

# Precision phenomenology with heavy-flavour jets at the LHC

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Rene Poncelet

based on 2011.01011, 2205.11879, 2212.00467 and 2308.02285  
and preliminary Les Houches studies



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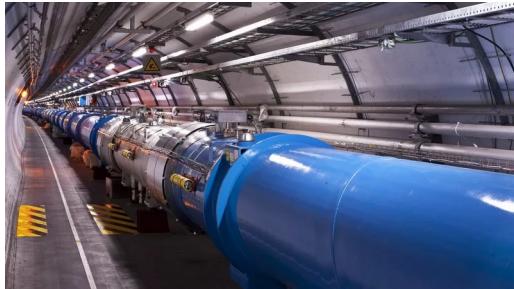
# Outline

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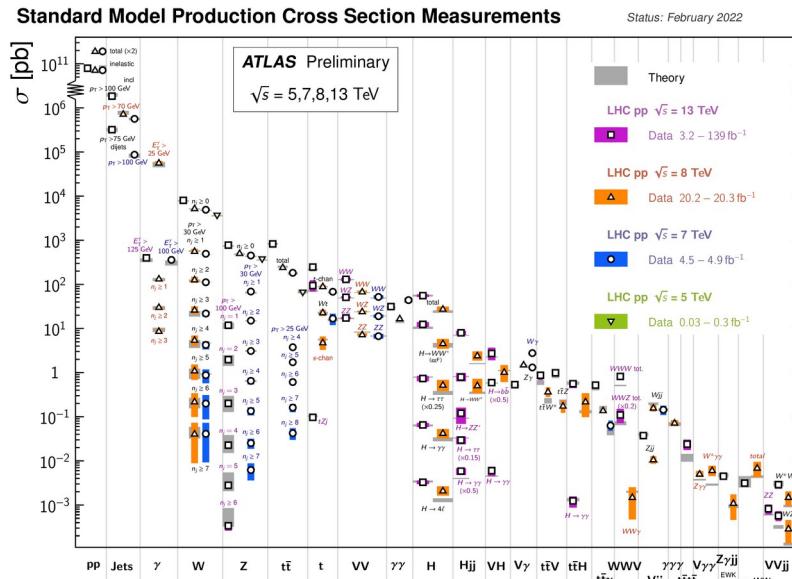
- Phenomenological motivation
  - Vector bosons + flavoured jets
  - Infrared safety/sensitivity
- NNLO QCD Phenomenology with W+c-jets
- Flavoured (anti- $k_T$ ) jet algorithms
  - (Tests of IR-safety)

# What are the fundamental building blocks of matter?

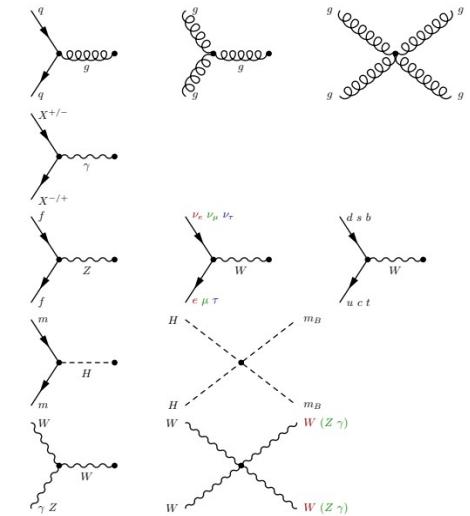
Scattering experiments



Credit: CERN



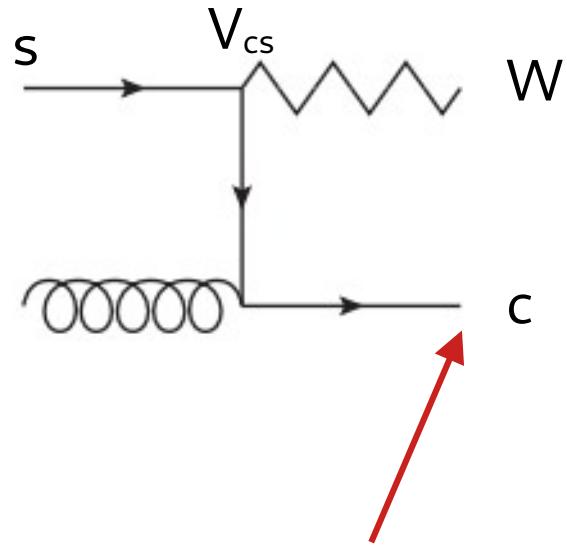
Theory/Model



Credit: Jack Lindon, CERN

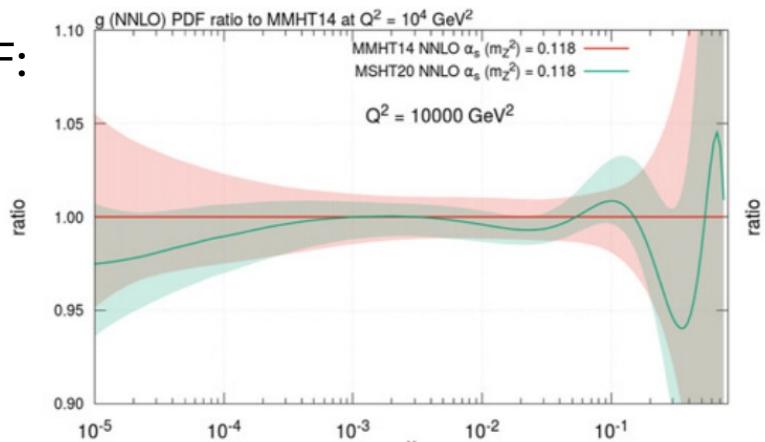
Looking into more exclusive observables ("flavoured jets")  
with more precision ("higher order corrections").

# $W + \text{charm jet}$

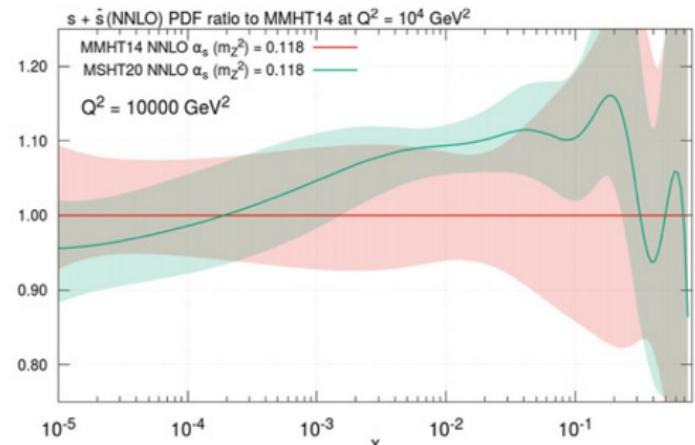


Tagging of charm jet  
to increase sensitivity  
to strange quark PDF

gluon PDF:



$s + \bar{s}$  PDF:



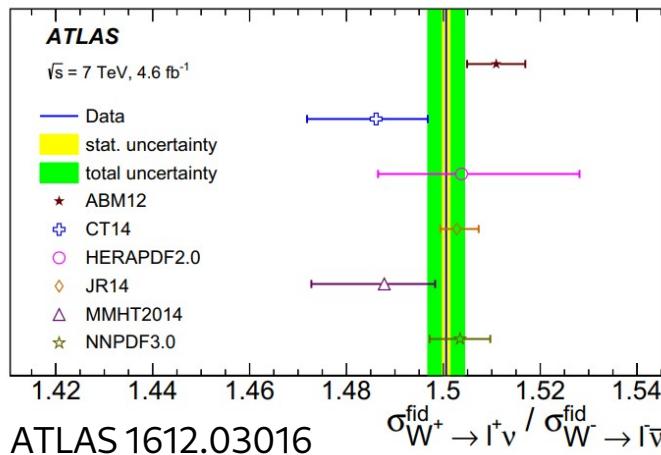
PDF4LHC22 [2203.05506]

# $W + \text{charm jet}$

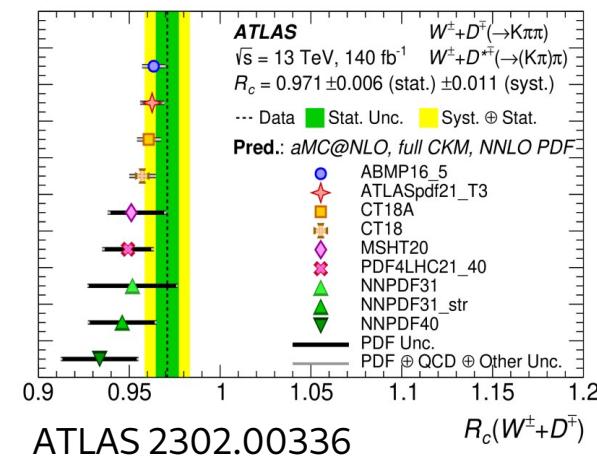
Could solve long-standing puzzle:  
**Strange – anti – strange asymmetry**

- pQCD: Three loop SM prediction  $q \rightarrow q' \neq q \rightarrow \bar{q}'$  small effect  $\langle x(s-\bar{s}) \rangle \sim 10^{-4}$
- Size of non-perturbative effect unknown

7 TeV analysis favours  $s \neq \bar{s}$

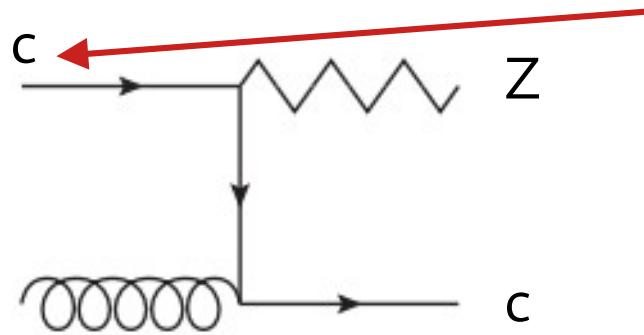


13 TeV analysis favours  $s = \bar{s}$



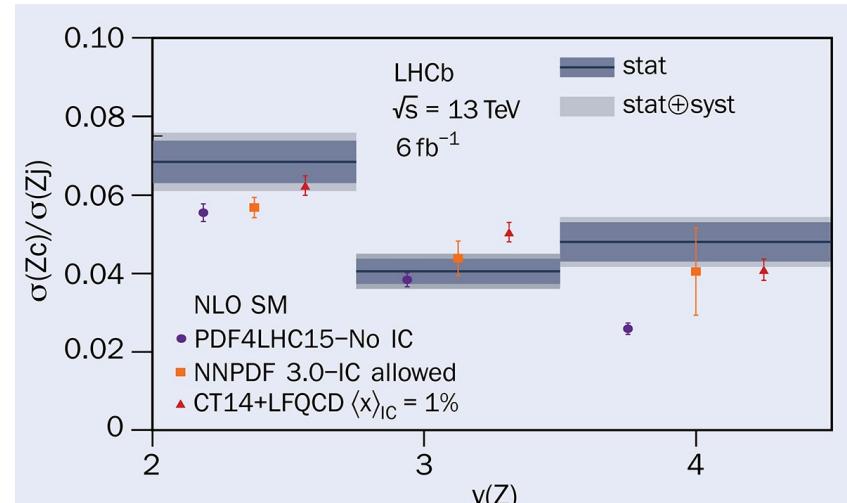
All at NLO QCD  
higher order corrections needed to fit properly the PDF

# Z + charm jet



Similar to W+charm but for charm PDF

Intrinsic charm component?  
Clarification needs  
→ higher order corrections  
→ charm jet definition



CERN/LHCb 2109.08084

# Flavoured jets are everywhere

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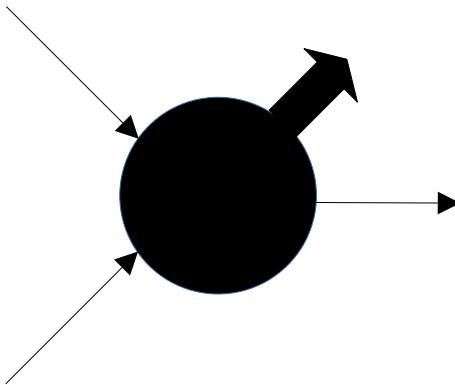
- Flavoured jets as signature
  - Top-quarks
  - Vector+heavy flavour:  $pp \rightarrow W/Z/A + c/b$
  - Higgs  $\rightarrow$  charm, Higgs  $\rightarrow$  bottom
  - New physics searches
- This talk: V + heavy-flavour
  - Benchmark for flavour tagging
  - IR safety/sensitivity
  - (Heavy-quark evolution: fragmentation and hadronisation)



