LDA training on random subsets of different sizes

```
library(ggplot2)

## Warning: package 'ggplot2' was built under R version 4.0.5

library(dplyr)

## Warning: package 'dplyr' was built under R version 4.0.5

## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':

## filter, lag

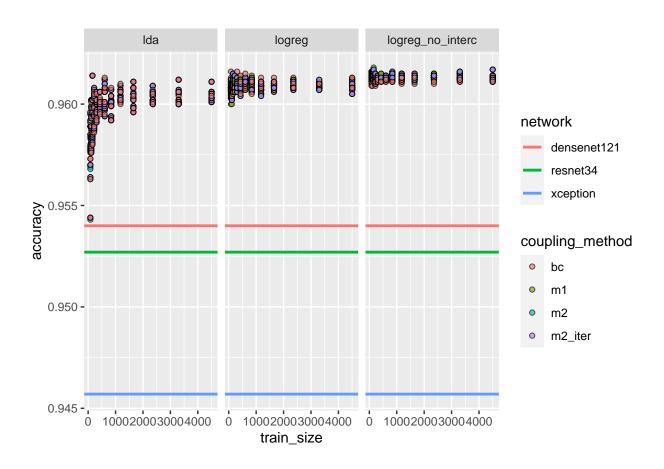
## The following objects are masked from 'package:base':

## intersect, setdiff, setequal, union
```

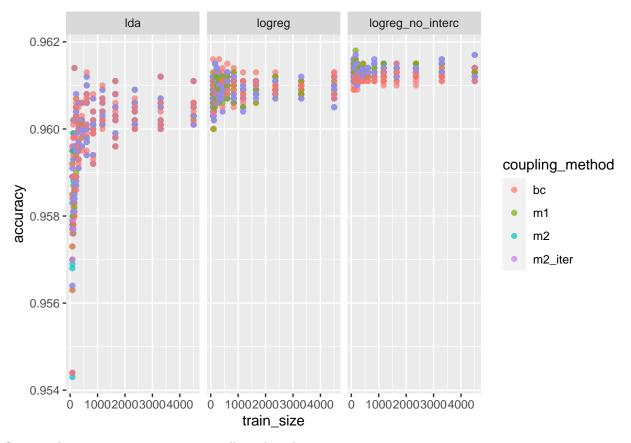
Experiment code is in the file training_subsets_sizes_experiment.py. Experiment on CIFAR10 dataset. This experiment trains WeightedLinearEnsemble on various subsets of different sizes of data on which neural networks were trained. Subsets of the same size are disjoint. Three different coupling methods are used: method one and two from (Wu, Lin, and Weng 2004) and Bayes covariant method (Šuch and Barreda 2016). Goal of this experiment is to determine, for which size of the LDA training set, the ensemble achieves the best performance.

scatter

```
acc_ens_subsets <- read.csv("../data/data_train_val_c10/0/exp_subsets_sizes_train_outputs/accuracies.cs
acc_nets <- read.csv("../data/data_train_val_c10/0/exp_subsets_sizes_train_outputs/net_accuracies.csv",
scatter <- ggplot() + geom_point(data=acc_ens_subsets, mapping=aes(x=train_size, y=accuracy, fill=coupl</pre>
```



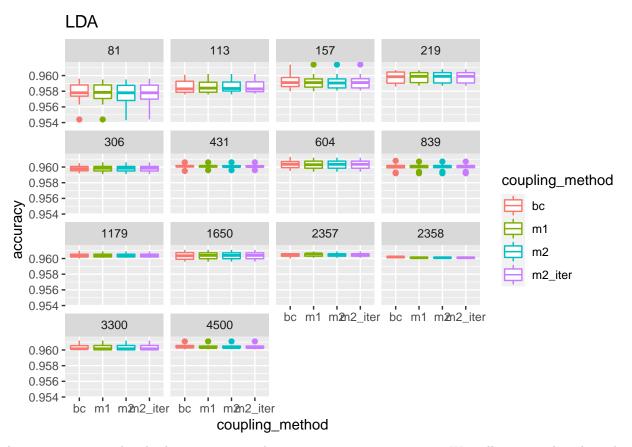
scatter2 <- ggplot() + geom_point(data=acc_ens_subsets, mapping=aes(x=train_size, y=accuracy, color=courseatter2</pre>



Scatter plots are quite messy, so we will use boxplots.

