

Heuristic Function

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I tested my agent in a Macbook Air 13" - so not a very powerful CPU. My searches were always running out of time and returning sub-optimal moves. I guess it is a great way to test an algorithm.

I ended up choosing: *Number of My Moves minus Number of Opponent's Moves*.

These were my attempts to select the heuristic function:

Number of My Moves

My first attempt of a heuristic function was to use *Number of my moves*. This was the function that was used in class for most examples, and a great starting point.

The result was that my agent was slightly worse than 'ID_Improved' agent, as shown below:

```
*****
Evaluating: ID_Improved
*****
```

Playing Matches:

Match 1:	ID_Improved	vs	Random	Result: 16 to 4
Match 2:	ID_Improved	vs	MM_Null	Result: 18 to 2
Match 3:	ID_Improved	vs	MM_Open	Result: 12 to 8
Match 4:	ID_Improved	vs	MM_Improved	Result: 13 to 7
Match 5:	ID_Improved	vs	AB_Null	Result: 19 to 1
Match 6:	ID_Improved	vs	AB_Open	Result: 9 to 11
Match 7:	ID_Improved	vs	AB_Improved	Result: 11 to 9

Results:

ID_Improved	70.00%
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```
*****
Evaluating: Student
*****
```

Playing Matches:

Match 1:	Student	vs	Random	Result: 18 to 2
Match 2:	Student	vs	MM_Null	Result: 18 to 2
Match 3:	Student	vs	MM_Open	Result: 9 to 11
Match 4:	Student	vs	MM_Improved	Result: 10 to 10
Match 5:	Student	vs	AB_Null	Result: 17 to 3
Match 6:	Student	vs	AB_Open	Result: 12 to 8
Match 7:	Student	vs	AB_Improved	Result: 10 to 10

Results:

Student 67.14%

Number of My Moves minus Number of Opponent's Moves

I then changed it to "Number of my moves" minus "Number of Opponent's moves". This has led to significant improvement of my agent, as shown below:

```
*****  
Evaluating: ID_Improved  
*****
```

Playing Matches:

Match 1: ID_Improved vs Random Result: 16 to 4
Match 2: ID_Improved vs MM_Null Result: 17 to 3
Match 3: ID_Improved vs MM_Open Result: 10 to 10
Match 4: ID_Improved vs MM_Improved Result: 7 to 13
Match 5: ID_Improved vs AB_Null Result: 19 to 1
Match 6: ID_Improved vs AB_Open Result: 9 to 11
Match 7: ID_Improved vs AB_Improved Result: 13 to 7

Results:

ID_Improved 65.00%

```
*****  
Evaluating: Student  
*****
```

Playing Matches:

Match 1: Student vs Random Result: 18 to 2
Match 2: Student vs MM_Null Result: 19 to 1
Match 3: Student vs MM_Open Result: 15 to 5

tournament.py:100: UserWarning: One or more agents lost a match this round due to timeout. The get_move() function must return before time_left() reaches 0 ms. You will need to leave some time for the function to return, and may need to increase this margin to avoid timeouts during tournament play.

warnings.warn(TIMEOUT_WARNING)

Match 4: Student vs MM_Improved Result: 14 to 6
Match 5: Student vs AB_Null Result: 17 to 3
Match 6: Student vs AB_Open Result: 16 to 4
Match 7: Student vs AB_Improved Result: 13 to 7

Results:

Student 80.00%

Even though I have gained some significant improvement, my agent ran out of time in one of the matches, without returning a move. I went back to the code and found out why - and fixed it.

Number of My Moves minus 2 x Number of Opponent's Moves

I then went and weighted the opponent's moves more, like it was suggested in class.

The improvement was not significant, as I expected.

```
*****
Evaluating: ID_Improved
*****
```

Playing Matches:

```
-----
Match 1: ID_Improved vs Random Result: 18 to 2
Match 2: ID_Improved vs MM_Null Result: 19 to 1
Match 3: ID_Improved vs MM_Open Result: 11 to 9
Match 4: ID_Improved vs MM_Improved Result: 13 to 7
Match 5: ID_Improved vs AB_Null Result: 17 to 3
Match 6: ID_Improved vs AB_Open Result: 8 to 12
Match 7: ID_Improved vs AB_Improved Result: 13 to 7
```

Results:

```
-----
ID_Improved 70.71%
```

```
*****
Evaluating: Student
*****
```

Playing Matches:

```
-----
Match 1: Student vs Random Result: 15 to 5
Match 2: Student vs MM_Null Result: 15 to 5
Match 3: Student vs MM_Open Result: 12 to 8
Match 4: Student vs MM_Improved Result: 14 to 6
Match 5: Student vs AB_Null Result: 18 to 2
Match 6: Student vs AB_Open Result: 12 to 8
Match 7: Student vs AB_Improved Result: 14 to 6
```

Results:

```
-----
Student 71.43%
```

This could have been just some random variation, so I tried again:

```
*****
Evaluating: ID_Improved
*****
```

Playing Matches:

```
-----
Match 1: ID_Improved vs Random Result: 18 to 2
```

Match 2:	ID_Improved	vs	MM_Null	Result:	18 to 2
Match 3:	ID_Improved	vs	MM_Open	Result:	13 to 7
Match 4:	ID_Improved	vs	MM_Improved	Result:	11 to 9
Match 5:	ID_Improved	vs	AB_Null	Result:	19 to 1
Match 6:	ID_Improved	vs	AB_Open	Result:	13 to 7
Match 7:	ID_Improved	vs	AB_Improved	Result:	13 to 7

Results:

ID_Improved 75.00%

Evaluating: Student

Playing Matches:

Match 1:	Student	vs	Random	Result:	17 to 3
Match 2:	Student	vs	MM_Null	Result:	20 to 0
Match 3:	Student	vs	MM_Open	Result:	15 to 5
Match 4:	Student	vs	MM_Improved	Result:	11 to 9
Match 5:	Student	vs	AB_Null	Result:	18 to 2
Match 6:	Student	vs	AB_Open	Result:	12 to 8
Match 7:	Student	vs	AB_Improved	Result:	8 to 12

Results:

Student 72.14%

So, this is definitely not the best heuristic function.

(Back to) Number of My Moves minus Number of Opponent's Moves

So, I went back to option 2, as it appears to be better.

Indeed, my agent's best game occurs when it is focused in winning at the same time that it tries to stop the opponent from wining.

Evaluating: ID_Improved

Playing Matches:

Match 1:	ID_Improved	vs	Random	Result:	18 to 2
Match 2:	ID_Improved	vs	MM_Null	Result:	17 to 3
Match 3:	ID_Improved	vs	MM_Open	Result:	11 to 9
Match 4:	ID_Improved	vs	MM_Improved	Result:	10 to 10
Match 5:	ID_Improved	vs	AB_Null	Result:	20 to 0
Match 6:	ID_Improved	vs	AB_Open	Result:	14 to 6
Match 7:	ID_Improved	vs	AB_Improved	Result:	15 to 5

Results:

ID_Improved 75.00%

Evaluating: Student

Playing Matches:

Match 1: Student vs Random Result: 19 to 1
Match 2: Student vs MM_Null Result: 19 to 1
Match 3: Student vs MM_Open Result: 16 to 4
Match 4: Student vs MM_Improved Result: 13 to 7
Match 5: Student vs AB_Null Result: 16 to 4
Match 6: Student vs AB_Open Result: 17 to 3
Match 7: Student vs AB_Improved Result: 11 to 9

Results:

Student 79.29%

2 x Number of My Moves minus Number of Opponent's Moves

And, in, one last attempt, I tried to weigh "my moves" (multiplying to by 2).

Evaluating: ID_Improved

Playing Matches:

Match 1: ID_Improved vs Random Result: 17 to 3
Match 2: ID_Improved vs MM_Null Result: 18 to 2
Match 3: ID_Improved vs MM_Open Result: 10 to 10
Match 4: ID_Improved vs MM_Improved Result: 14 to 6
Match 5: ID_Improved vs AB_Null Result: 15 to 5
Match 6: ID_Improved vs AB_Open Result: 12 to 8
Match 7: ID_Improved vs AB_Improved Result: 14 to 6

Results:

ID_Improved 71.43%

Evaluating: Student

Playing Matches:

tournament.py:100: UserWarning: One or more agents lost a match this round due to timeout. The get_move() function must return before time_left() reaches 0 ms. You will need to leave some time for the

function to return, and may need to increase this margin to avoid timeouts during tournament play.