Rely on our capability to  
→ identify flavoured jets  
→ and interpret them

# Heavy flavour production

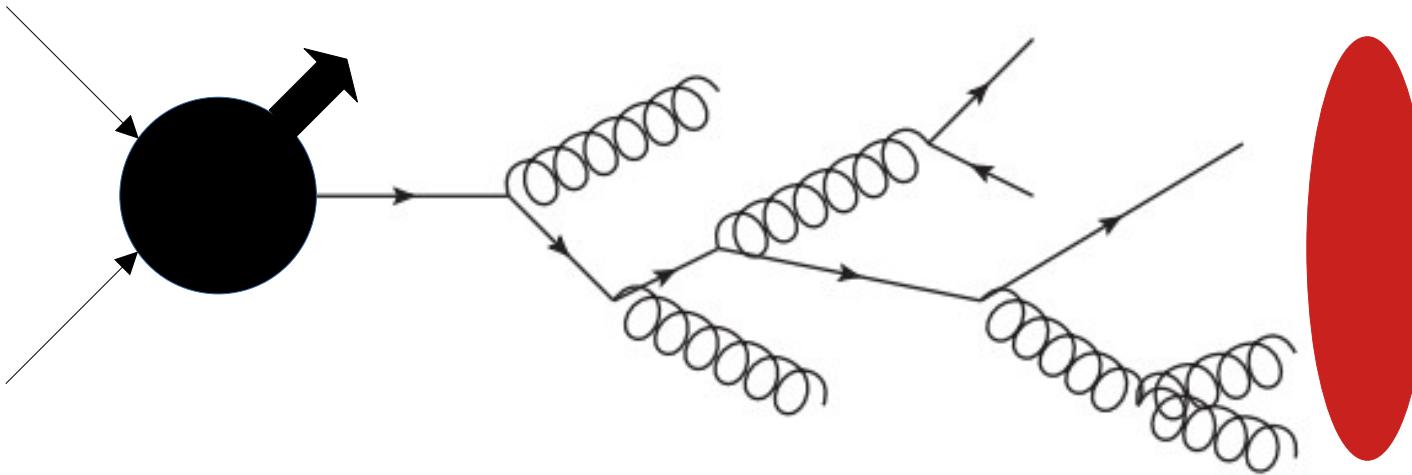
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Setup for this talk:  
Production of a massive quark(s)  
with high transverse momentum:  $p_T \gg m$

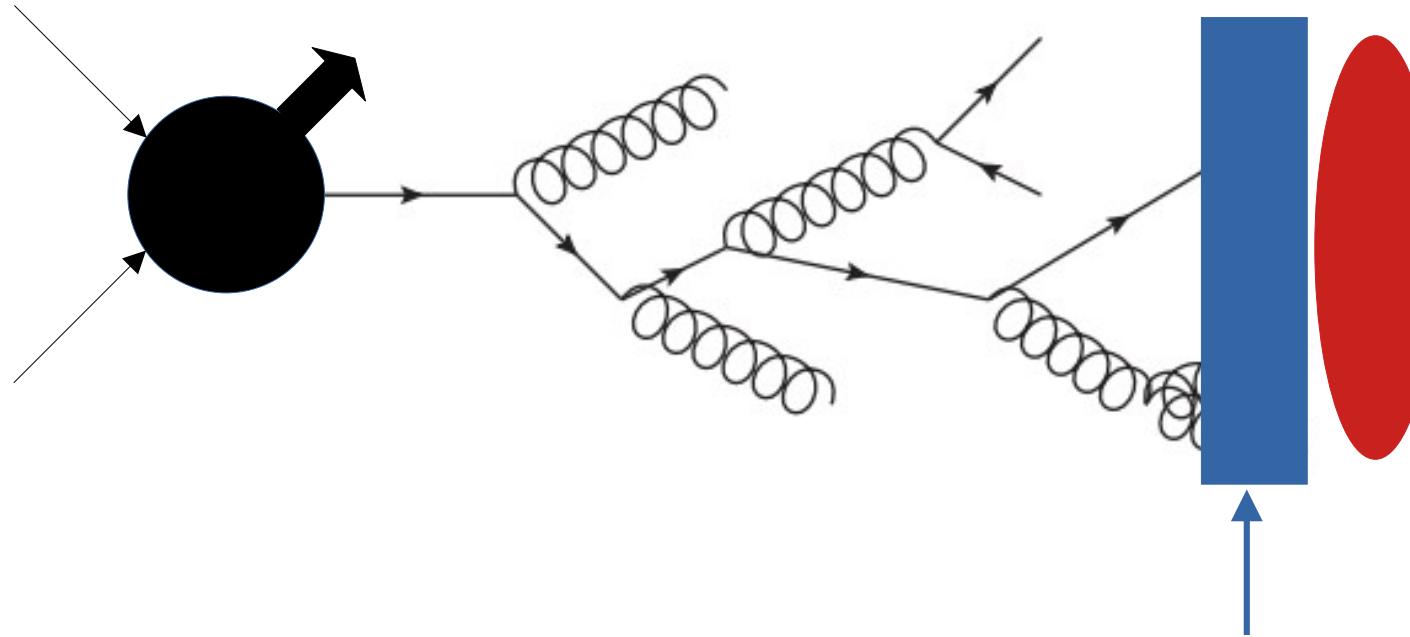
# Partonic jet evolution

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# Partonic jet evolution

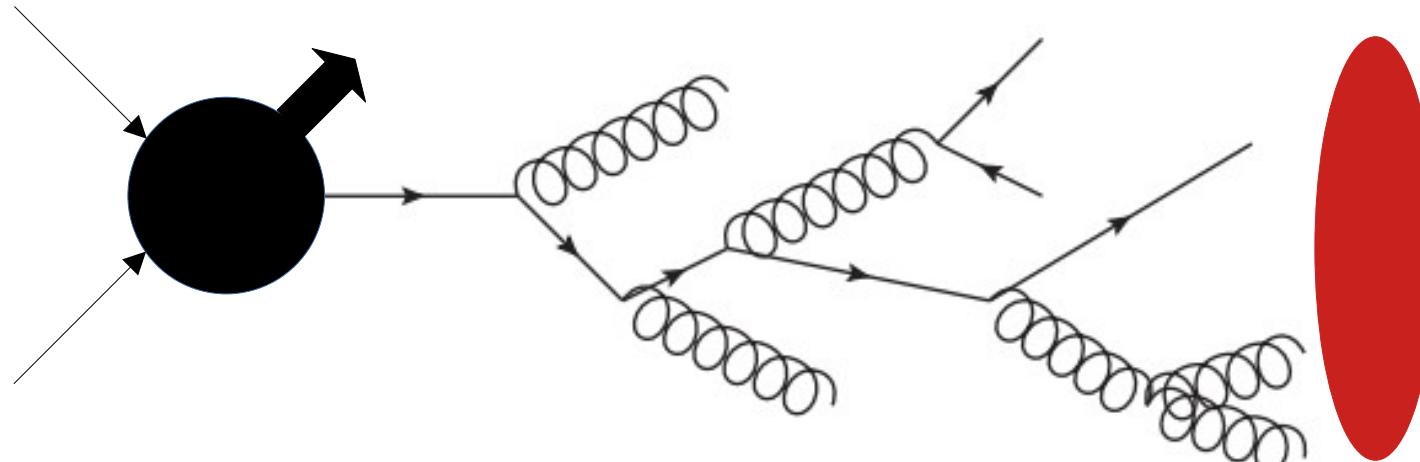
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- Fragmentation/Hadronisation
- Partonic jet flavour: Quark-Hadron Duality
- Heavy B/D – hadron's long life time:  
experiment signature (displaced vertices)  
→ distinguishable from “light” jets

# Partonic jet evolution

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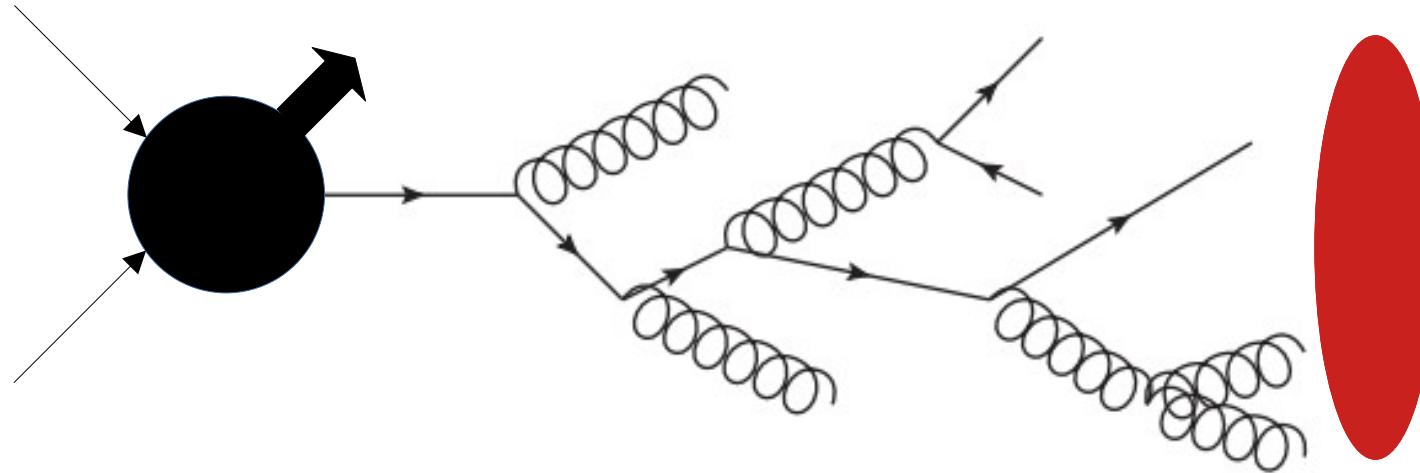
## Massive treatment of quark

- Mass acts as IR regulator  $\rightarrow$  no IR divergences from collinear splitting
- Price to pay:  $\log(pT/m)$ , how to treat PDFs (high  $Q^2$  process due to V-boson)?
  - $\rightarrow$  Resummation for reliable predictions
  - $\rightarrow$  Parton-showers (at low accuracy)
- **But** Higher order calculations more difficult
  - $\rightarrow$  some applications (like PDF fits) need **fixed order** pQCD at higher orders

} NLO+PS

# Partonic jet evolution

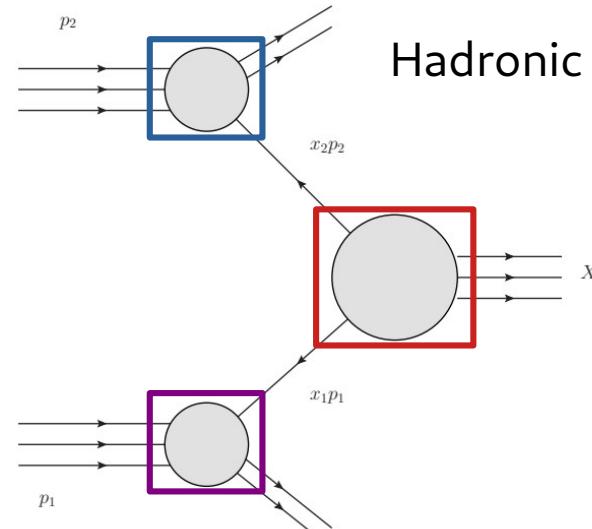
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High transverse momentum  $\rightarrow$  massless quarks

- Collinear (mass) divergences absorbed by renormalisation
- Consistent treatment with PDFs (high  $Q^2 \rightarrow$  c/b quarks in DGLAP)
- Bonus: higher order calculations easier  $\rightarrow$  NNLO QCD de-facto standard
- **BUT:** IR-safety more demanding due to collinear and soft flavoured particles

# Hadronic cross section in collinear factorization – NNLO QCD



Hadronic X-section:

$$\sigma_{h_1 h_2 \rightarrow X} = \sum_{ij} \int_0^1 \int_0^1 dx_1 dx_2 \phi_{i,h_1}(x_1, \mu_F^2) \phi_{j/h_2}(x_2, \mu_F^2) \hat{\sigma}_{ij \rightarrow X}(\alpha_s(\mu_R^2), \mu_R^2, \mu_F^2)$$

Parton distribution functions

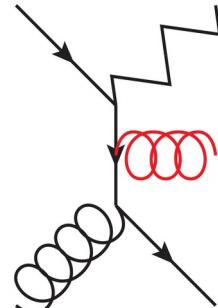
Perturbative expansion of partonic cross section:

$$\hat{\sigma}_{ab \rightarrow X} = \hat{\sigma}_{ab \rightarrow X}^{(0)} + \hat{\sigma}_{ab \rightarrow X}^{(1)} + \hat{\sigma}_{ab \rightarrow X}^{(2)} + \mathcal{O}(\alpha_s^3)$$

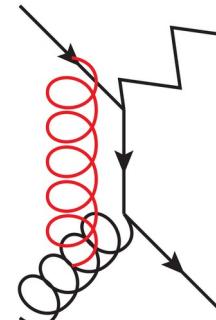
The NLO bit:

$$\hat{\sigma}_{ab}^{(1)} = \hat{\sigma}_{ab}^R + \hat{\sigma}_{ab}^V + \hat{\sigma}_{ab}^C$$

