

South China University of Technology

The Experiment Report of Machine Learning

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Subject	Software Engineering		
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1. Topic:

Logistic Regression, Linear Classification and Stochastic Gradient

Descent

2. Time:

2017-12-02 2:00-5:00 PM

3. Reporter:

任嘉宁

4. Purposes:

- Compare and understand the difference between gradient descent and stochastic gradient descent.
- Compare and understand the differences and relationships
 between Logistic regression and linear classification.
- Further understand the principles of SVM and practice on larger data.

5. Data sets and data analysis:

Experiment uses a9a of LIBSVM Data, including 32561/16281(testing) samples and each sample has 123/123 (testing) features.

6. Experimental steps:

Logistic Regression and Stochastic Gradient Descent:

- Load the training set and validation set.
- Initialize logistic regression model parameters with random

numbers.

- Select the loss function and calculate its derivation.
- Calculate gradient G toward loss function from partial samples.
- Update model parameters using different optimized methods(NAG, RMSProp, AdaDelta and Adam).
- Select the appropriate threshold, mark the sample whose predict scores greater than the threshold as positive, on the contrary as negative. Predict under validation set and get the different optimized method loss \mathcal{L}_{NAG} , $\mathcal{L}_{RMSProp}$, $\mathcal{L}_{AdaDelta}$ and \mathcal{L}_{Adam} .
- Repeate step 4 to 6 for several times, and drawing graph of \mathcal{L}_{NAG} , $\mathcal{L}_{RMSProp}$, $\mathcal{L}_{AdaDelta}$ and \mathcal{L}_{Adam} with the number of iterations.

Linear Classification and Stochastic Gradient Descent:

- Load the training set and validation set.
- Initialize SVM model parameters with random numbers.
- Select the loss function and calculate its derivation.
- Calculate gradient G toward loss function from partial samples.
- Update model parameters using different optimized

- methods(NAG, RMSProp, AdaDelta and Adam).
- Select the appropriate threshold, mark the sample whose predict scores greater than the threshold as positive, on the contrary as negative. Predict under validation set and get the different optimized method loss \mathcal{L}_{NAG} , $\mathcal{L}_{RMSProp}$, $\mathcal{L}_{AdaDelta}$ and \mathcal{L}_{Adam} .
- Repeate step 4 to 6 for several times, and drawing graph of \mathcal{L}_{NAG} , $\mathcal{L}_{RMSProp}$, $\mathcal{L}_{AdaDelta}$ and \mathcal{L}_{Adam} with the number of iterations.

7. Code:

Logistic Regression and Stochastic Gradient Descent:

NAG:

RMSProp:

Adadelta:

```
# AdaDelta
       gamma=0.95
  4 epsilon=1e-5
5 loss_AdaDeltahistory=[]
  6 test_AdaDeltahistory=[]
7 w=0.001*np.random.random((1,124))
8 G=np.zeros((1,124))
       delta_t=np.zeros((1,124))
 10 for k in range(time):
       mask=np.random.choice(X_train.shape[0],256,replace=False)
X_batch=X_train[mask]
             y_batch=y_train[mask]
AdaDeltaloss=np.mean(np.log(1+np.exp(-y_batch.reshape(-1,1)*(X_batch.dot(w.T)))))+lamda/2*(np.linalg.norm(w, 2)**2)
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            AdaDeltatestloss=np.mean(np.log(1-np.exp(-y_test.reshape(-1,1)*(X_test.dot(w.T)))))+lamda/2*(np.linalg.norm(w, 2)**2)
dw=lamda*w - np.mean((y_batch.reshape(-1,1) * X_batch)/(1 + np.exp(y_batch.reshape(-1,1) * X_batch.dot(w.T))),
             axis = 0, keepdims = True)
G=gamma*G+(1-gamma)*np.multiply(dw, dw)
             delta_w=np.multiply(np.sqrt(delta_t+epsilon)/np.sqrt(G+epsilon),dw)
w=w+delta_w
delta_t=gamma*delta_t+(1-gamma)*np.multiply(delta_w, delta_w)
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23
             loss_AdaDeltahistory.append(AdaDeltaloss)
test_AdaDeltahistory.append(AdaDeltatestloss)
 26 print(Accuracy(X_test, w))
0.8517290092746146
```

Adam:

```
1 # Adam
     heta=0.9
     датла=0.999
     eta=0.001
b eta=0.001

epsilon=le-8

7 loss_Adamhistory=[]

8 test_Adamhistory=[]

9 w=0.001 np.random.random((1,124))

10 n=np.zeros((1,124))

11 Cmp.rares((1,124))
11 G=np.zeros((1,124))
12 for k in range(time):
13 mask=np.random.chc
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25
          alpha=learning_rate*(np.sqrt(1-gamma**(k+1)))/(1-beta**(k+1))
w=w-alpha*m/(np.sqrt(G+epsilon))
          loss_Adamhistory.append(Adamloss)
test_Adamhistory.append(Adamtestloss)
27 | 28 | print(Accuracy(X_test,w))
```

