ell,\sigma: \mathrm{Heap}[\ell\leftarrow v]: \mathrm{FutexM}[\ell\leftarrow[]],\epsilon)$$

FUTEXWAITABORT
$$\sigma.\text{Heap}(\ell) = v' \qquad v \neq v'$$

$$\boxed{ \textbf{futex_wait } \ell \ v, \sigma) \rightarrow_{\text{h}} (\text{EAGAIN}, \sigma, \epsilon) }$$

$$\ell \notin \text{dom}(\sigma.\text{HEAP})$$

$$(\mathbf{ref}\,v,\sigma) \to_{\mathsf{h}} (\ell,\sigma: \mathrm{HEAP}[\ell \leftarrow v]: \mathrm{FUTEXM}[\ell \leftarrow []],\epsilon)$$

FUTEXWAITABORT
$$\sigma.\text{Heap}(\ell) = v' \qquad v \neq v'$$

$$\boxed{ \textbf{futex_wait } \ell \ v, \sigma) \rightarrow_{\text{h}} (\text{EAGAIN}, \sigma, \epsilon) }$$

FUTEXWAITWAIT

$$\sigma$$
.Heap $(\ell) = v$
 σ .#Alive > σ .#Waiting + 1 σ .FutexM $(\ell) = B$ $n = \text{length}(B)$

 $(\mathbf{futex_wait}\ \ell\ v, \sigma) \rightarrow_\mathsf{h} (\mathbf{WAIT}(\ell, n), \sigma: \mathbf{FutexM}[\ell \leftarrow B ++[\mathbf{false}]]: \#\mathbf{WAITING} ++, \epsilon)$

$$\ell \notin \text{dom}(\sigma.\text{HEAP})$$

$$(\mathbf{ref}\,v,\sigma) \to_{\mathsf{h}} (\ell,\sigma: \mathrm{HEAP}[\ell \leftarrow v]: \mathrm{FUTEXM}[\ell \leftarrow []],\epsilon)$$

FUTEXWAITABORT
$$\sigma.\text{Heap}(\ell) = v' \qquad v \neq v'$$

$$\boxed{ \textbf{futex_wait } \ell \ v, \sigma) \rightarrow_{\text{h}} (\text{EAGAIN}, \sigma, \epsilon) }$$

FUTEXWAITWAIT

$$\sigma.\mathsf{HEAP}(\ell) = v$$

$$\sigma.\mathsf{\#ALIVE} > \sigma.\mathsf{\#WAITING} + 1 \qquad \sigma.\mathsf{FUTEXM}(\ell) = B \qquad n = \mathsf{length}(B)$$

$$(\mathsf{futex_wait} \ \ell \ v, \sigma) \to_\mathsf{h} \ (\mathsf{WAIT}(\ell, n), \sigma : \mathsf{FUTEXM}[\ell \leftarrow B ++[\mathsf{false}]] : \mathsf{\#WAITING} ++, \epsilon)$$

WAITWAIT
$$\sigma.\text{FUTEXM}(\ell)[n] = \text{false}$$

$$\overline{(\text{WAIT}(\ell, n), \sigma) \rightarrow_{\text{h}} (\text{WAIT}(\ell, n), \sigma, \epsilon)}$$

$$\ell \notin \text{dom}(\sigma.\text{HEAP})$$

$$(\mathbf{ref}\,v,\sigma) \to_{\mathsf{h}} (\ell,\sigma: \mathrm{Heap}[\ell \leftarrow v]: \mathrm{FutexM}[\ell \leftarrow []],\epsilon)$$

FUTEXWAITABORT
$$\sigma.\text{HEAP}(\ell) = v' \qquad v \neq v'$$

$$\boxed{ \textbf{futex_wait } \ell \ v, \sigma) \rightarrow_{\mathsf{h}} (\text{EAGAIN}, \sigma, \epsilon) }$$

FUTEXWAITWAIT

$$\sigma.\mathsf{HEAP}(\ell) = v$$

$$\sigma.\mathsf{\#ALIVE} > \sigma.\mathsf{\#WAITING} + 1 \qquad \sigma.\mathsf{FUTEXM}(\ell) = B \qquad n = \mathsf{length}(B)$$

$$(\mathsf{futex_wait} \ \ell \ v, \sigma) \to_\mathsf{h} \ (\mathsf{WAIT}(\ell, n), \sigma : \mathsf{FUTEXM}[\ell \leftarrow B ++[\mathsf{false}]] : \mathsf{\#WAITING} ++, \epsilon)$$