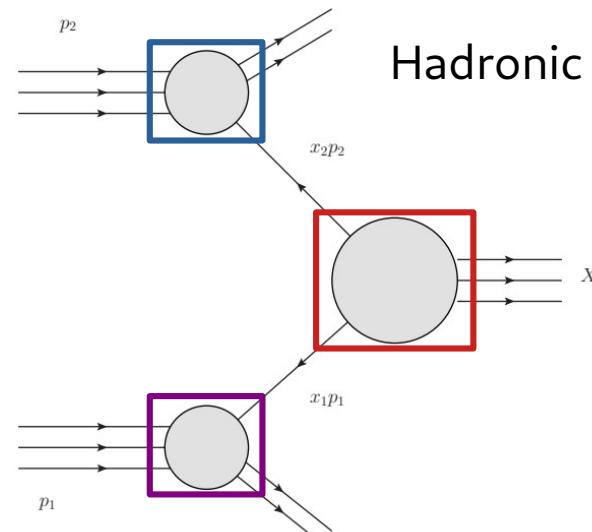
Real radiation



Virtual correction



# Hadronic cross section in collinear factorization – NNLO QCD



$$\text{Hadronic X-section: } \sigma_{h_1 h_2 \rightarrow X} = \sum_{ij} \int_0^1 \int_0^1 dx_1 dx_2 \phi_{i,h_1}(x_1, \mu_F^2) \phi_{j/h_2}(x_2, \mu_F^2) \hat{\sigma}_{ij \rightarrow X}(\alpha_s(\mu_R^2), \mu_R^2, \mu_F^2)$$

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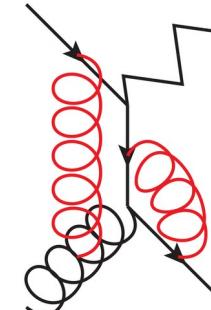
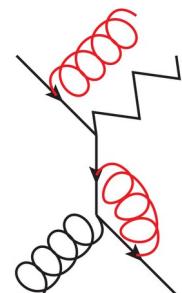
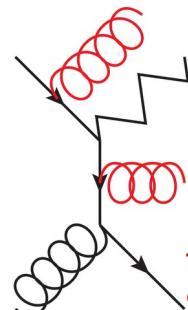
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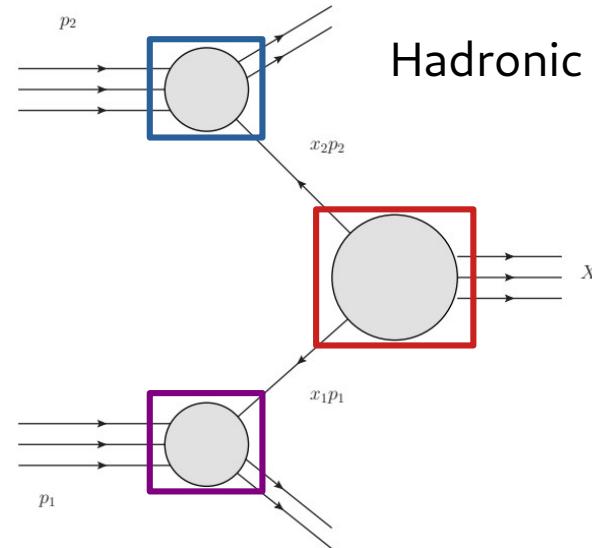
The NNLO bit:  $\hat{\sigma}_{ab}^{(2)} = \hat{\sigma}_{ab}^{\text{RR}} + \hat{\sigma}_{ab}^{\text{RV}} + \hat{\sigma}_{ab}^{\text{VV}} + \hat{\sigma}_{ab}^{\text{C2}} + \hat{\sigma}_{ab}^{\text{C1}}$

Real/Virtual correction

Double virtual corrections



# Hadronic cross section in collinear factorization – NNLO QCD



$$\text{Hadronic X-section: } \sigma_{h_1 h_2 \rightarrow X} = \sum_{ij} \int_0^1 \int_0^1 dx_1 dx_2 \phi_{i,h_1}(x_1, \mu_F^2) \phi_{j/h_2}(x_2, \mu_F^2) \hat{\sigma}_{ij \rightarrow X}(\alpha_s(\mu_R^2), \mu_R^2, \mu_F^2)$$

Parton distribution functions

Perturbative expansion of partonic cross section:

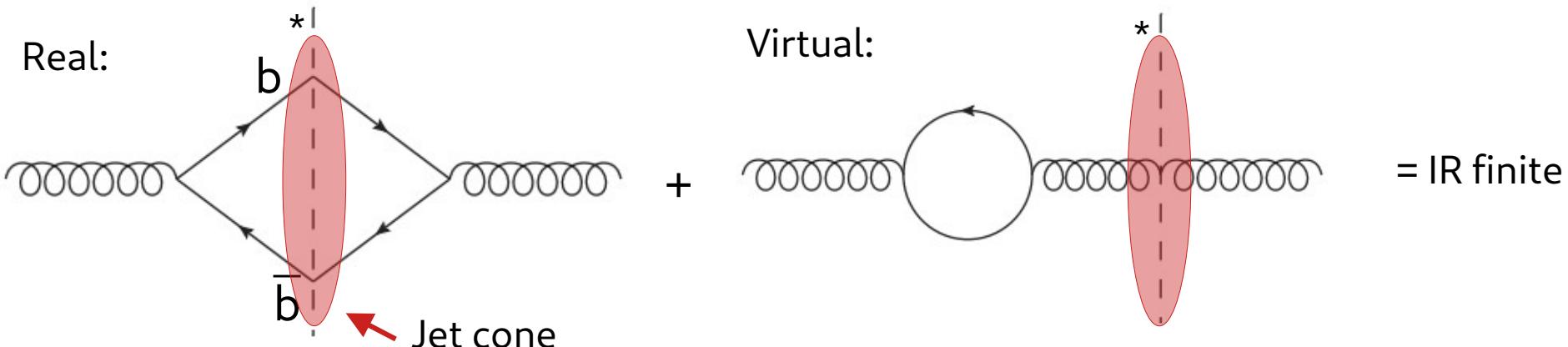
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Calculations performed with sector-improved residue subtraction scheme  
1408.2500 & 1907.12911

# IR safety issues starting from NLO QCD

Massless QCD: Cancellation of IR divergences between real and virtual corrections



Flavoured?  
(Keeping in mind quark-hadron duality)

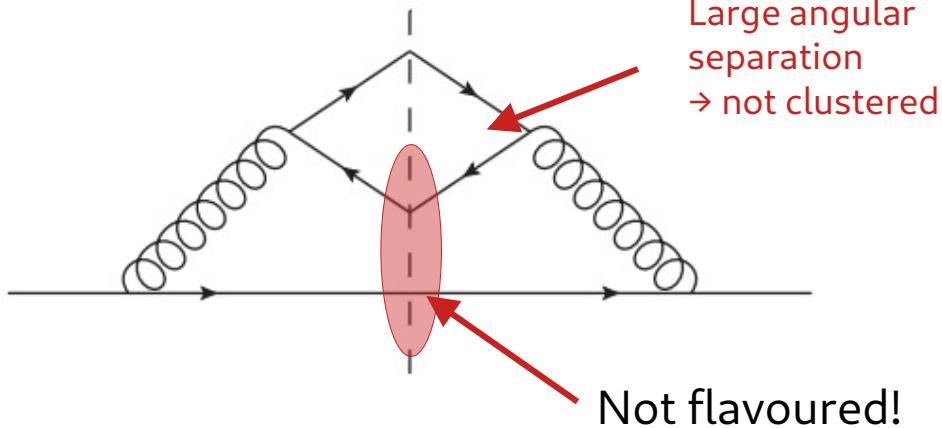


$b \bar{b}$  has to count as a gluon/light jet!

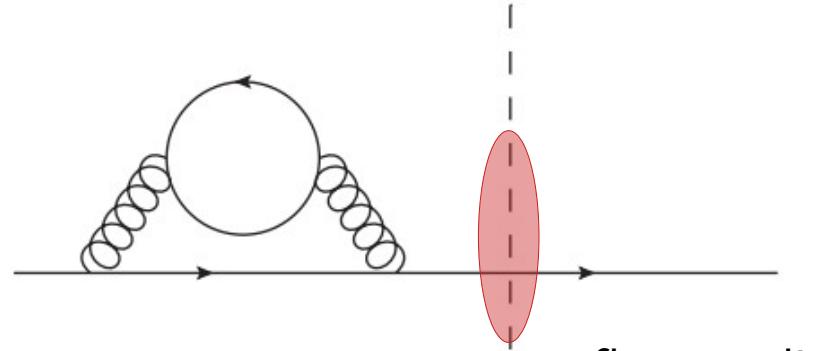
\*: cut symbolises the “measured” final state

# IR safety issues starting from NNLO QCD

Double soft limit of quark pairs



Not flavoured!



flavoured!

- These double soft splitting need to be captured
- Requires to interleave kinematics and flavour information!

# Solution: Modified jet algorithms

- Implies correlated treatment of kinematics and flavour information

Standard kT algorithm:

Pair distance:

$$d_{ij} = \min(k_{T,i}^2, k_{T,j}^2) R_{ij}^2$$

$$R_{ij}^2 = (\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2)/R^2$$

"Beam" distance for determination condition:

$$d_i = k_{T,i}^2$$

Flavour kT algorithm:

Pair distance:

$$d_{ij} = R_{ij}^2 \begin{cases} \max(k_{T,i}, k_{T,j})^\alpha \min(k_{T,i}, k_{T,j})^{2-\alpha} & \text{softer of } i,j \text{ is flavoured} \\ \min(k_{T,i}, k_{T,j})^\alpha & \text{else} \end{cases}$$

Beam distance:

$$d_{i,B} = \begin{cases} \max(k_{T,i}, k_{T,B}(y_i))^\alpha \min(k_{T,i}, k_{T,B}(y_i))^{2-\alpha} & i \text{ is flavoured} \\ \min(k_{T,i}, k_{T,B}(y_i))^\alpha & \text{else} \end{cases}$$

$$d_B(\eta) = \sum_i k_{T,i} (\theta(\eta_i - \eta) + \theta(\eta - \eta_i)) e^{\eta_i - \eta}$$

$$d_{\bar{B}}(\eta) = \sum_i k_{T,i} (\theta(\eta - \eta_i) + \theta(\eta_i - \eta)) e^{\eta - \eta_i}$$

Infrared safe definition of jet flavor,  
Banfi, Salam, Zanderighi hep-ph/0601139

# Approaches to heavy flavour

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## Massive

- FO more complicated
- Resummation of logs → PS
- Flavour-scheme/PDFs?

## Massless

- Easier
- IR safety of jets?
- Mass/Threshold effects at intermediate pT?

## FONLL

- Matching between Massive/massless
- Useful for PDF fits?

## Fragmentation

- Perturbative fragmentation → Resummation of mass effects
- Hadronic observables

# Approaches to heavy flavour

---

## Massive

- FO more complicated
- Resummation of logs → PS
- Flavour-scheme/PDFs?

## Massless

- Easier
- IR safety of jets?
- Mass/Threshold effects at intermediate pT?

How does this compare to experiment?

## FONLL

- Matching between Massive/massless
- Useful for PDF fits?