Linear Classification and Stochastic Gradient Descent:

NAG:

```
v=np.zeros((1,124))
      gamma=0.9
w=np.random.random((1,124))*0.001
 6 learning_rate=0.05
7 loss_NAGhistory=[]
      test_NAGhistory=[]
10 for k in range (time):
           mask=np.random.choice(X_train.shape[0], 256, replace=False)
X_batch=X_train[mask]
             N_Datch-A_train[mask]
dw=np.zeros((1, X_batch. shape[1]))
NAGloss = lamda * 0.5*(np. linalg.norm(w, 2)**2)+np. mean(np. maximum(1-y_batch. reshape(-1, 1)*(X_batch. dot(w.T)), 0))
NAGtestloss = lamda * 0.5*(np. linalg.norm(w, 2)**2)+np. mean(np. maximum(1-y_test.reshape(-1, 1)*(X_test. dot(w.T)), 0))
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              loss_NAGhistory.append(NAGloss)
test_NAGhistory.append(NAGtestloss)
              for i in range(%_batch.shape[0]):
    if 1-y_batch[i]*(%_batch[i].dot((w-gamma*v).T))>=0:
              dw += -y_batch[i] *X_batch[i].reshape((1,124))
dw= dw/X_batch.shape[0] + lamda*(w-gamma*v)
              v= {\tt gamma*v+learning\_rate*dw}
26 print(Accuracy(X_test, w))
```

0.8480437319574965

RMSProp:

```
1 # RMSProp
       датта=0.95
      epsilon=1e-8
 5 learning_rate=0.005
6 w=np.random.random((1,124))*0.001
     G=np.zeros((1,124))
loss_RMSProphistory=[]
 9 test_RMSProphistory=[]
11 for k in range (time):
             mask=np.random.choice(X_train.shape[0], 256, replace=False)
             X batch=X train[mask]
14
15
              y_batch=y_train[mask]
               dw=np. zeros((1, X_batch. shape[1]))
              RMSPropless = lamda * 0.5*(np. linalg.norm(w, 2)**2)+np. mean(np. maximum(1-y_batch. reshape(-1, 1)*(K_batch. dot(w.T)), 0))
RMSProprestloss = lamda * 0.5*(np. linalg.norm(w, 2)**2)+np. mean(np. maximum(1-y_test. reshape(-1, 1)*(K_test. dot(w.T)), 0))
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              loss_RMSProphistory.append(RMSProploss)
test_RMSProphistory.append(RMSProptestloss)
              for i in range(X_batch.shape[0]):
    if 1-y_batch[i]*(X_batch[i].dot(w.T))>=0:
             dw += "y_batch[i] "X_batch[i]. dot(w.1)) =0:
dw += "y_batch[i] "X_batch[i].reshape((1,124))
dw = dw/X_batch.shape(0]+ landa"w
G=gamma"G+(1-gamma) "np. multiply(dw, dw)
w=w np. multiply(learning_rate/np.sqrt(G+epsilon), dw)
26 | print(Accuracy(X_test,w))
```

Adadelta:

0.8482279958233524

Adam:

8. The initialization method of model parameters:

W: set with random numbers and multiply 0.001;

G, v, m, delta t :set all to zeros.

9. The selected loss function and its derivatives:

Logistic Regression and Stochastic Gradient Descent:

$$\mathcal{L} = \frac{1}{n} \sum_{i=1}^{n} log(1 + e^{-y_i w^T x_i}) + \frac{\lambda}{2} ||w||_2^2$$
$$\frac{\partial \mathcal{L}}{\partial w} = -\frac{1}{n} \sum_{i=1}^{n} \frac{y_i x_i}{1 + e^{y_i w^T x_i}} + \lambda w$$

Linear Classification:

$$\mathcal{L} = \frac{\lambda ||w||^2}{2} + \frac{1}{n} \sum_{i=1}^{n} \max(0, 1 - yi(w^T xi))$$

$$g_w(xi) = -yixi \quad 1 - yi(w^T xi) \ge 0$$

$$g_w(xi) = 0 \quad 1 - yi(w^T xi) < 0$$

$$\frac{\partial \mathcal{L}}{\partial w} = \frac{1}{n} \sum_{i=1}^{n} g_{w}(xi) + \lambda w$$