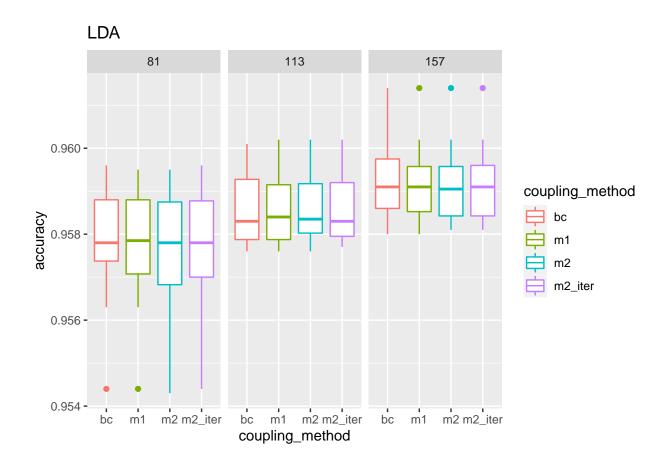
LDA

box_acc <- acc_ens_subsets %>% filter(combining_method=="lda") %>% ggplot() + geom_boxplot(mapping=aes(box_acc

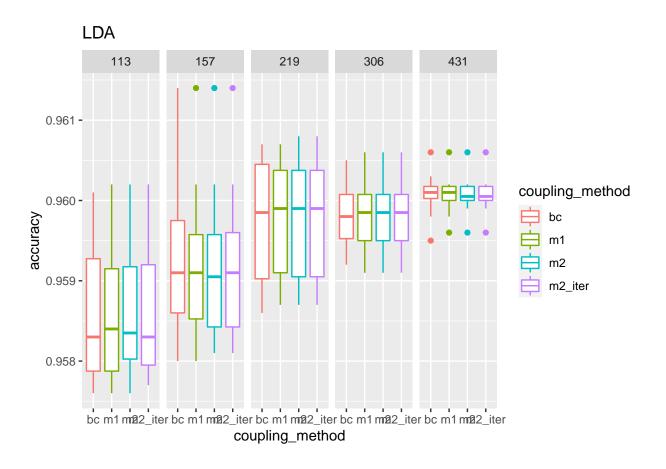


Accuracy seems to be slowly increasing with increasing training set size. We will inspect this closer by plotting for smaller subset sizes range.

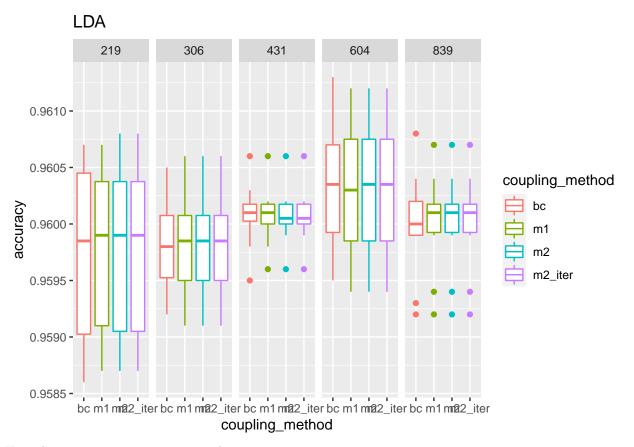
acc_ens_subsets %>% filter(0 < train_size & train_size < 200 & combining_method=="lda") %>% ggplot() + ,



acc_ens_subsets %>% filter(100 < train_size & train_size < 500 & combining_method=="lda") %>% ggplot()

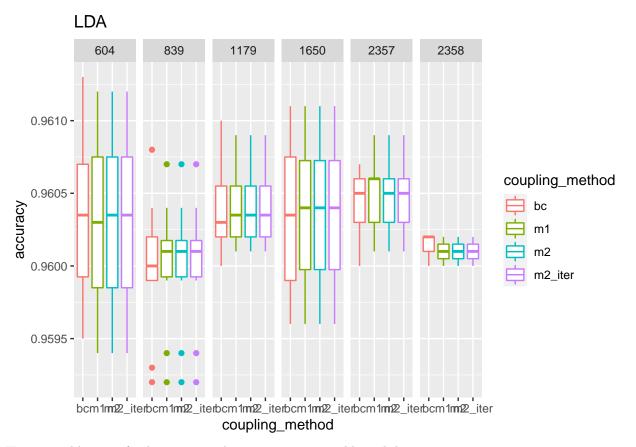


acc_ens_subsets %>% filter(200 < train_size & train_size < 1000 & combining_method=="lda") %>% ggplot()