## Fragmentation

- Perturbative fragmentation → Resummation of mass effects
- Hadronic observables

# Experimental b/c-tagging

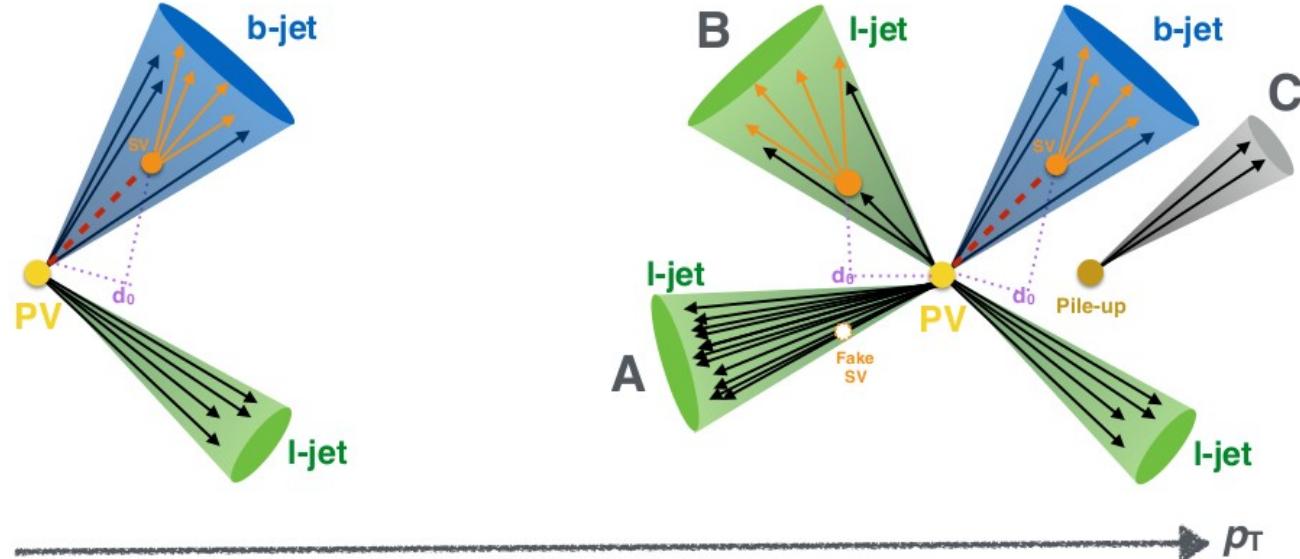
Credit: Arnaud Duperrin (DIS23 talk)

## Secondary vertex (SV) tagging

- Long-life time  
→ several mm flight
- Looking for the decay products of B-hadron decays forming SV

## Challenges

- Fake SV from fragmentation
- Material interactions
- Pile-up



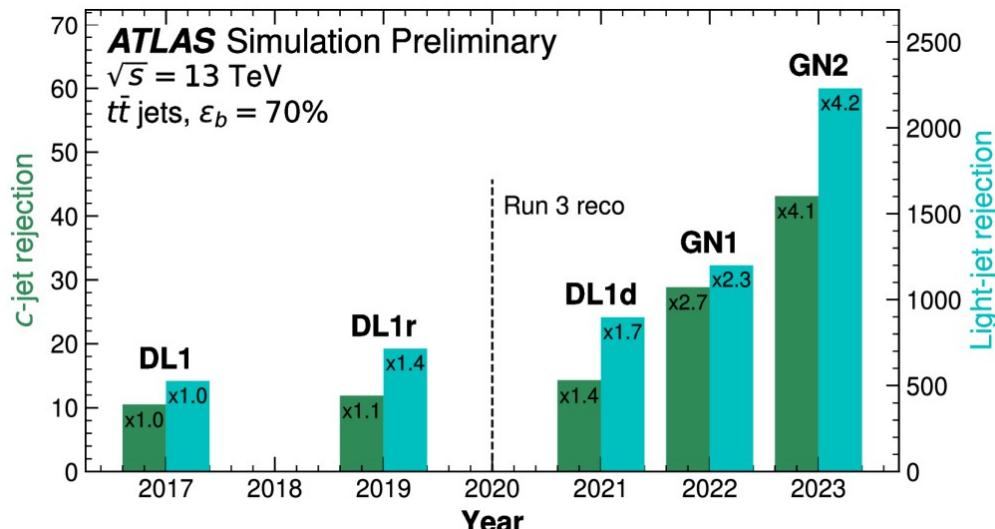
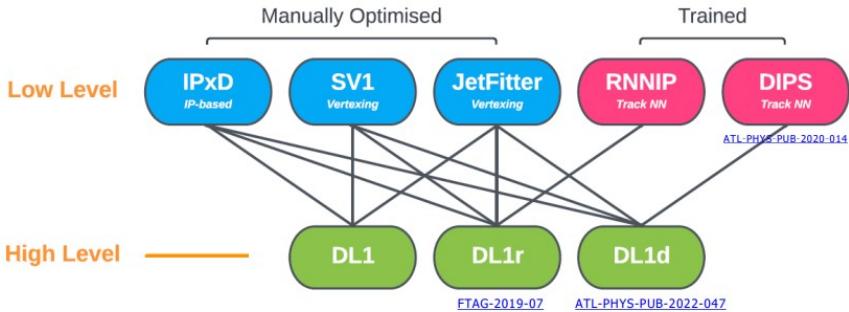
# Experimental b/c-tagging with NN

Credit: Arnaud Duperrin (DIS23 talk)

## Using NN to perform b-tagging

- Many Run II/III analysis use already NN based taggers
- For example ATLAS: DL1
  - uses precomputed low-level infos
- Next generation will directly use hit, track and jet information
  - further performance boost

The truth level information comes from MC simulations



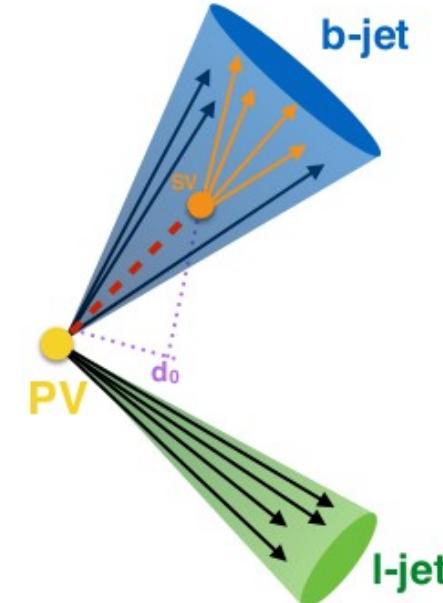
# Ghost tagging

A jet is defined as flavoured if:

- 1) it contains at least one B/D hadron  
FO: IR-unsafe because of  $g \rightarrow b\bar{b}$  splitting
- 2) within  $dR < R$  of jet axis  
FO: IR-unsafe because soft wide angle emission
- 3) with  $pT > pT_{cut}$   
FO: collinear unsafe  $b \rightarrow b$  g splitting  
(okay in fragmentation approach)



“Truth” labelling used in Monte Carlo samples, used to train the NN



*Technically okay for PS+hadronisation models*  
**BUT**  
**Unsatisfactory from theory point of view**  
(trading IR safety with sensitivity)

# Issues for precision phenomenology

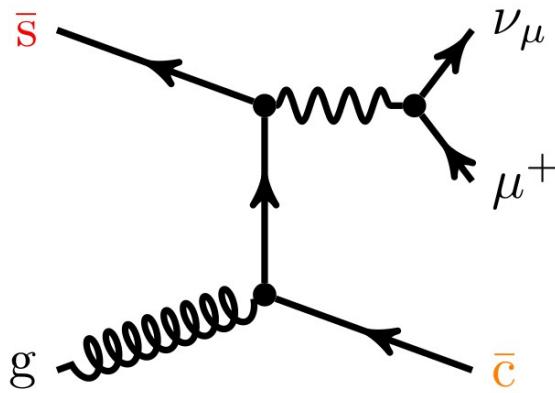
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- The flavoured jet algorithms require detailed flavour information  
→ flavour algorithms difficult to implement experimentally  
Limited by detector-resolution & efficiencies!
- For now: comparisons to higher order QCD partonic computations require corrections for the differences in tagging procedures! → Unfolding!
  - 1)  $g \rightarrow b\bar{b}$  splitting if both  $b$ 's hadronise to B-hadrons  
(this is different to  $b\bar{b} = g$  @ fixed order)
  - 2) Hadronisation/non-perturbative models
- Unfolding corrections can be sizeable  $O(5\text{-}10\%)$

# NNLO QCD W+c-jet

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# W+charm production



**A detailed investigation of W+c-jet at the LHC,**  
Czakon, Mitov, Pellen, Poncelet 2212.00467

Simple phase space:

$$p_{T,\ell} > 30 \text{ GeV}, \quad |\eta_\ell| < 2.5$$
$$p_{T,j_c} > 20 \text{ GeV}, \quad |\eta_{j_c}| < 2.5$$

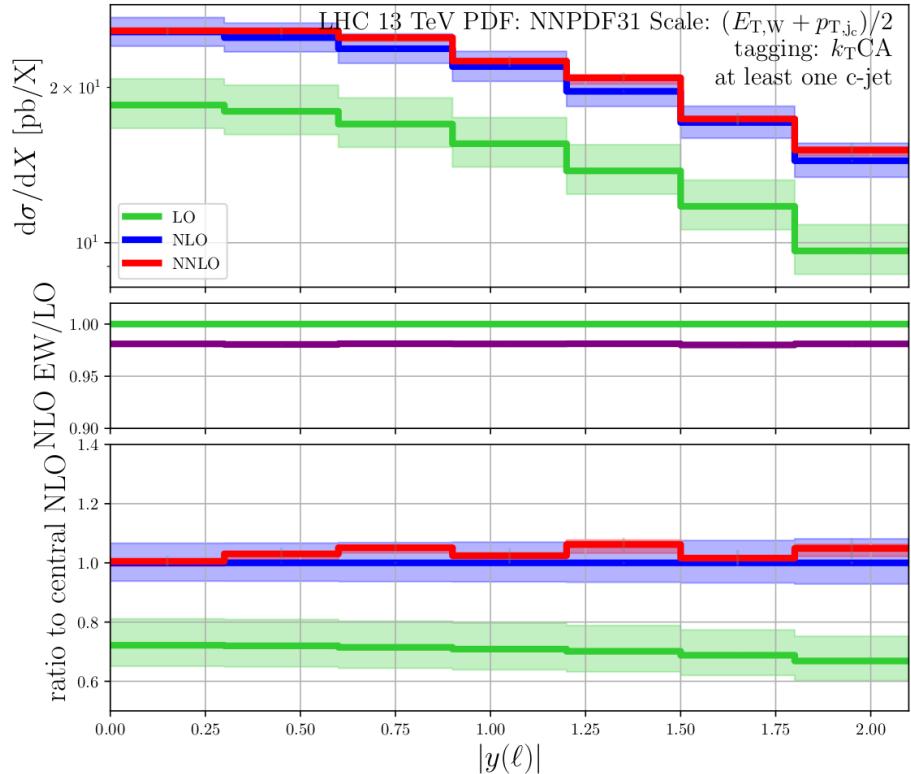
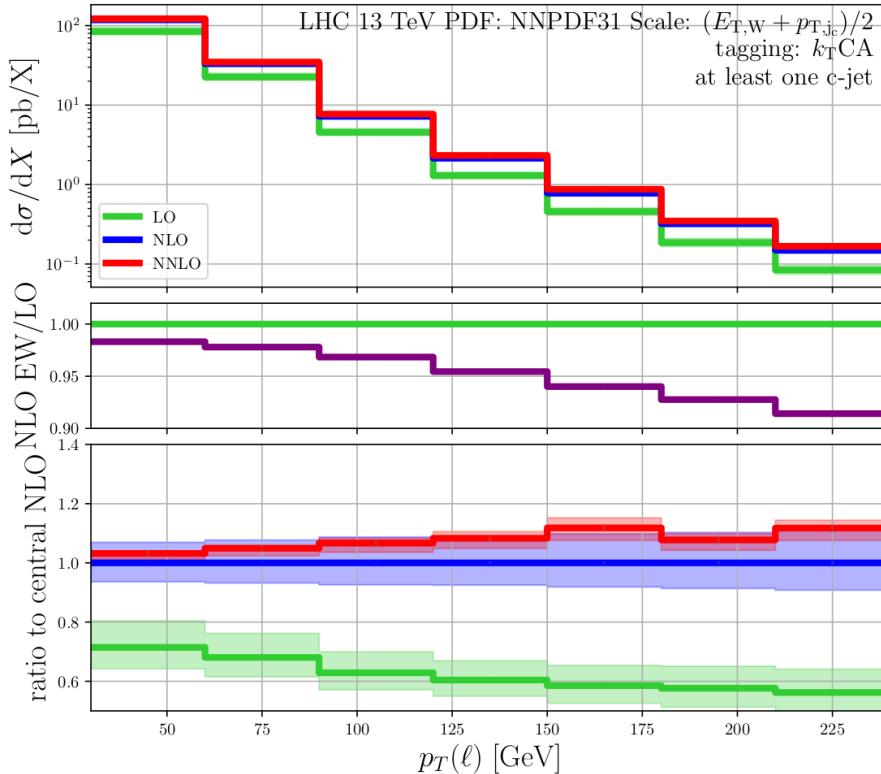
Various effects studied:

- NNLO QCD corrections
- Electroweak corrections
- Off-diagonal CKM matrix
- PDF sensitivity
- Tagging requirements
- Flavoured jet-algorithms