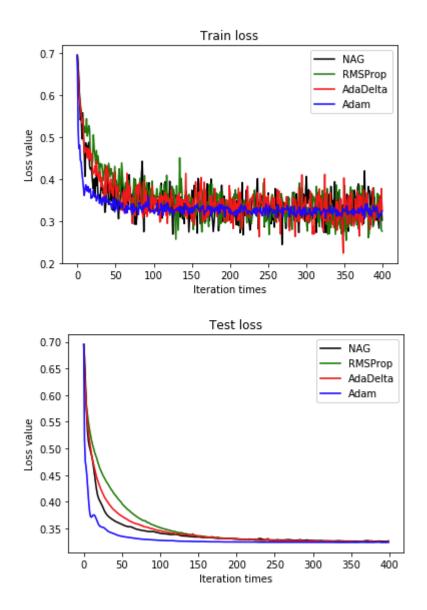
10.Experimental results and curve:

Logistic Regression and Stochastic Gradient Descent:

 $\lambda = 0$, Iteration times=400

	Hyper-parameter selection	Predicted Results (Best Results)
NAG	gamma=0.9 learning_rate=0.05 Batch_size=256	23 print(Accuracy(X_test,w)) 0.8506848473680978
RMSProp	learning_rate=0.005 gamma=0.9 epsilon=1e-8 Batch_size=256	27 print(Accuracy(X_test,w)) 0.8503777409250046
AdaDelta	gamma=0.95 epsilon=1e-5 Batch_size=256	26 print(Accuracy(X_test,w)) 0.8517290092746146
Adam	beta=0.9 gamma=0.999 eta=0.001 epsilon=1e-8	28 print(Accuracy(X_test,w)) 0.8510533750998096
	Batch_size=4096	

Loss curve:



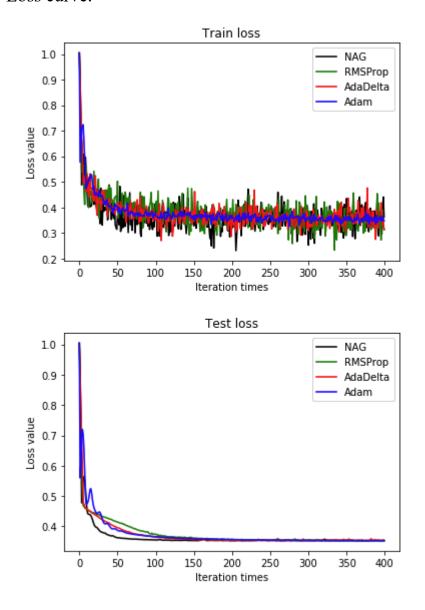
Linear Classification and Stochastic Gradient Descent:

 $\lambda = 0$, Iteration times=400

	Hyper-parameter selection	Predicted Results (Best Results)
NAG	gamma=0.9 learning_rate=0.05 Batch_size=256	27 print(Accuracy(X_test,w)) 0.8480437319574965
RMSPro p	3 gamma=0.95 4 epsilon=1e-8 5 learning_rate=0.005 Batch_size=256	27 print(Accuracy(X_test,w)) 0.8502548983477674

AdaDelt a	gamma=0.95 epsilon=1e-5 Batch_size=512	28 print(Accuracy(X_test,w)) 0.8482279958233524
Adam	3 beta=0.9 4 gamma=0.999 5 eta=0.001 6 epsilon=1e-8 7 learning_rate=0.001 Batch_size=4096	31 print(Accuracy(X_test,w)) 0.8494564215957251

Loss curve:



11. Results analysis:

1. When the Regular modulus equal to 0, the accuracy is the

- highest. And the loss is much smaller.
- 2. Batch size is association with the amplitude of train loss, the larger the batch size, the smaller the amplitude of train loss.
- 3. If learning_rate in NAG =0.001, NAG should iterate a lot of time to convergence(probably 3000times), so I change the learning_rate to 0.05 in NAG. And the iteration time reduce a lot. So do the RMSProp, so I change the learning_rate to 0.005 in RMSProp.
- 4. If epsilon in AdaDelta = 1e-8, AdaDelta should iterate a lot of time to convergence(probably 3000times), so I change the epsilon to 1e-5, it perform much better.

12. Similarities and differences between logistic regression and linear classification:

Both methods are common classification algorithms. Look at the objective function, the difference is that logistic loss is used in logistic regression, svm uses hinge loss. The purpose of these two loss functions is to increase the weight of the data points that have a greater impact on the classification and reduce the weight of the data points with less classification. SVM approach is to consider only support vectors, which is the most relevant and classification of the few points to learn classifier. Logistic regression reduces the weights of points farther away from the classification plane

through nonlinear mapping, and increases the weight of the data points most relevant to the classification.

13.Summary:

The algorithm behaves differently on different models and also has a relationship with hyperparameter learning rate η and so on.