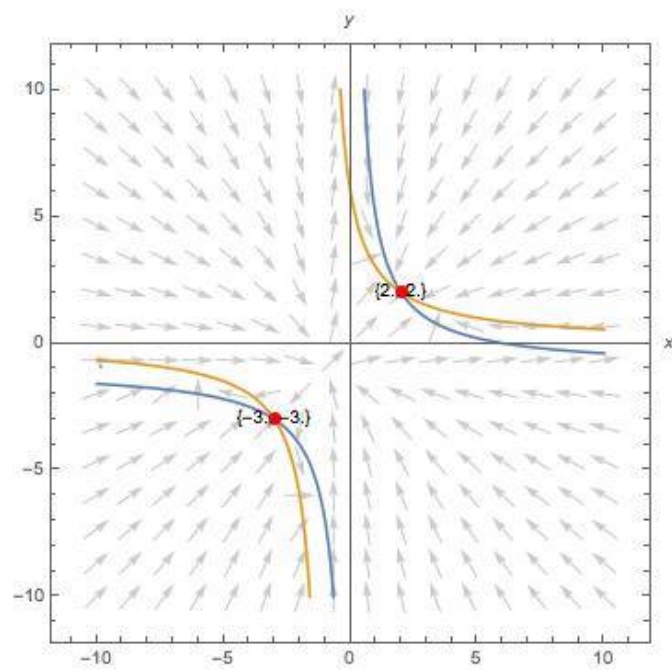
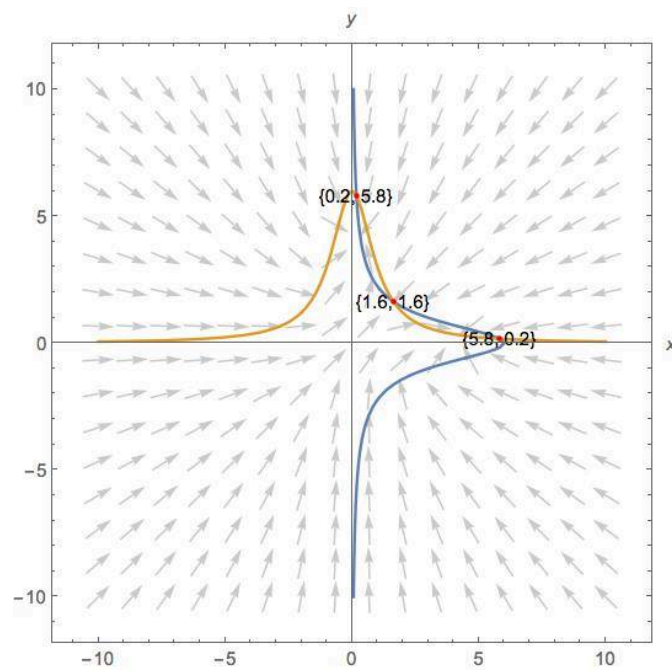


1.

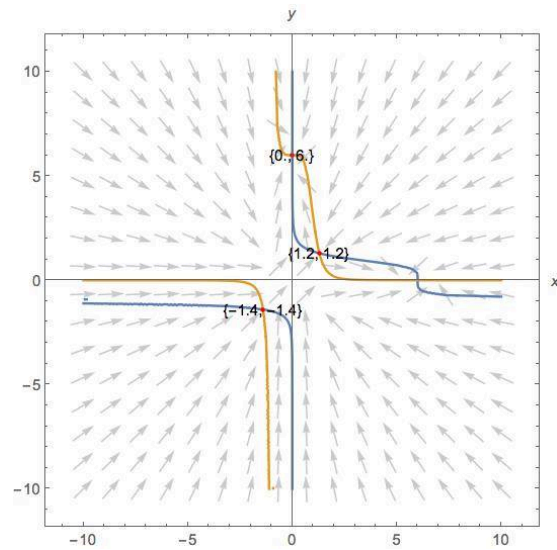
$n=1$  (2,2) stable



$n=2$  (0.2, 5.8), (5.8, 0.2) stable/ (1.6, 1.6) unstable



n=5 (0,6),(6,0) stable/ (1.2,1.2) unstable



1b.

$$\frac{dm}{dt} = \alpha_m(1 - \text{Probability}_{goff}) - \gamma_m[m]$$

$$\frac{dm}{dt} = \alpha_m(1 - \text{Probability}_{A_{unbound}} * \text{Probability}_{P_{unbound}}) - \gamma_m[m]$$

$$\frac{dm}{dt} = \alpha_m \left( 1 - \frac{[A]}{k1 + [A]} * \frac{[P]^2}{k2^2 + [P]^2} \right) - \gamma_m[m]$$

$$[m]_{ss} = \frac{\alpha_m}{\gamma_m} \left( \frac{[A]}{k1 + [A]} * \frac{[P]^2}{k2^2 + [P]^2} \right)$$

$$\frac{dP}{dt} = \frac{\alpha_m \alpha_p}{\gamma_m} \left( 1 - \frac{[A]}{k1 + [A]} * \frac{[P]^2}{k2^2 + [P]^2} \right) - \gamma_p[P]$$

$$\frac{dP}{dt} = \frac{\alpha_m \alpha_p}{\gamma_m} \left( \frac{[A]}{k1 + [A]} + \frac{[P]^2}{k2^2 + [P]^2} - \frac{k1 * k2^2}{(k1 + [A])(k2^2 + [P]^2)} \right) - \gamma_p[P]$$

2b.