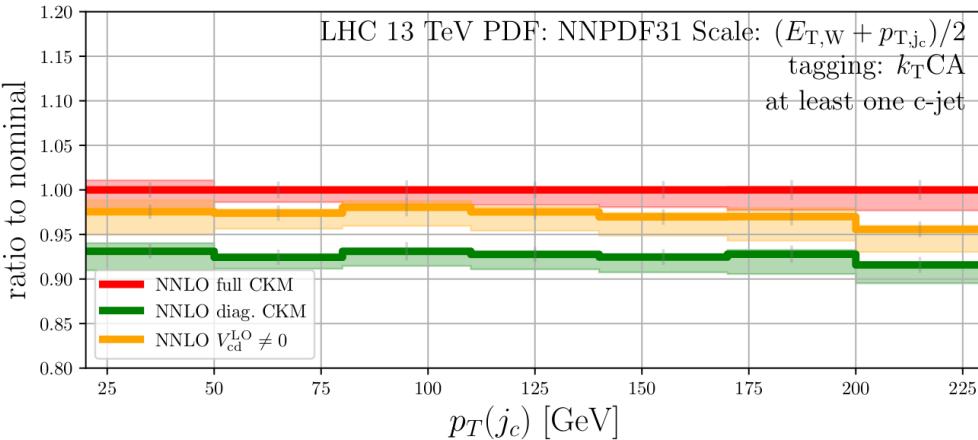
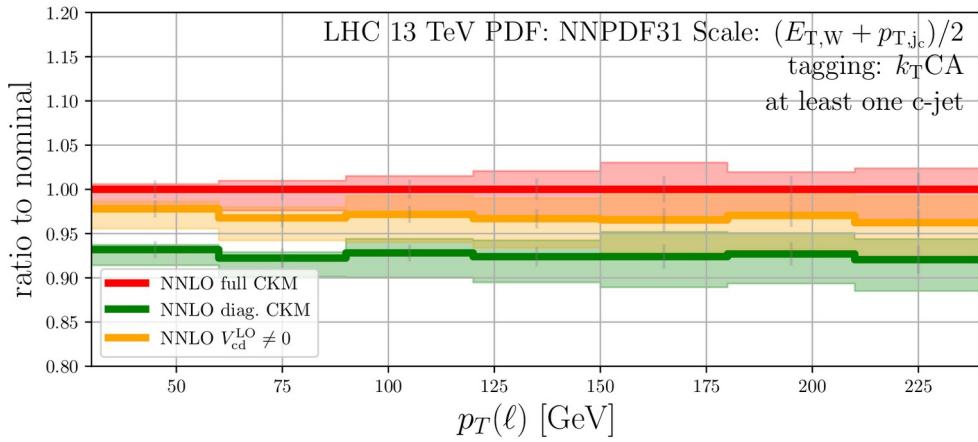
All ~5% effects

# Perturbative corrections

## Flavour-kT, inclusive c-jet requirements

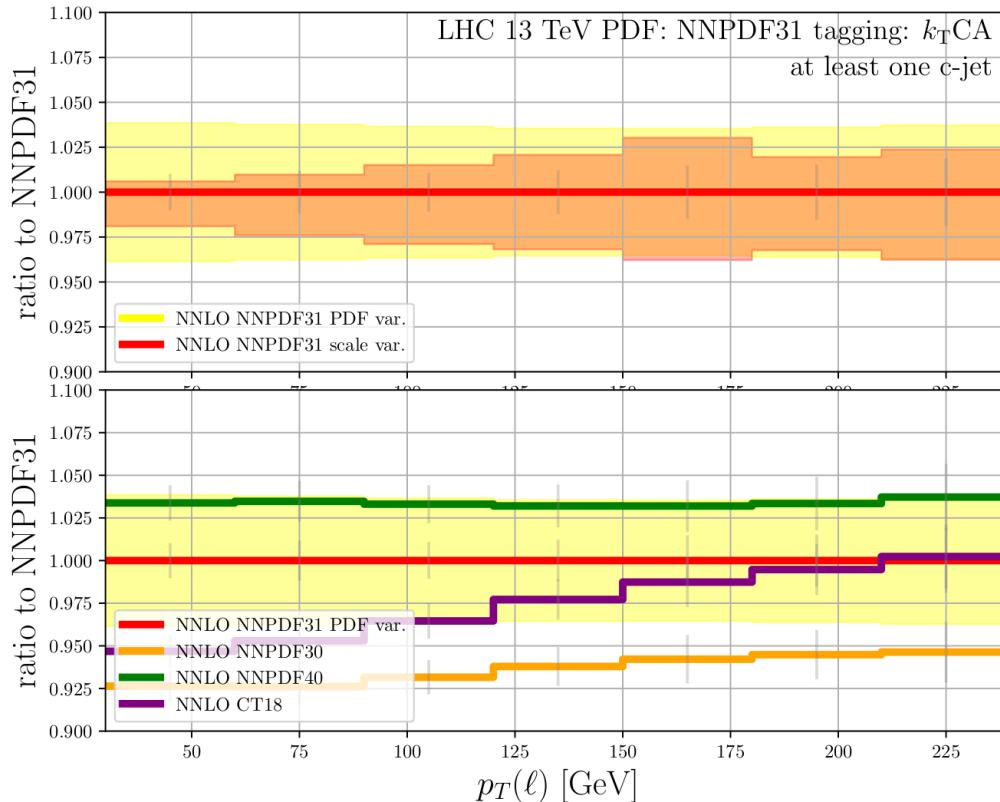


# Off-diagonal CKM



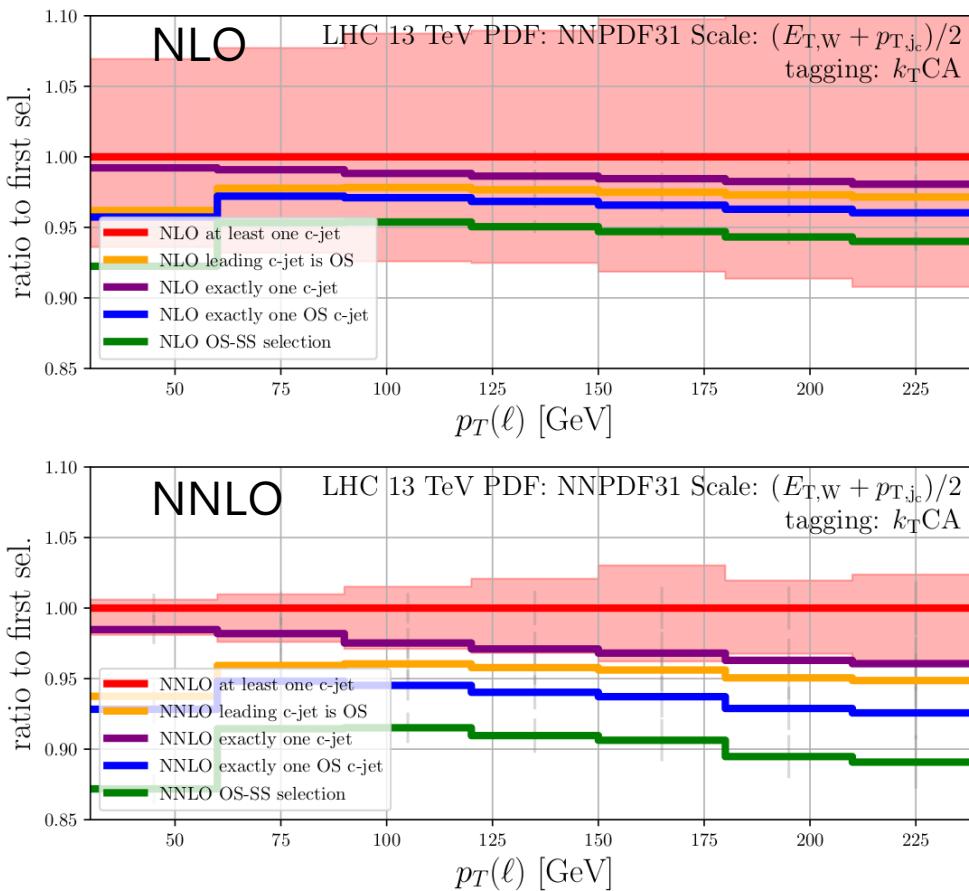
- Full CKM effects through NNLO QCD
- Sizeable with respect NNLO corrections!
- LO  $V_{cd}$  captures most of the full CKM

# PDF dependence



- PDF uncertainty: ~5%
- PDF model variations: ~5-8%  
→ different s-quark PDF treatment:
  - NNPDF asymmetric
  - CT18 symmetric
- Uncertainty > NNLO QCD uncertainty

# Different tagging requirements



## Different tagging requirements

- The leading c-jet (based on its transverse momentum) is of OS type, no requirement on c-jet multiplicity,
- One and only one c-jet is required, no requirement on c-jet charge,
- One and only one c-jet of OS type,
- One and only one c-jet of SS type,
- OS-SS (“OS minus SS”) cross section.

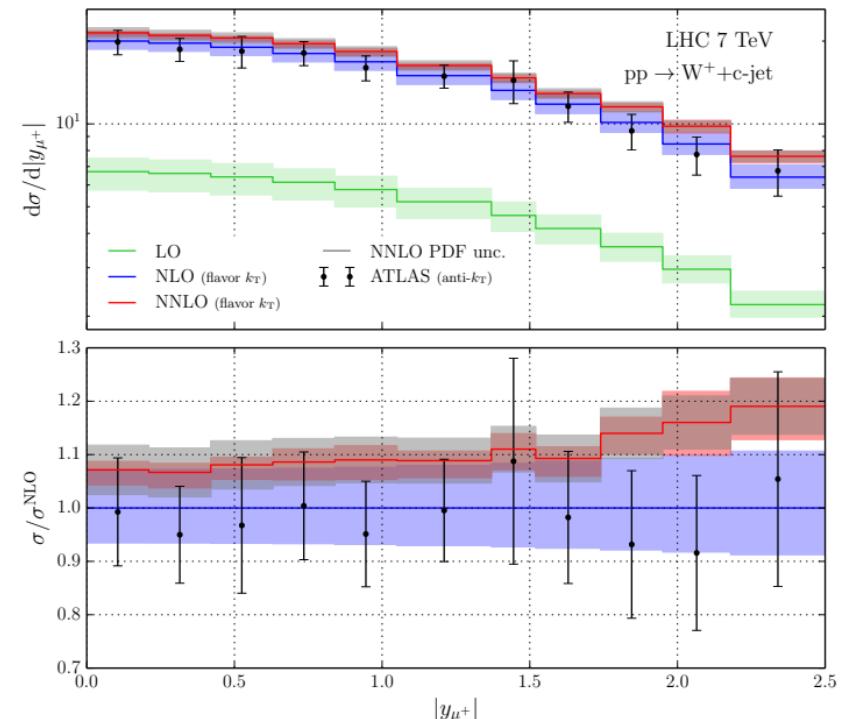
# $W+c$ -jet with flavour $k_T$ at NNLO QCD

NNLO QCD predictions for  $W+c$ -jet production at the LHC,  
Czakon, Mitov, Pellen, Poncelet 2011.01011

NNLO QCD 7 TeV results:

- Full NNLO corrections for  $V_{cb}$  contribution
- Off-diagonal CKM only LO QCD
- Comparison flv.  $k_T$  results vs. ATLAS

Measurement of the production of a  $W$  boson in association with a charm quark in  $pp$  collisions at  $\sqrt{s} = 7$  TeV with the ATLAS detector, 1402.6263



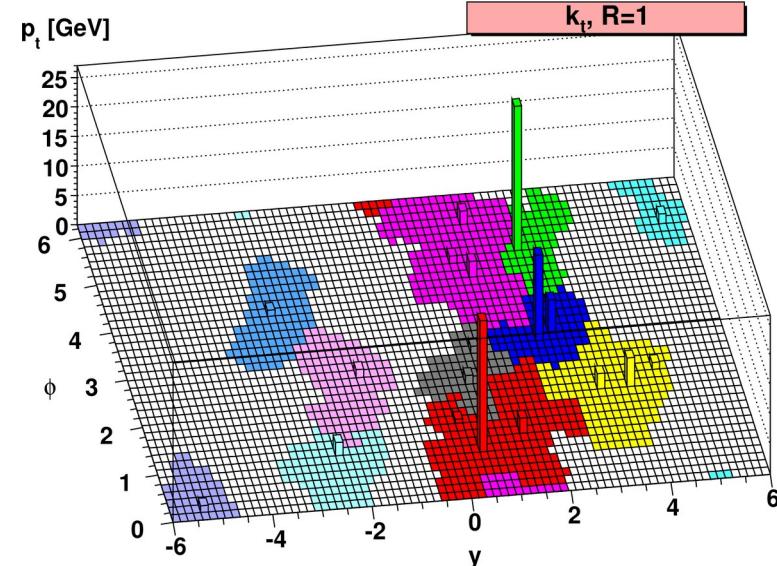
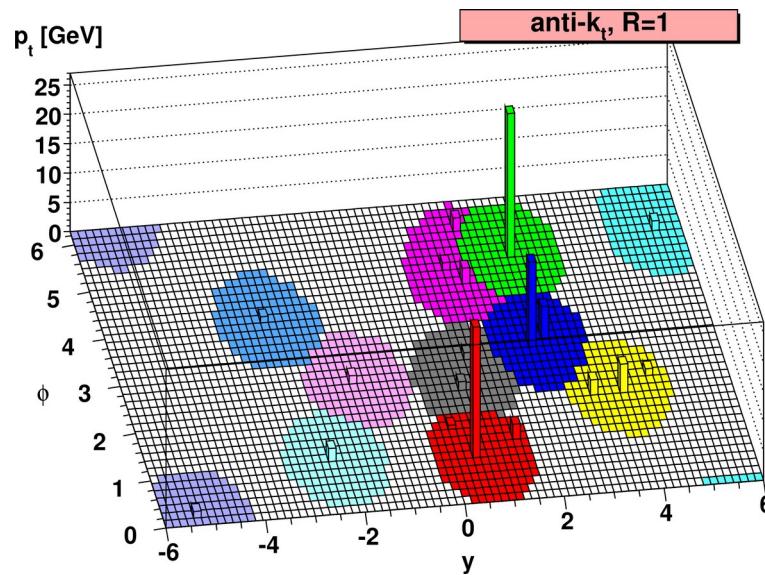
Caveat: flavour- $k_T$  vs. anti- $k_T$

# Flavour anti- $k_T$ ?

The standard algorithm for the LHC is the anti- $k_T$ :

- nice geometric properties
- less sensitive to soft physics

Towards Jetography  
Salam 0906.1833



# New proposals for flavour-safe anti-kT jets

- Flavour with Soft-drop  
**Practical Jet Flavour Through NNLO**  
Caletti, Larkoski, Marzani, Reichelt 2205.01109 SDF
- Flavour anti-kT  
**Infrared-safe flavoured anti-kT jets,**  
Czakon, Mitov, Poncelet 2205.11879 CMP
- Fragmentation approach  
**A Fragmentation Approach to Jet Flavor**  
Caletti, Larkoski, Marzani, Reichelt 2205.01117  
**B-hadron production in NNLO QCD: application to LHC ttbar events with leptonic decays,**  
Czakon, Generet, Mitov and Poncelet, 2102.08267 GHS
- Flavour dressing → standard anti-kT + flavour assignment  
**QCD-aware partonic jet clustering for truth-jet flavour labelling**  
Buckley, Pollard 1507.00508 A dress of flavour to suit any jet  
Gauld, Huss, Stagnitto 2208.11138
- Interleaved flavour neutralisation  
**Flavoured jets with exact anti-kT kinematics and tests of infrared and collinear safety**  
Caola, Grabarczyk, Hutt, Salam, Scyboz, Thaler 2306.07314 IFN
- TBC...