```
warnings.warn(TIMEOUT_WARNING)
```

Match 1:	Student	vs	Random	Result: 18 to 2
Match 2:	Student	vs	MM_Null	Result: 16 to 4
Match 3:	Student	vs	MM_Open	Result: 11 to 9
Match 4:	Student	vs	MM_Improved	Result: 14 to 6
Match 5:	Student	vs	AB_Null	Result: 18 to 2
Match 6:	Student	vs	AB_Open	Result: 10 to 10
Match 7:	Student	vs	AB_Improved	Result: 10 to 10

Results:

Student 69.29%

The result was disappointing. I tried once more:

Evaluating: ID_Improved

Playing Matches:

Match 1:	ID_Improved	vs	Random	Result: 19 to 1
Match 2:	ID_Improved	vs	MM_Null	Result: 18 to 2
Match 3:	ID_Improved	vs	MM_Open	Result: 11 to 9
Match 4:	ID_Improved	vs	MM_Improved	Result: 12 to 8
Match 5:	ID_Improved	vs	AB_Null	Result: 19 to 1
Match 6:	ID_Improved	vs	AB_Open	Result: 10 to 10
Match 7:	ID_Improved	vs	AB_Improved	Result: 12 to 8

Results:

ID_Improved 72.14%

Evaluating: Student

Playing Matches:

Match 1:	Student	vs	Random	Result: 18 to 2
Match 2:	Student	vs	MM_Null	Result: 16 to 4
Match 3:	Student	vs	MM_Open	Result: 12 to 8
Match 4:	Student	vs	MM_Improved	Result: 12 to 8
Match 5:	Student	vs	AB_Null	Result: 18 to 2
Match 6:	Student	vs	AB_Open	Result: 13 to 7
Match 7:	Student	vs	AB_Improved	Result: 11 to 9

Results:

Student 71.43%

The result was still disappointing. I went back to option 2:

(Back to) Number of My Moves minus Number of Opponent's Moves

```
*****
Evaluating: ID_Improved
*****
```

Playing Matches:

```
-----
Match 1: ID_Improved vs Random      Result: 14 to 6
Match 2: ID_Improved vs MM_Null     Result: 18 to 2
Match 3: ID_Improved vs MM_Open     Result: 14 to 6
Match 4: ID_Improved vs MM_Improved Result: 8 to 12
Match 5: ID_Improved vs AB_Null     Result: 14 to 6
Match 6: ID_Improved vs AB_Open     Result: 14 to 6
Match 7: ID_Improved vs AB_Improved Result: 13 to 7
```

Results:

```
-----
ID_Improved      67.86%
```

```
*****
Evaluating: Student
*****
```

Playing Matches:

```
-----
Match 1: Student vs Random      Result: 17 to 3
Match 2: Student vs MM_Null     Result: 18 to 2
Match 3: Student vs MM_Open     Result: 16 to 4
Match 4: Student vs MM_Improved Result: 13 to 7
Match 5: Student vs AB_Null     Result: 19 to 1
Match 6: Student vs AB_Open     Result: 16 to 4
Match 7: Student vs AB_Improved Result: 10 to 10
```

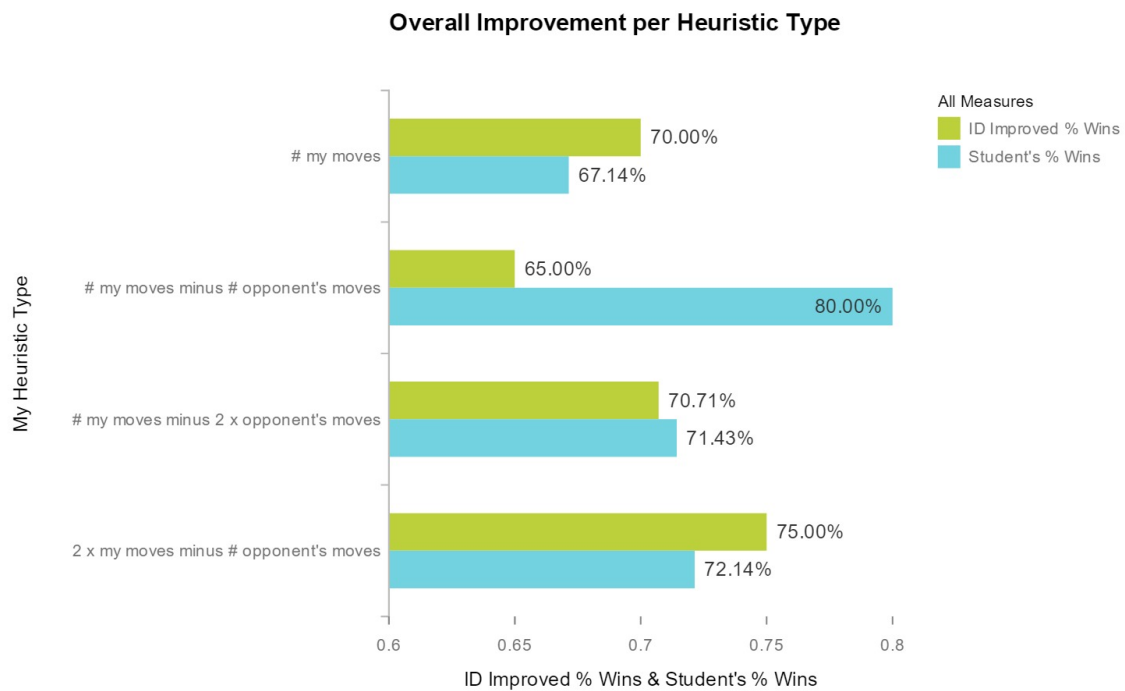
Results:

```
-----
Student          77.86%
(aind) Rens-MacBook-Air:AIND-Isolation Ren$
```

The results are summarized on the visualization below:

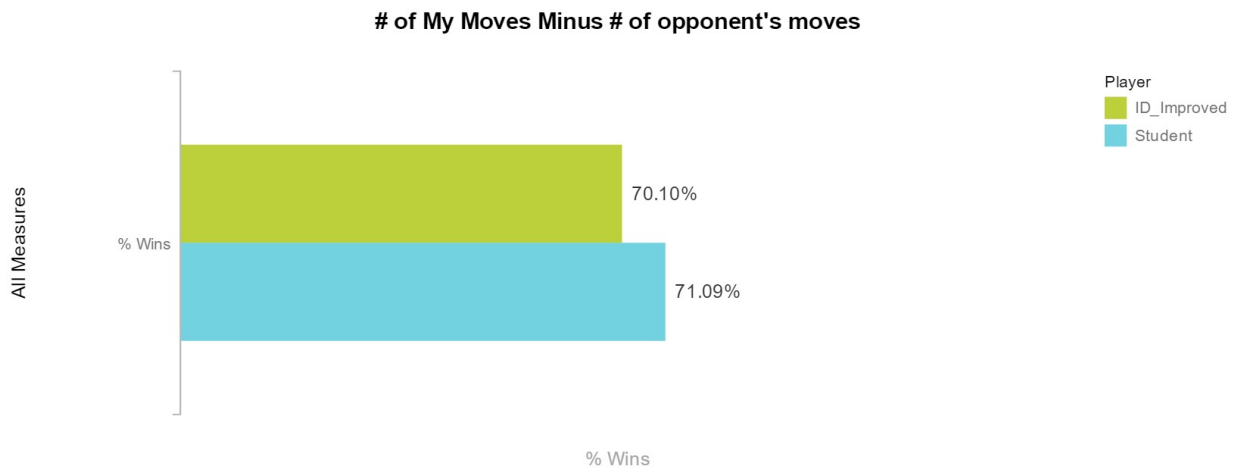
Choosing a Heuristic Function

The best improvement was achieved by using the function 'Number of My Moves Minus Number of Opponent's Moves' - the Student player won 80% of the times when compared with the benchmark 65%



Why I selected *My moves minus Opponent's Moves*

I then ran the Tournament script 38 times to confirm that it would consistently produce good results. While it did not produce the same results as originally (bringing the number of wins from 65% to 80%), there was consistent improvement over the benchmark “ID Improved” measure, as shown in the visualization below:



Running "Number of My Moves Minus Number of Opponent's Moves" over 38 tournaments produced positive results (the student was consistently better), but not as encouraging as the 80% over 65% that I obtained the first time.

Looking at the game it is not difficult to understand why this heuristic function is the best one:

1. The heuristic accurately balances the need to be aggressive (i.e. choosing winning moves) with being defensive (choosing moves that make it harder for the opponent to pick a winning move). Any other choice would have favoured one option over the other.
2. It is a simple calculation - so, the agent will have the opportunity to calculate this simple function many times before running out of time over an iterative deepening cycle. This function is less simple than the first option (number of my moves), but is simpler than the others that involve multiplications. This may appear irrelevant, but when the agent may have to calculate this function millions (or billions) of times, a simple function allows for more trials within the available time.
3. And obviously - this heuristic function has proven itself. It has consistently produced better results than the others. I also tried the function on a faster computer - my MacBook Pro with faster CPU - and the results were consistent - the level of improvement was the same. As my former manager used to say, there is nothing like “runs on the board” to prove a point.