

# Learning Sum-Product Networks

## Master's Dissertation

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SPSAS 2019



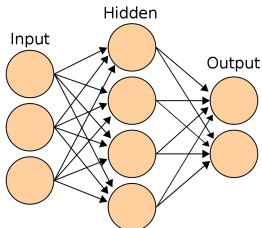
Supported by CNPq Grant 133787/2019-2

# Motivation

What if you could have...

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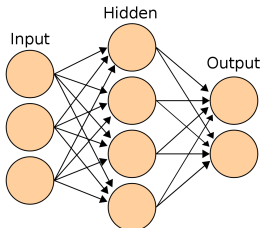
What if you could have...



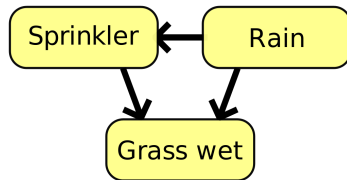
The expressivity and toolset of  
neural networks...

# Motivation

What if you could have...



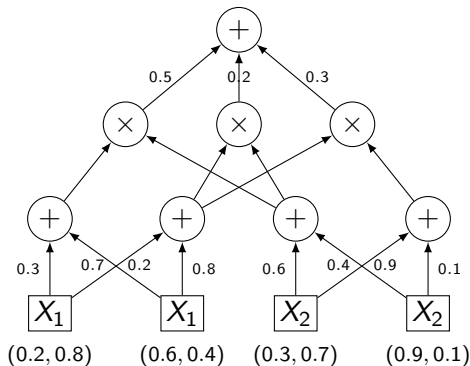
The expressivity and toolset of neural networks...



... and the interpretability and probabilistic semantics of PGMs.

# Sum-Product Network (SPN)

Sum-product networks (SPNs) are density estimators with a deep architecture.



# Learning SPNs

## Structure

- Poon dense architecture
- LearnSPN
- Clustering architecture
- Random-Tensorized SPNs
- ID-SPNs
- SPNs + Chow-Liu Trees

## Parameter

- Gradient descent;
- Expectation-Maximization;
- Extended Baum-Welch;
- Collapsed Variational Inference;
- Concave-convex procedure;
- Bayesian Moment Matching.

# Some results

Not quite there yet on the discriminative side...

MNIST classification accuracy results

LearnSPN	ID-SPN	SPN-SVD	DSPN-SVD
81.8%	84.4%	85%	97.6%
SPN-TH	RAT-SPN	Prometheus	DC-SPN
98.34%	98.19%	98.37%	99.19%

...but gradually getting better.

## More results

SPNs shine on generative tasks!



Figure: Image reconstruction







# Applications

SPNs have reached incredible results in different fields:




- Image segmentation, classification and completion
- Protein folding
- Speech recognition
- Natural language processing
- Semantic mapping and control in robotics
- Activity recognition
- Semantic Web

# Thank you!

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