# Flavour anti-kT

Anti-kT:  $d_{ij} = \min(k_{T,i}^{-2}, k_{T,j}^{-2}) R_{ij}^2 \quad d_i = k_{T,i}^{-2}$

Infrared-safe flavoured anti-kT jets,  
Czakon, Mitov, Poncelet 2205.11879

Proposed modification:

A **soft** term designed to modify the distance of flavoured pairs.

$$d_{ij}^{(F)} = d_{ij} \begin{cases} \mathcal{S}_{ij} & i,j \text{ is flavoured pair} \\ 1 & \text{else} \end{cases}$$

$$\mathcal{S}_{ij} \equiv 1 - \theta (1 - \kappa_{ij}) \cos\left(\frac{\pi}{2} \kappa_{ij}\right) \quad \text{with} \quad \kappa_{ij} \equiv \frac{1}{a} \frac{k_{T,i}^2 + k_{T,j}^2}{2k_{T,\max}^2}.$$

A scale to define “soft”  
→ Can be any hard scale

Allow systematic variations

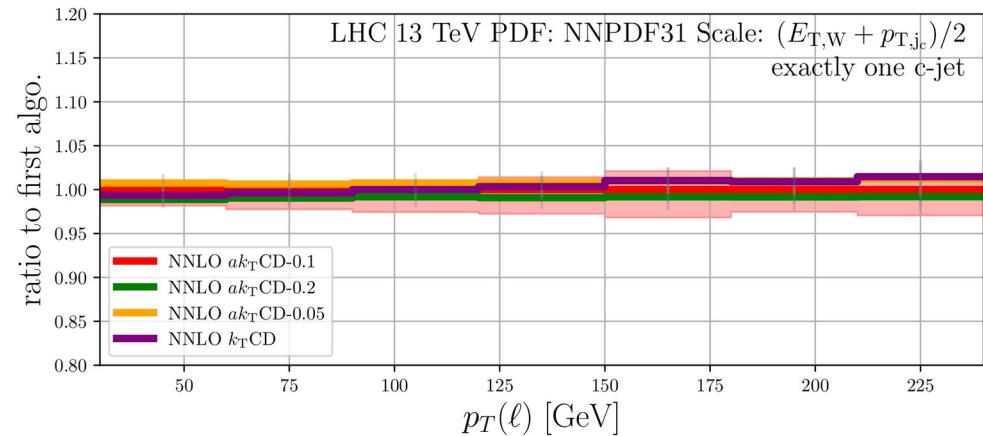
**Variant:**  
2306.07314

$$\mathcal{S}_{ij} \rightarrow \bar{\mathcal{S}}_{ij} = \mathcal{S}_{ij} \frac{\Omega_{ij}^2}{\Delta R_{ij}^2} \quad \Omega_{ik}^2 \equiv 2 \left[ \frac{1}{\omega^2} (\cosh(\omega \Delta y_{ik}) - 1) - (\cos \Delta \phi_{ik} - 1) \right]$$

# W+charm - jet algorithm dependence

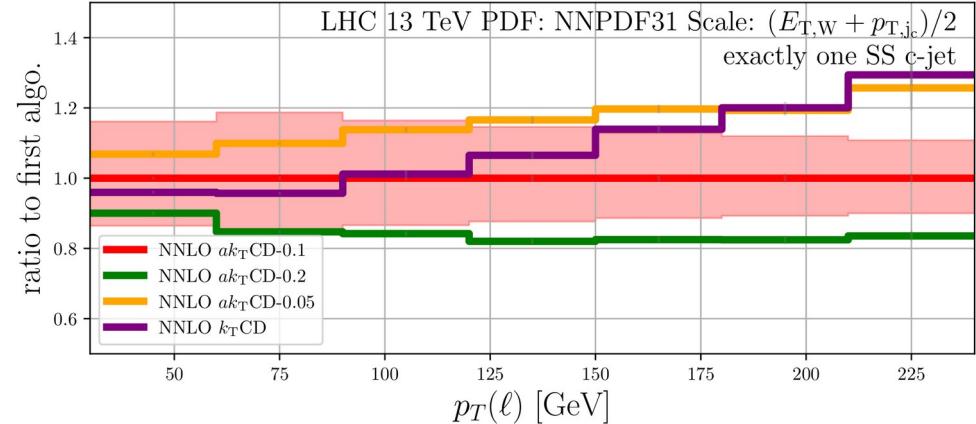
Exactly one c-jet requirement (OS+SS):

- Comparison of parameters  $a$ :  
→ small dependence < 2%
- Comparison to flv-kT:  
→ small dependence @ NNLO < 2%



ONLY large effect in SS contribution

- Exactly one c-jet of SS type:  
Larger dependence ~15%  
(roughly size of NNLO scale band)
- BUT: SS contribution ~2-5%
- => OS ~0.2-0.5% dependence



# Comparison to CMS data

Measurement of the production cross section for a W boson in association  
with a charm quark in proton-proton collisions at  $\text{Sqrt}(s) = 13 \text{ TeV}$   
CMS 2308.02285

Similar phase space:

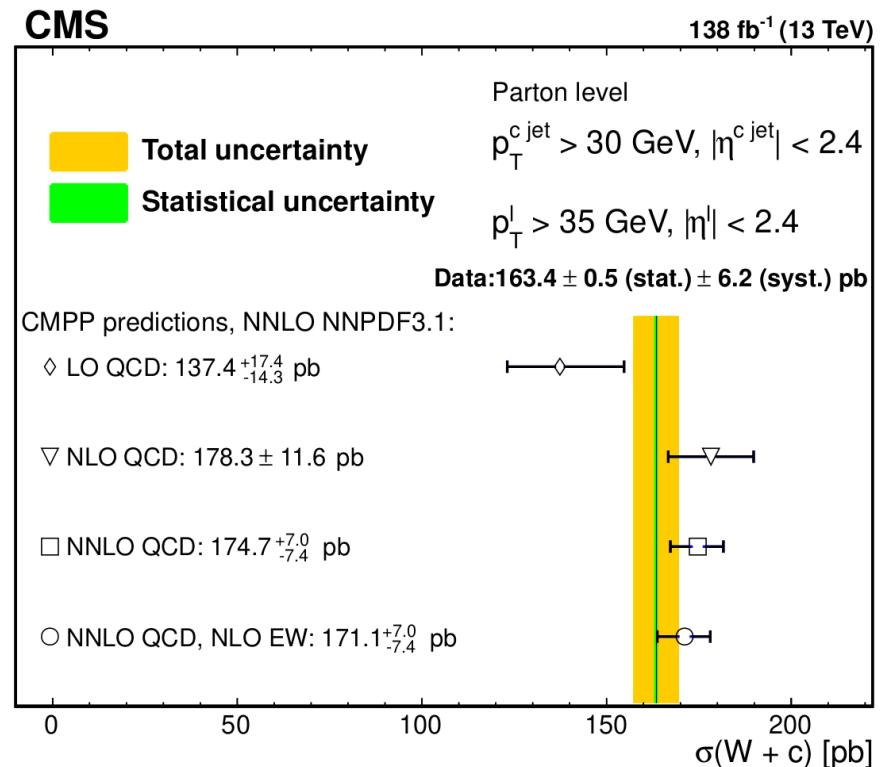
$$p_T^\ell > 35 \text{ GeV}, |\eta^\ell| < 2.4, p_T^{\text{c jet}} > 30 \text{ GeV}$$

$$|\eta^{\text{c jet}}| < 2.4, \Delta R(\text{jet}, \ell) > 0.4$$

Measurement of OS – SS cross-section  
unfolded to parton-level (anti-kT algorithm)

→ hadronisation and fragmentation corr.  $\sim 10\%$

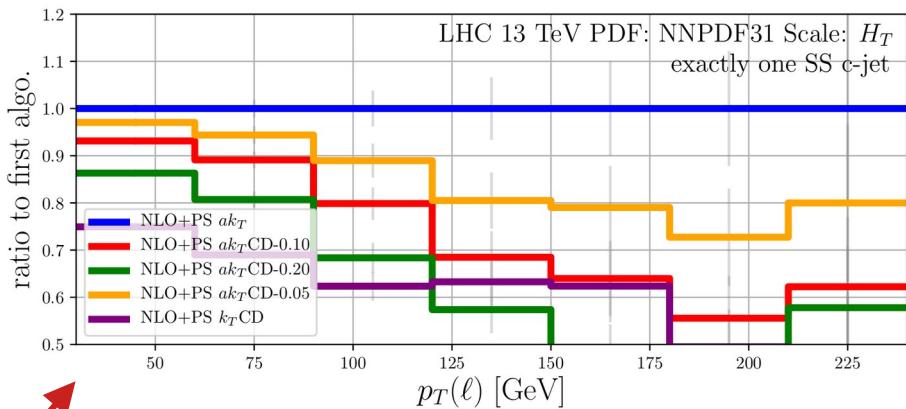
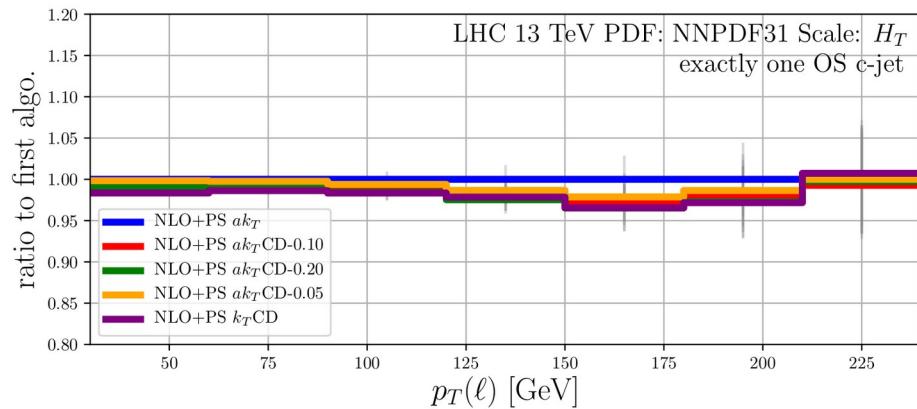
+ anti-kT → flv. Anti-kT correction on fixed-order



Not ideal but a full flv. Anti-kT unfolding was not feasible at that time...