WAITWAIT
$$\sigma.\text{FUTEXM}(\ell)[n] = \textbf{false} \qquad \sigma.\text{FUTEXM}(\ell)[n] = \textbf{true}$$

$$\overline{(\text{WAIT}(\ell,n),\sigma) \rightarrow_{\text{h}} (\text{WAIT}(\ell,n),\sigma,\epsilon)} \qquad \overline{(\text{WAIT}(\ell,n),\sigma) \rightarrow_{\text{h}} ((),\sigma,\epsilon)}$$

$$\sigma$$
.FutexM(ℓ)[n] = false

(futex_wake ℓ, σ) \rightarrow_h (1, σ : FutexM(ℓ)[$n \leftarrow true$]: #Waiting--, ϵ)

$$\sigma$$
.FutexM(ℓ)[n] = false

(futex_wake ℓ, σ) \rightarrow_h (1, σ : FutexM(ℓ)[$n \leftarrow \text{true}$]: #Waiting--, ϵ)

FUTEXWAKEZERO
$$\sigma.\text{FUTEXM} = B \qquad true = \bigwedge_{b \in B} b$$

$$(\text{futex_wake } \ell, \sigma) \rightarrow_{\text{h}} (0, \sigma, \epsilon)$$

FUTEXWAKEONE

$$\sigma$$
.FutexM(ℓ)[n] = false

(futex_wake ℓ, σ) \rightarrow_h (1, σ : FutexM(ℓ)[$n \leftarrow \text{true}$]: #Waiting--, ϵ)

FUTEXWAKEZERO
$$\sigma.\text{FUTEXM} = B \qquad true = \bigwedge_{b \in B} b$$

$$(\text{futex_wake } \ell, \sigma) \rightarrow_{\text{h}} (0, \sigma, \epsilon)$$

WaitSpuriousWake

$$\sigma$$
.FutexM(ℓ)[n] = false

$$(WAIT(\ell, n), \sigma) \rightarrow_h ((), \sigma : FUTEXM(\ell)[n \leftarrow true] : \#WAITING--, \epsilon)$$

$$P_{\top} \models_{\perp} \exists v', q, B. \ \ell \xrightarrow{q} v' * \mathsf{futex}(\ell, B) *$$

$$\left(v \neq v' * (\ell \xrightarrow{q} v' * \mathsf{futex}(\ell, B) \perp \Rightarrow_{\top} Q(\mathsf{EAGAIN})) \right)$$

$$\vee \left(v = v' * ((\ell \xrightarrow{q} v' * \mathsf{futex}(\ell, B + \mathsf{false})) \right)$$

 $\{P\}$ futex_wait $\ell v \{u.Q(u)\}$

$$P_{\top} \models_{\perp} \exists v', q, B. \, \ell \stackrel{q}{\mapsto} v' * \operatorname{futex}(\ell, B) *$$

$$\left(\begin{array}{c} (v \neq v' * (\ell \stackrel{q}{\mapsto} v' * \operatorname{futex}(\ell, B) \perp \nearrow \searrow \top Q(\operatorname{EAGAIN})) \\ \vee (v = v' * (\qquad (\ell \stackrel{q}{\mapsto} v' * \operatorname{futex}(\ell, B + + [\operatorname{false}]) \qquad \qquad \downarrow \nearrow \searrow \top R(\operatorname{len}(B)))) \end{array} \right)$$

$$R(n)_{\top} \models_{\perp} \exists B_{1}, b, B_{2}. \, n = \operatorname{len}(B_{1}) * \operatorname{futex}(\ell, B_{1} + + [b] + + B_{2}) *$$

$$\left(\begin{array}{c} (b = \operatorname{false} \rightarrow \qquad \qquad (\qquad \qquad \operatorname{futex}(\ell, B_{1} + + [b] + + B_{2}) \perp \nearrow \searrow \top R(n))) \\ \wedge (b = \operatorname{true} \rightarrow (\operatorname{futex}(B_{1} + + [b] + + B_{2}) \perp \nearrow \searrow \top Q(0))) \\ \wedge (b = \operatorname{false} \rightarrow \qquad \qquad (\qquad \qquad \operatorname{futex}(B_{1} + + [\operatorname{true}] + + B_{2}) \perp \nearrow \searrow \top Q(0))) \\ \end{array} \right)$$