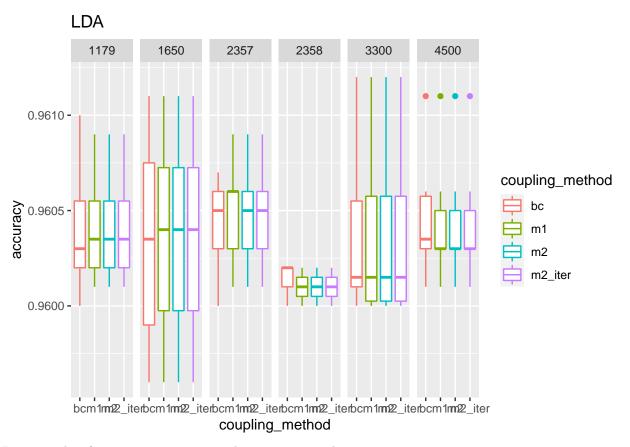
Here the accuracy increase seems to be stopping at train set size 604.

 $acc_ens_subsets \%>\% \ filter(500 < train_size \& train_size < 3000 \& combining_method == "lda") \%>\% \ ggplot()$



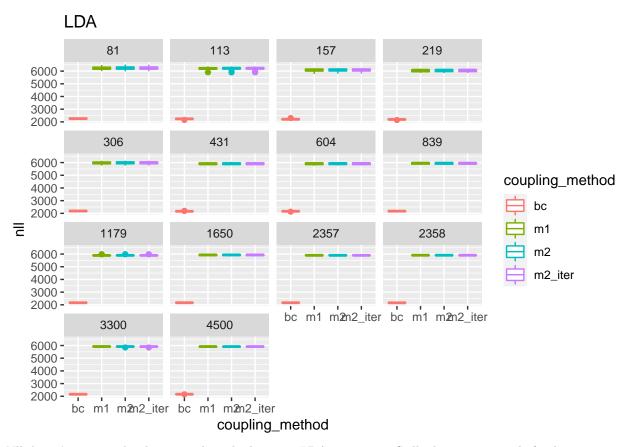
Here is visible some further increase, but it is not very stable and decreases again.

acc_ens_subsets %>% filter(1000 < train_size & train_size < 5000 & combining_method=="lda") %>% ggplot(



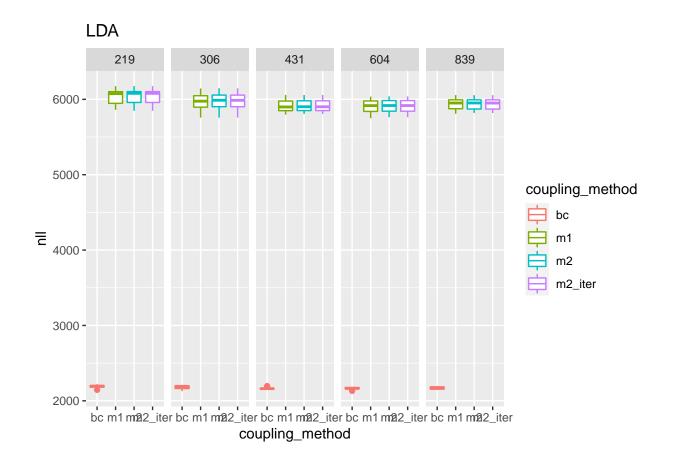
It seems, that from train set size around 1000 accuracy decreases again.

box_nll <- acc_ens_subsets %>% filter(combining_method=="lda") %>% ggplot() + geom_boxplot(mapping=aes(box_nll