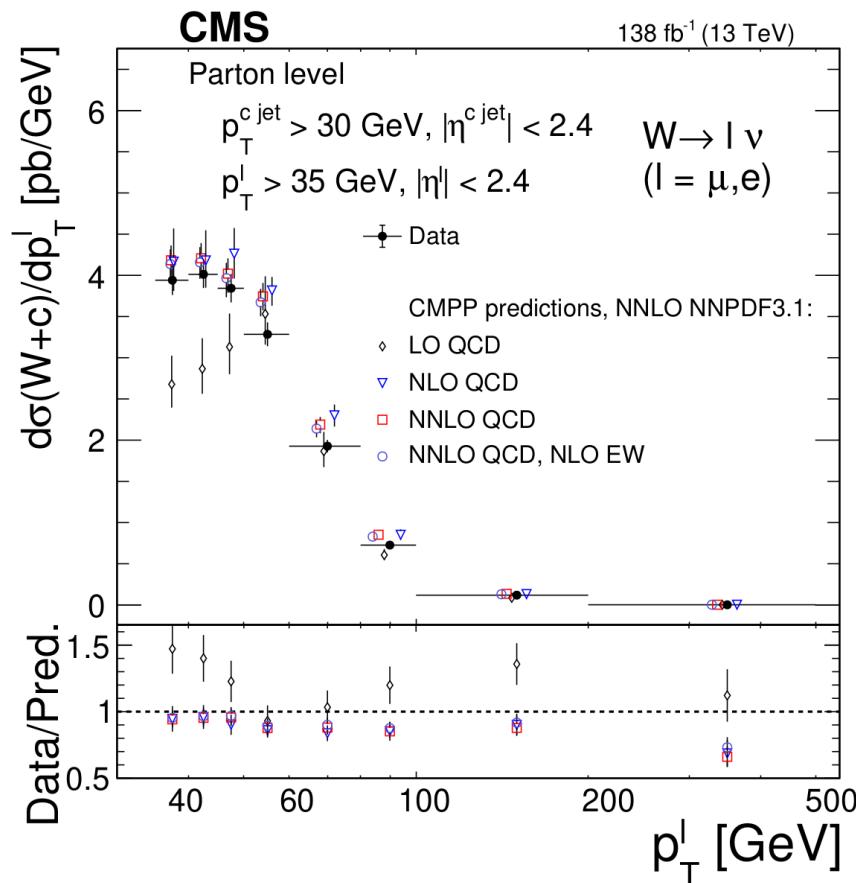
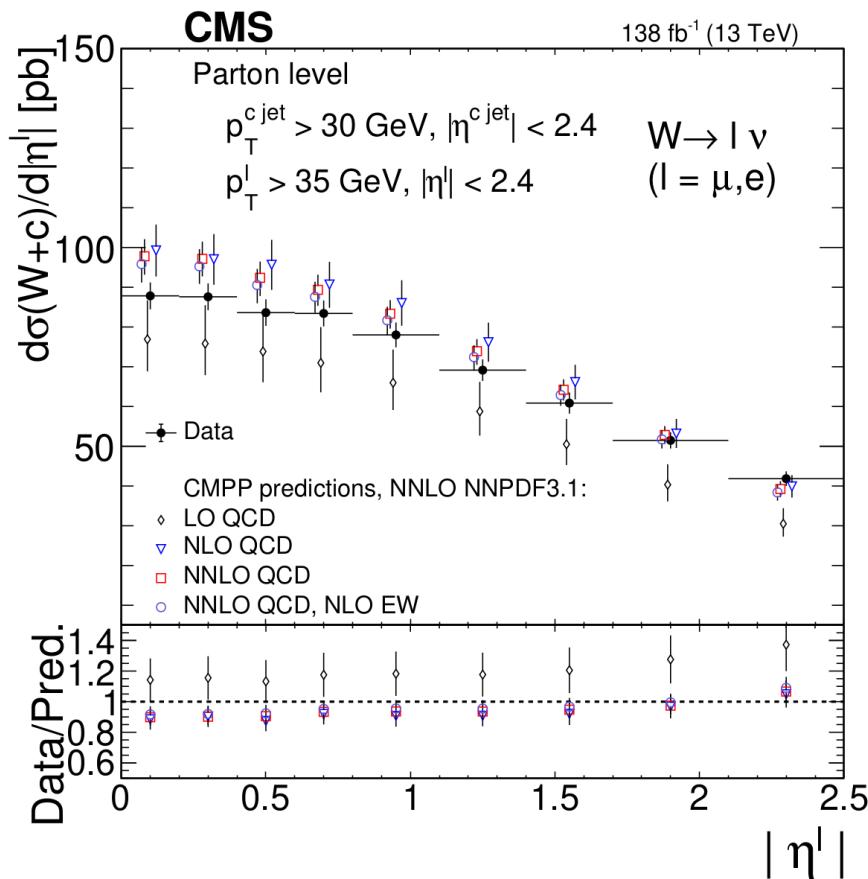
# Unfolding corrections

NLO+PS (fl. anti- $k_T$ ) / NLO+PS (anti- $k_T$ )



SS  $\sim$  2-5% of OS  
 $\rightarrow$  OS – SS unfolding corrections < 2%

# Comparison to CMS data



# Comparison of flavoured jet algorithms

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# Comparisons

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Les Houches 23 workshop ( aka FlavourFest : ) )

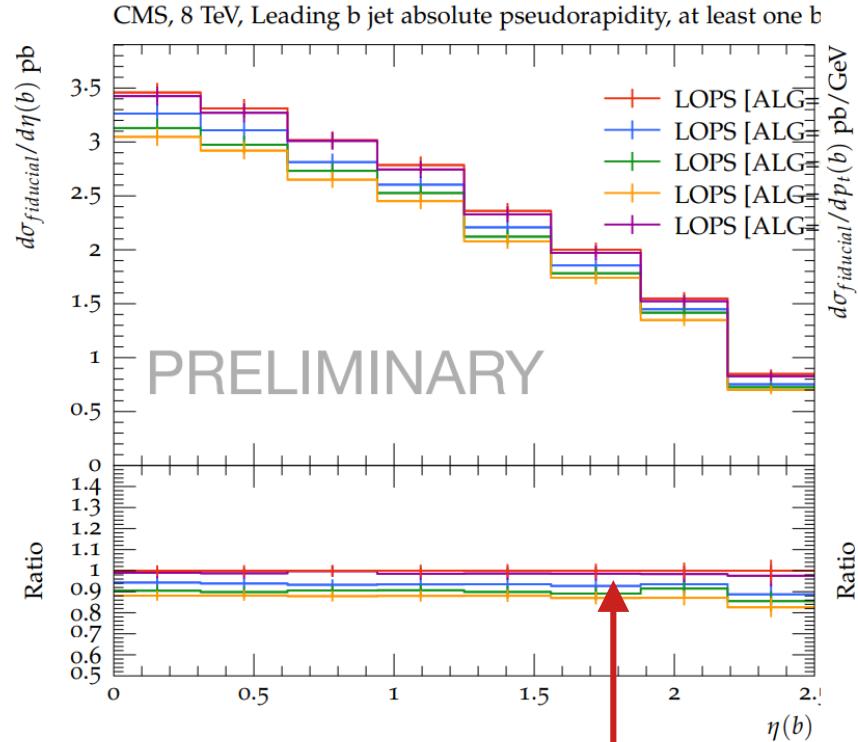
- CMPΩ: Flavour anti-kT (with fixed  $S_{ij}$ )
- SDF: Flavour with Soft-drop (only IR-safe up to  $\alpha_s^2$  corrections)
- GHS: Flavour dressing → standard anti-kT + flavour assignment
- IFN: Interleaved flavour neutralisation

Implementation in  
FastJet package

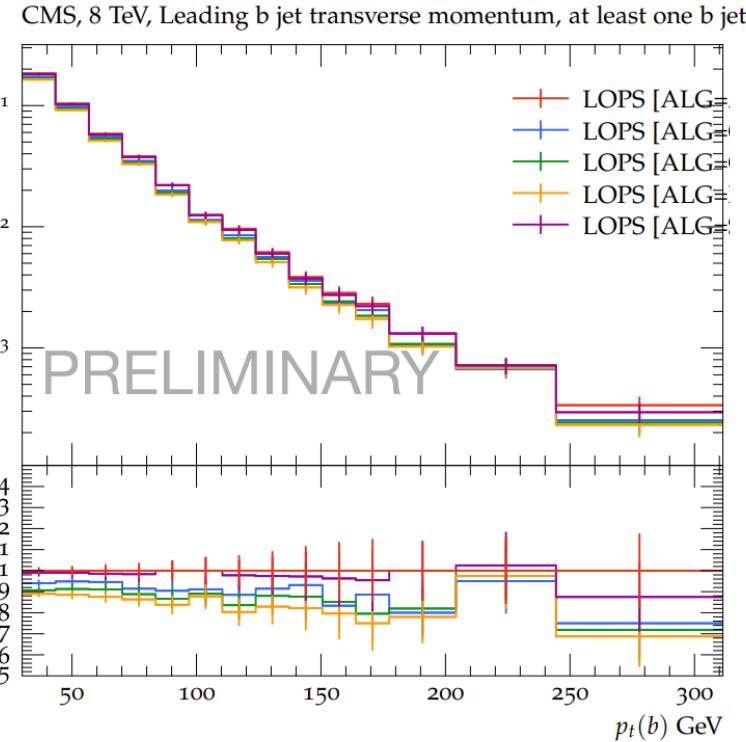
Benchmark process: Z+b-jet following CMS analysis 1611.06507

# Comparison with parton showers

HERWIG LO PS



Les Houches Jet Flavour WG

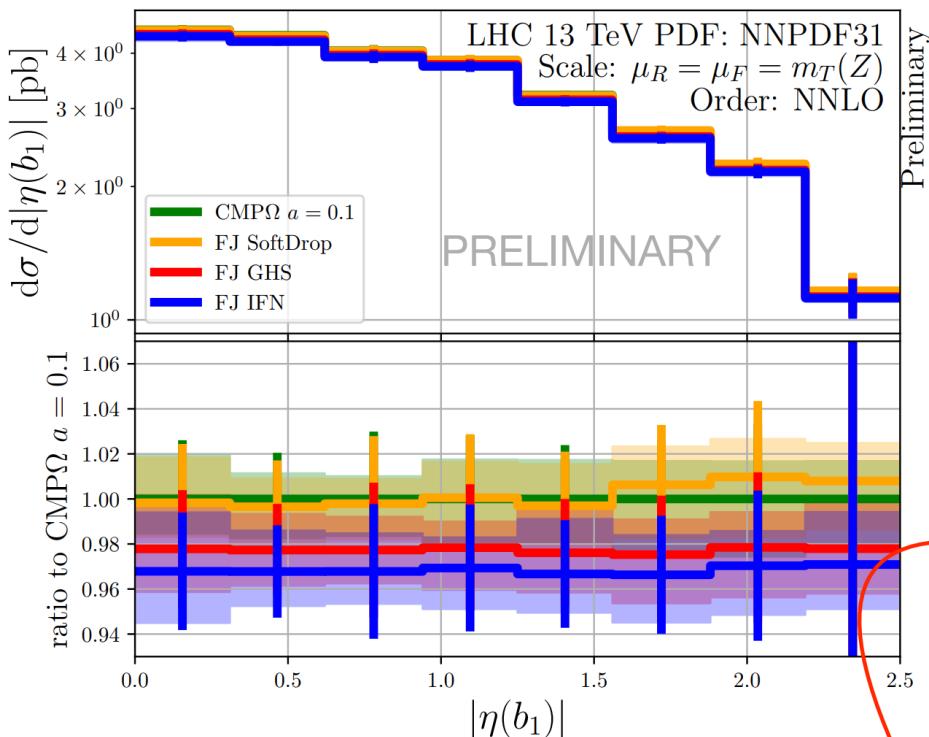


SDF  $\sim$  anti- $k_T$   $\rightarrow$  consequence of IR unsafety at higher orders?

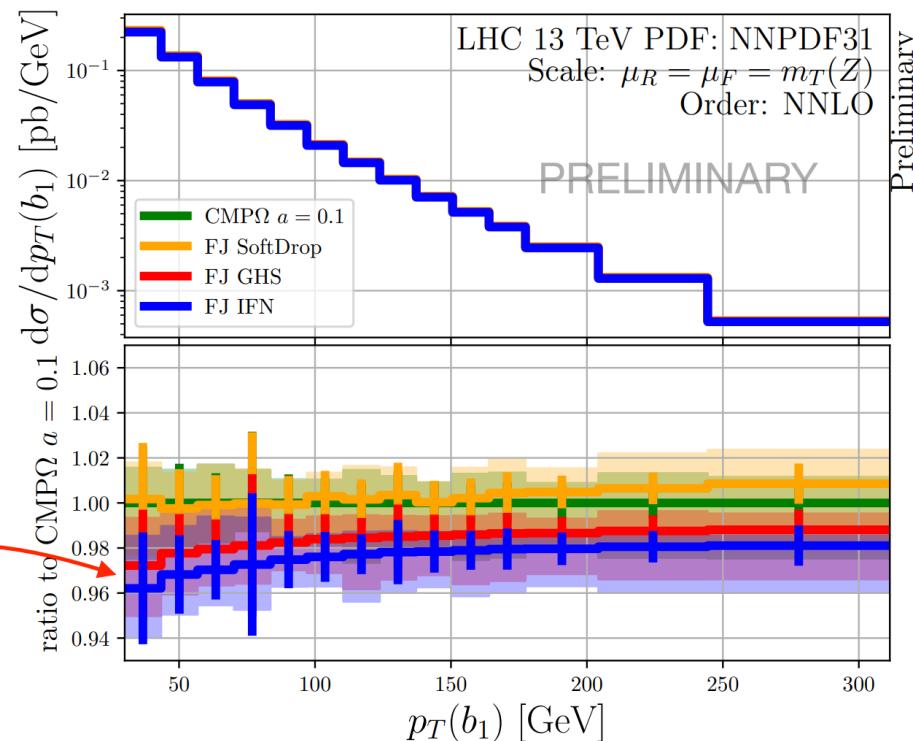
# NNLO QCD comparisons

Calculations performed with sector-improved residue subtraction scheme  
1408.2500 & 1907.12911

Les Houches Jet Flavour WG



interesting shape difference at  
low  $p_T$ : it deserves further  
investigation!