$$\{P\} \text{ futex_wait } \ell v \{u. Q(u)\}$$

```
P_{\top} \models_{\perp} \exists v', q, B. \ \ell \stackrel{q}{\mapsto} v' * \operatorname{futex}(\ell, B) *
\begin{pmatrix} (v \neq v' * (\ell \stackrel{d}{\mapsto} v' * \operatorname{futex}(\ell, B) \ _{\perp} \bigstar_{\top} Q(\operatorname{EAGAIN})) \end{pmatrix} \\ \vee (v = v' * ( (\ell \stackrel{d}{\mapsto} v' * \operatorname{futex}(\ell, B + [\operatorname{false}]) \ _{\perp} \bigstar_{\top} R(\operatorname{len}(B)))) \end{pmatrix}
R(n)_{\top} \models_{\perp} \exists B_{1}, b, B_{2}. \ n = \operatorname{len}(B_{1}) * \operatorname{futex}(\ell, B_{1} + + [b] + + B_{2}) *
\begin{pmatrix} (b = \operatorname{false} \to ( \operatorname{futex}(\ell, B_{1} + + [b] + + B_{2}) \ _{\perp} \bigstar_{\top} Q(0))) \end{pmatrix}
\wedge (b = \operatorname{false} \to ( \operatorname{futex}(B_{1} + + [b] + + B_{2}) \ _{\perp} \bigstar_{\top} Q(0)))
\{P\} \ \operatorname{futex\_wait} \ell v \ \{u. Q(u)\}
```

```
P_{\top} \biguplus_{\bot} \exists v', q, B. \ \ell \xrightarrow{q} v' * \operatorname{futex}(\ell, B) * \\ \left( v \neq v' * (\ell \xrightarrow{q} v' * \operatorname{futex}(\ell, B) \ _{\bot} \bigstar_{\top} Q(\operatorname{EAGAIN}) \right) \\ \vee \left( v = v' * (\exists O. \operatorname{obs}(O) * (\ell \xrightarrow{q} v' * \operatorname{futex}(\ell, B ++ [false]) * \operatorname{wobs}(\ell, \operatorname{len}(B), O) \ _{\bot} \bigstar_{\top} R(\operatorname{len}(B))) \right) \\ R(n)_{\top} \biguplus_{\bot} \exists B_{1}, b, B_{2}. \ n = \operatorname{len}(B_{1}) * \operatorname{futex}(\ell, B_{1} ++ [b] ++ B_{2}) * \\ \left( b = \operatorname{false} \to \exists O', \lambda \prec O'. \operatorname{ob}(\lambda) * \operatorname{wobs}(\ell, n, O') * (\operatorname{ob}(\lambda) * \operatorname{wobs}(\ell, n, O') * \operatorname{futex}(\ell, B_{1} ++ [b] ++ B_{2}) \ _{\bot} \bigstar_{\top} R(n)) \right) \\ \wedge \left( b = \operatorname{false} \to \exists O'. \operatorname{wobs}(\ell, n, O') * (\operatorname{obs}(O') * \operatorname{futex}(B_{1} ++ [\operatorname{true}] ++ B_{2}) \ _{\bot} \bigstar_{\top} Q(0)) \right) \\ \wedge \left( b = \operatorname{false} \to \exists O'. \operatorname{wobs}(\ell, n, O') * (\operatorname{obs}(O') * \operatorname{futex}(B_{1} ++ [\operatorname{true}] ++ B_{2}) \ _{\bot} \bigstar_{\top} Q(0)) \right)
```

 $\{P\}$ futex_wait $\ell v \{u. Q(u)\}$

$$P_{\top} \Longrightarrow_{\bot} \exists B. \, \mathsf{futex}(\ell, B) *$$

$$\left(\begin{array}{c} (\forall n. B[n] = \mathit{false} \to \exists O. \, \mathsf{wobs}(\ell, n, O) * (\mathsf{obs}(O) * \mathsf{futex}(\ell, B[n \leftarrow \mathit{true}] \, \bot \bigstar_{\top} \, Q(1))) \\ \land ((\forall n. B[n] = \mathit{true}) \to \mathsf{futex}(\ell, B) \, \bot \bigstar_{\top} \, Q(0)) \end{array} \right)$$

$$\left\{ P \right\} \, \mathbf{futex_wake} \, \ell \, \left\{ u. \, Q(u) \right\}$$

Agenda

Problem: classic deadlock-freedom specs are too restrictive

Solution: Parameterize modules by client-specific deadlock-freedom

argument

Application: Futexes (Compare-and-sleep)

Outlook

Locks

Futex

Condition variables

Locks

Channels

Semaphores

Futex

Condition variables

Locks

Channels

Semaphores

Futex

Busy-waiting

- Deadlock-free monitors
- Obligations transfer via channels

Near future: "Futexes are tricky"

Optimized futex mutex

```
class mutex3 {
     public:
      mutex() : val(0) {}
      void lock() {
        int c;
        if ((c = cmpxchg(val, 0, 1)) != 0) {
          if (c != 2)
             c = xchg(val, 2);
          while (c != 0) {
10
            futex_wait(&val, 2);
11
             c = xchg(val, 2);
12
13
14
15
16
      void unlock() {
17
        if (atomic_dec(val) != 1) {
18
           val = 0;
19
          futex_wake(&val, 1);
20
21
22
24
    private:
25
      int val;
26
    };
```