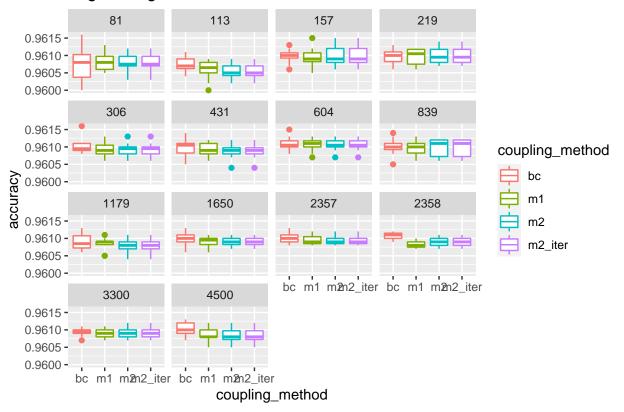


Nll doesn't seem to be doing much with changing LDA train size. Still, this metric needs further attention because of the zero probabilities produced by ensemble.

acc_ens_subsets %>% filter(200 < train_size & train_size < 1000 & combining_method=="lda") %>% ggplot()

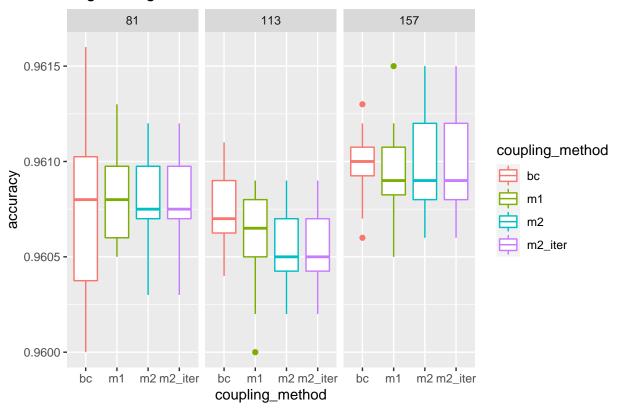


box_acc <- acc_ens_subsets %>% filter(combining_method=="logreg") %>% ggplot() + geom_boxplot(mapping=a
box_acc

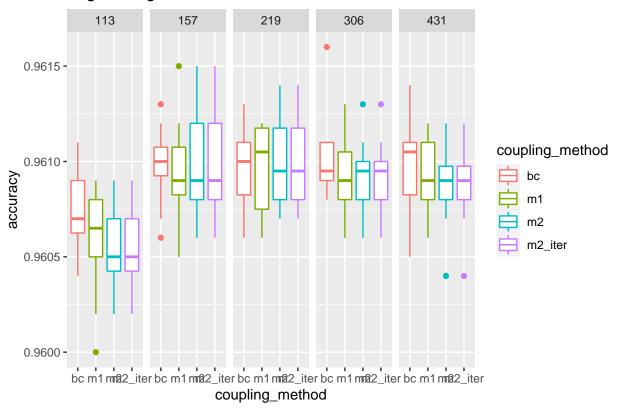


Accuracy seems to be slowly increasing with increasing training set size. We will inspect this closer by plotting for smaller subset sizes range.

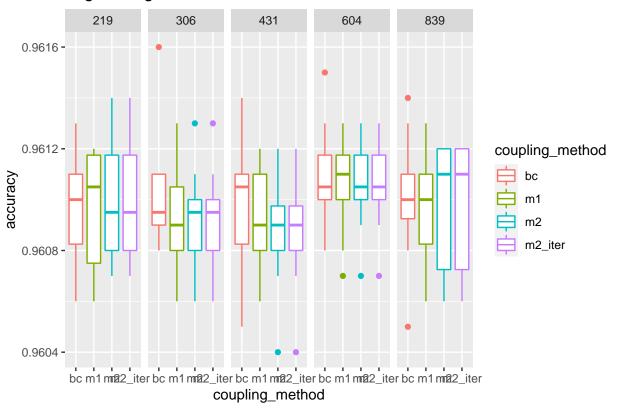
acc_ens_subsets %>% filter(0 < train_size & train_size < 200 & combining_method=="logreg") %>% ggplot()



acc_ens_subsets %>% filter(100 < train_size & train_size < 500 & combining_method=="logreg") %>% ggplot