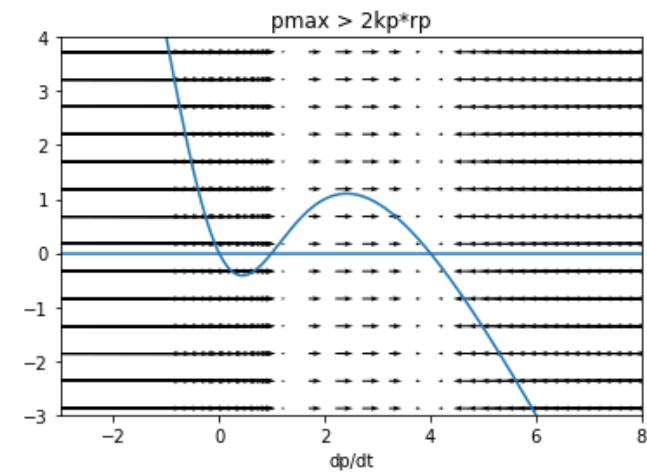
$$\frac{dP}{dt} = P_{max} \left( \frac{[P]^2}{k2^2 + [P]^2} \right) - \gamma_p[P] = 0$$

$$P_{max} \left( \frac{[P]^2}{k2^2 + [P]^2} \right) = \gamma_p[P]$$

$$\frac{dP}{dt} = 0 \rightarrow [P] = 0, \quad \frac{P_{max} \pm \sqrt{P_{max}^2 - 4\gamma_p^2 k2^2}}{2\gamma_p}$$

When  $P_{max} > 2\gamma_p k^2$ , 3 equilibrium points.

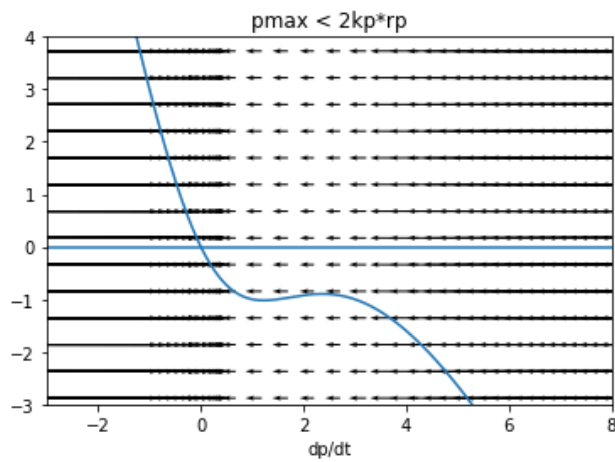
( $k_2=k_p$ )



$P_{max}=10, k=2, r_p=2$

>> 2 stable points, 1 unstable, which is  $P = \frac{P_{max} - \sqrt{P_{max}^2 - 4\gamma_p^2 k^2}}{2\gamma_p}$ .

When  $P_{max} < 2\gamma_p k^2$ , 1 equilibrium point. only when  $P=0$



$P_{max}=10, k=3, r_p=2$

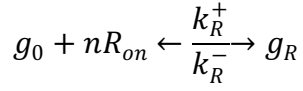
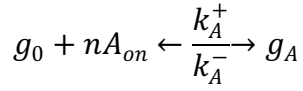
>>  $P=0$ , stable point.

3a

$$A_{off} + I \leftarrow \frac{k_{AI}^+}{k_{AI}^-} \rightarrow A_{on}$$

$$R_{on} + I \leftarrow \frac{k_{RI}^+}{k_{RI}^-} \rightarrow A_{on}$$

3b.



$$[g_A]_{ss} = \frac{k_A^+}{k_A^-} [g_0] [A]^n$$

$$[g_R]_{ss} = \frac{k_R^+}{k_R^-} [g_0] [R]^n$$

$$\frac{g_A}{g_{TOT}} = \frac{\frac{k_A^+}{k_A^-} [g_0] [A]^n}{[g_0] + \frac{k_A^+}{k_A^-} [g_0] [A]^n + \frac{k_R^+}{k_R^-} [g_0] [R]^n}$$

$$\frac{g_A}{g_{TOT}} = \frac{\frac{k_A^+}{k_A^-} [A]^n}{1 + \frac{k_A^+}{k_A^-} [A]^n + \frac{k_R^+}{k_R^-} [R]^n}$$

3c.

$$[A_{on}]_{ss} = \frac{k_{AI}^+}{k_{AI}^-} [A_{off}] [I]$$

$$[R_{on}]_{ss} = \frac{k_{RI}^-}{k_{RI}^+} \frac{[R_{off}]}{[I]}$$

$$\frac{k_{AI}^+}{k_{AI}^-} = k_{AI}, \quad \frac{k_{RI}^-}{k_{RI}^+} = k_{RI}^{-1}$$

$$\frac{g_A}{g_{TOT}} = \frac{k_A k_{AI}^n [A_{off}]^n [I]^n}{1 + k_A k_{AI}^n [A_{off}]^n [I]^n + k_R k_{RI}^{-n} \frac{[R_{off}]^n}{[I]^n}}$$

Although the paper mentioned the hill coefficient can combine up to multiplicatively, as it suggested, the final hill coefficient should be  $n*n$ ; however, it's hard to derive from the above equation.