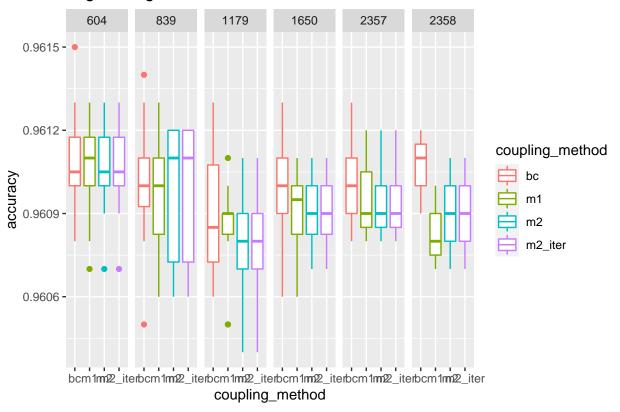


acc_ens_subsets %>% filter(200 < train_size & train_size < 1000 & combining_method=="logreg") %>% ggplo



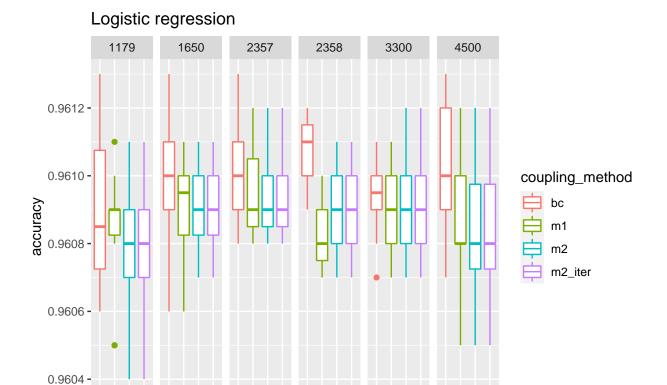
Here the accuracy increase seems to be stopping at train set size 604.

 $\verb|acc_ens_subsets|| \% \% | filter(500 < train_size & train_size < 3000 & combining_method == "logreg") \% \% | ggplowers | % \% | ggplowers$



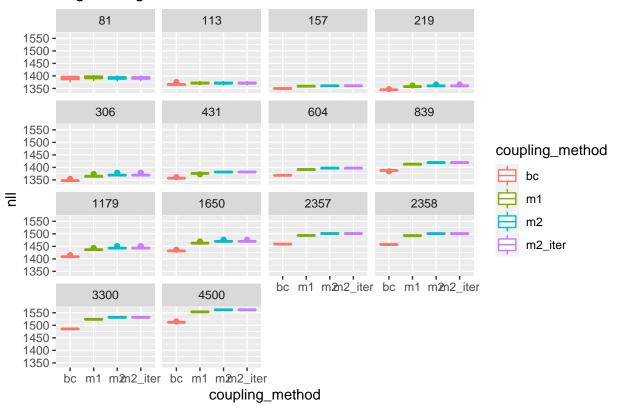
Here is visible some further increase, but it is not very stable and decreases again.

acc_ens_subsets %>% filter(1000 < train_size & train_size < 5000 & combining_method=="logreg") %>% ggpl



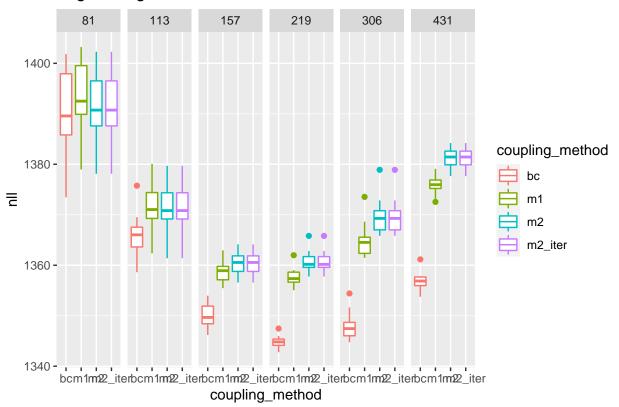
bcm1mm2_iterbcm1mm

box_nll <- acc_ens_subsets %>% filter(combining_method=="logreg") %>% ggplot() + geom_boxplot(mapping=a
box_nll



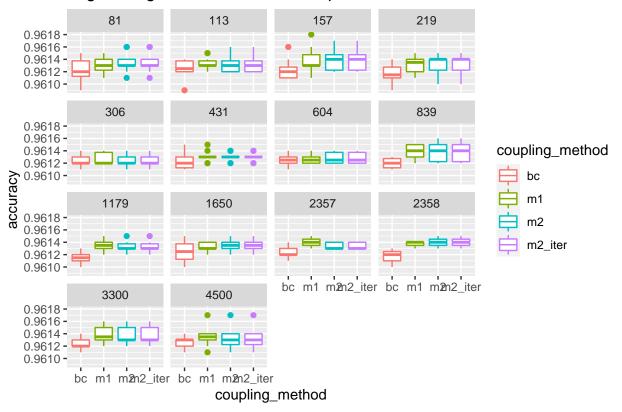
Nll is decreasing with increasing train set size for up to size around 200, then it starts increasing.

acc_ens_subsets %>% filter(0 < train_size & train_size < 500 & combining_method=="logreg") %>% ggplot()



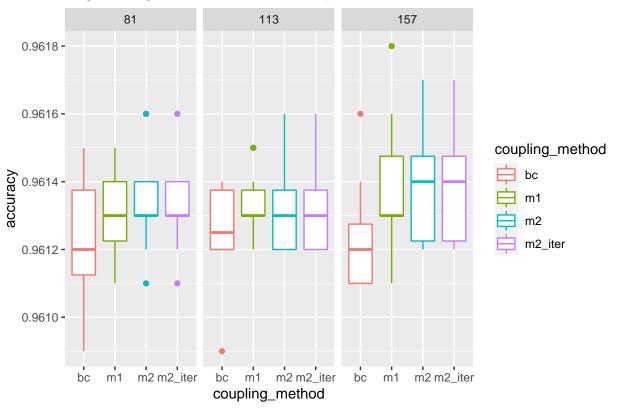
Logistic regression without intercept

box_acc <- acc_ens_subsets %>% filter(combining_method=="logreg_no_interc") %>% ggplot() + geom_boxplot
box_acc

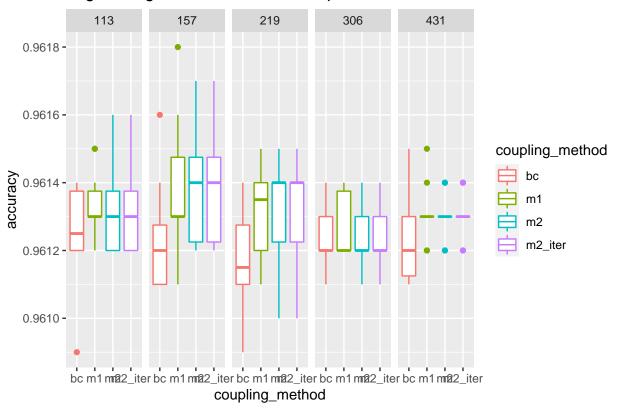


Accuracy seems to be slowly increasing with increasing training set size. Coupling method be achieves inferior results for some train sizes. We will inspect this closer by plotting for smaller subset sizes range.

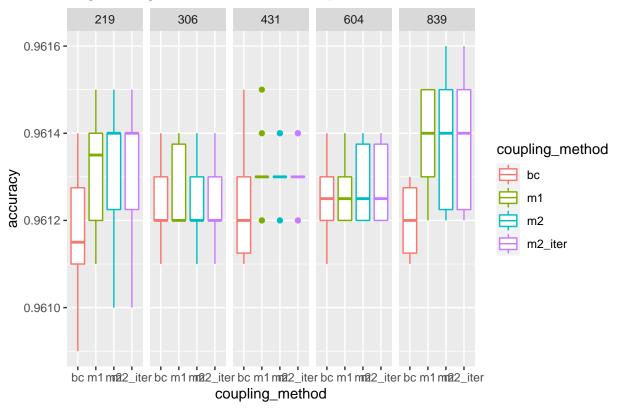
acc_ens_subsets %>% filter(0 < train_size & train_size < 200 & combining_method=="logreg_no_interc") %>



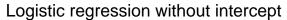
acc_ens_subsets %>% filter(100 < train_size & train_size < 500 & combining_method=="logreg_no_interc")

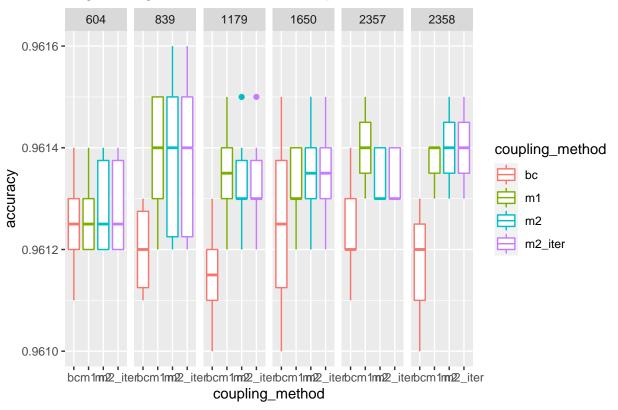


acc_ens_subsets %>% filter(200 < train_size & train_size < 1000 & combining_method=="logreg_no_interc")



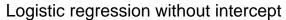
acc_ens_subsets %>% filter(500 < train_size & train_size < 3000 & combining_method=="logreg_no_interc")

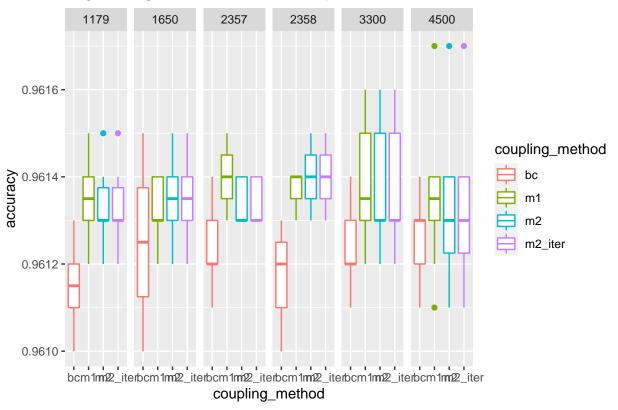




Here the accuracy increase seems to be stopping at train set size 839. However, accuracy of method bc is already decreasing.

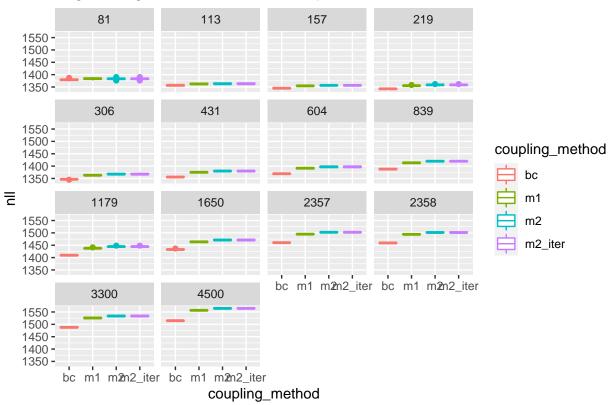
 $\verb|acc_ens_subsets| \%>\% \ \, \texttt{filter(1000 < train_size \& train_size < 5000 \& combining_method=="logreg_no_interc" | 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 1000 < 100$





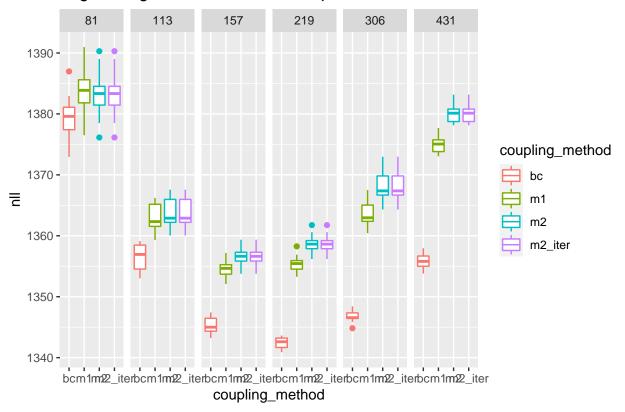
It seems, that from train set size around 1000 accuracy is stagnating.

box_nll <- acc_ens_subsets %>% filter(combining_method=="logreg_no_interc") %>% ggplot() + geom_boxplot
box_nll



Nll is decreasing with increasing train set size for up to size around 200, then it starts increasing.

acc_ens_subsets %>% filter(0 < train_size & train_size < 500 & combining_method=="logreg_no_interc") %>



Šuch, Ondrej, and Santiago Barreda. 2016. "Bayes Covariant Multi-Class Classification." *Pattern Recognition Letters* 84: 99–106.

Wu, Ting-Fan, Chih-Jen Lin, and Ruby C Weng. 2004. "Probability Estimates for Multi-Class Classification by Pairwise Coupling." *Journal of Machine Learning Research* 5 (Aug): 975–1005.