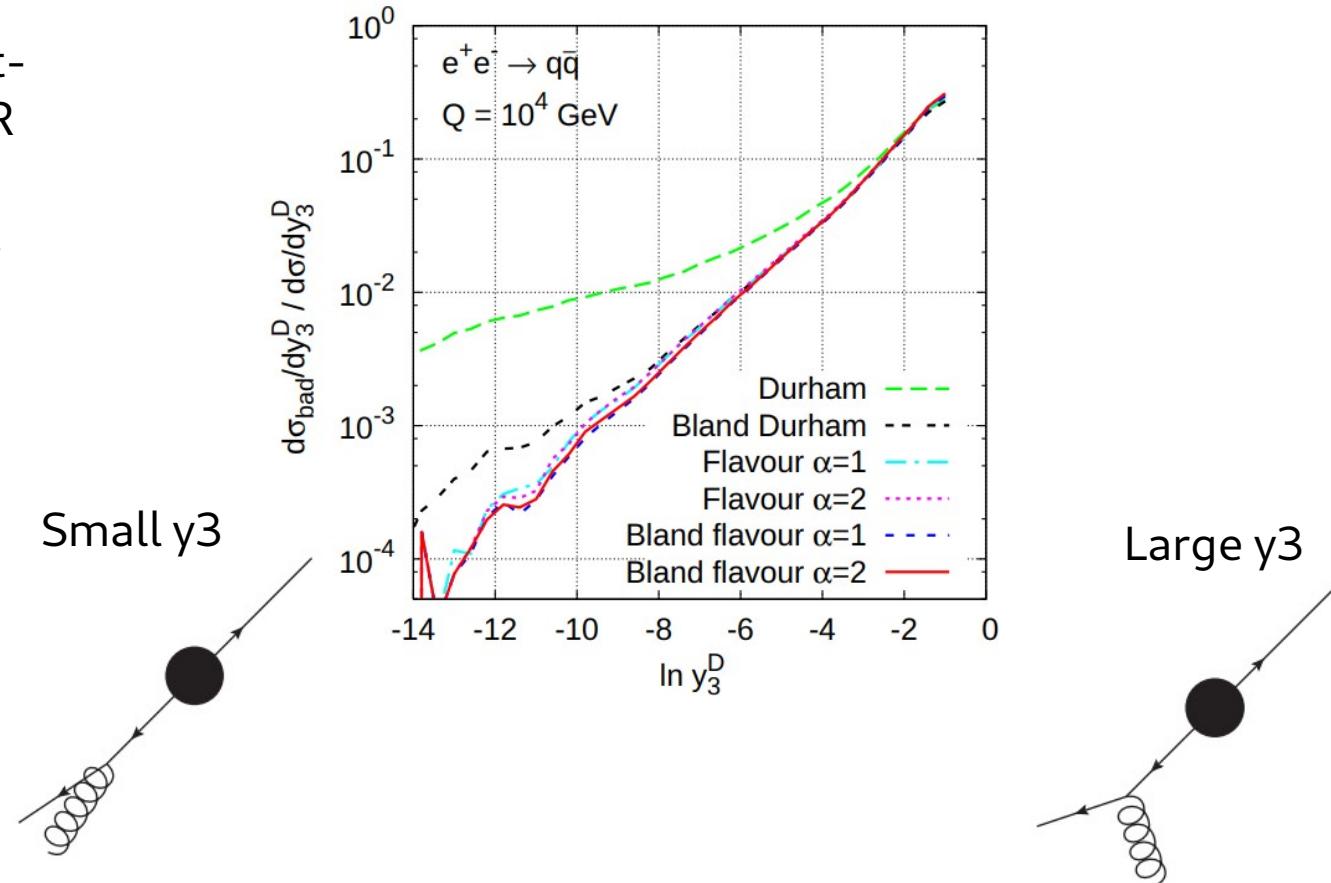


# Tests of IR safety

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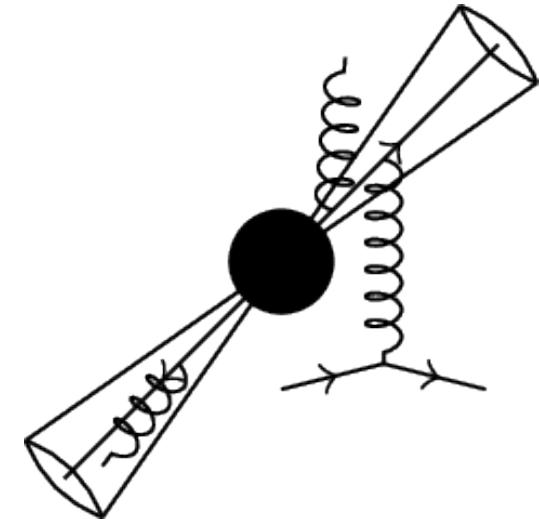
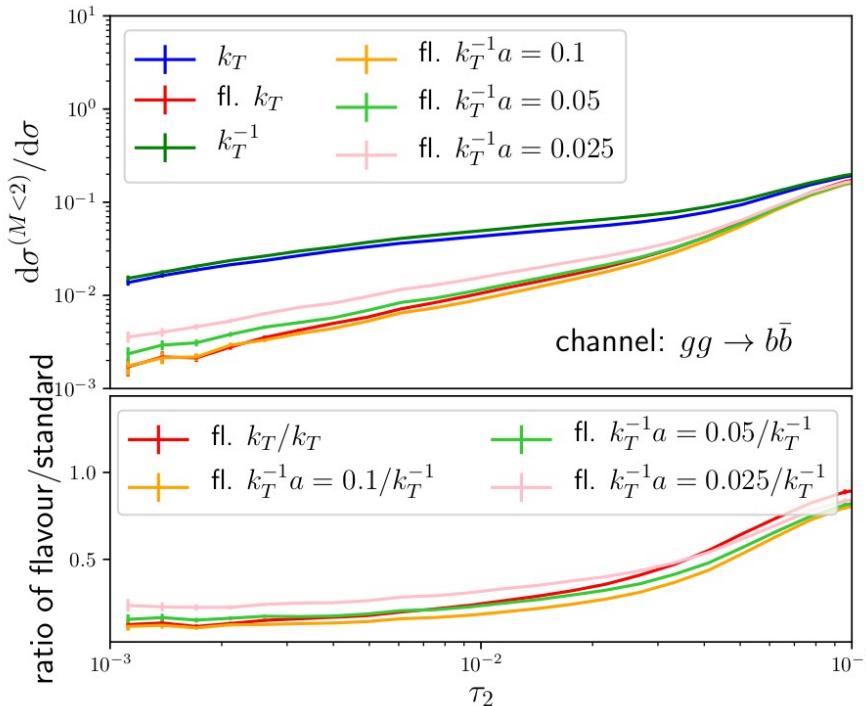
# Tests of IR safety

- Rate of bad-identified jet-flavour as a function of IR sensitive variable
- Parton-shower to model many emissions



# Tests of IR safety with parton showers

In the di-jet limit the flavour needs to correspond to tree level flavours  
→ misidentification rate needs to vanish in di-jet back-to-back limit  
→ IR sensitive observable 2-jettiness



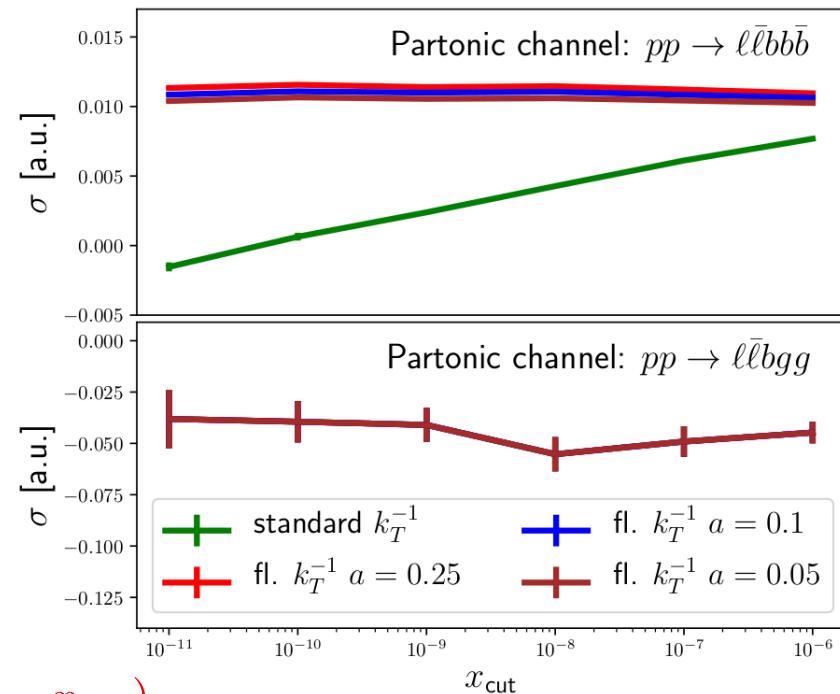
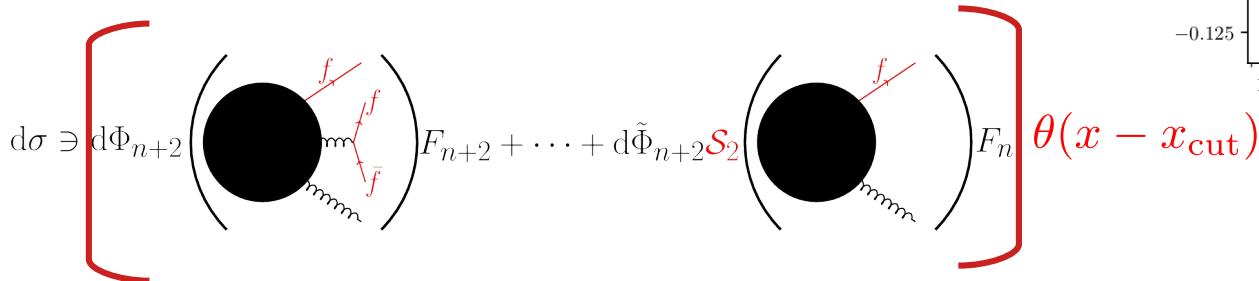
# Tests of IR safety with NNLO FO computations

IR sensitivity of jet cross sections on (technical)  
IR regulating parameter  $x$

In the limit  $x_{\text{cut}} \rightarrow 0$ :

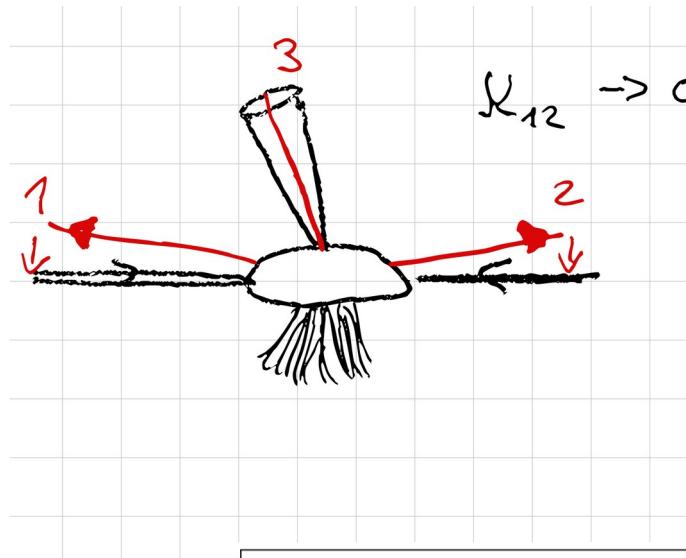
IR safe jet flavour  $\rightarrow$  no dependence on  $x_{\text{cut}}$

IR non-safe jet flavour  $\rightarrow$  logarithmic divergent

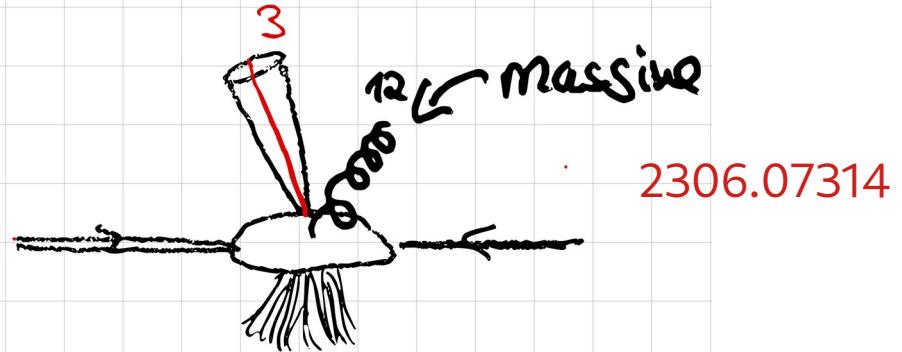


# New developments...

Issue for double collinear limits wrt. to initial states



Many thanks to  
Caola, Grabarczyk, Hutt, Salam, Scyboz, Thaler



if  $y_{12} - y_3 < R$

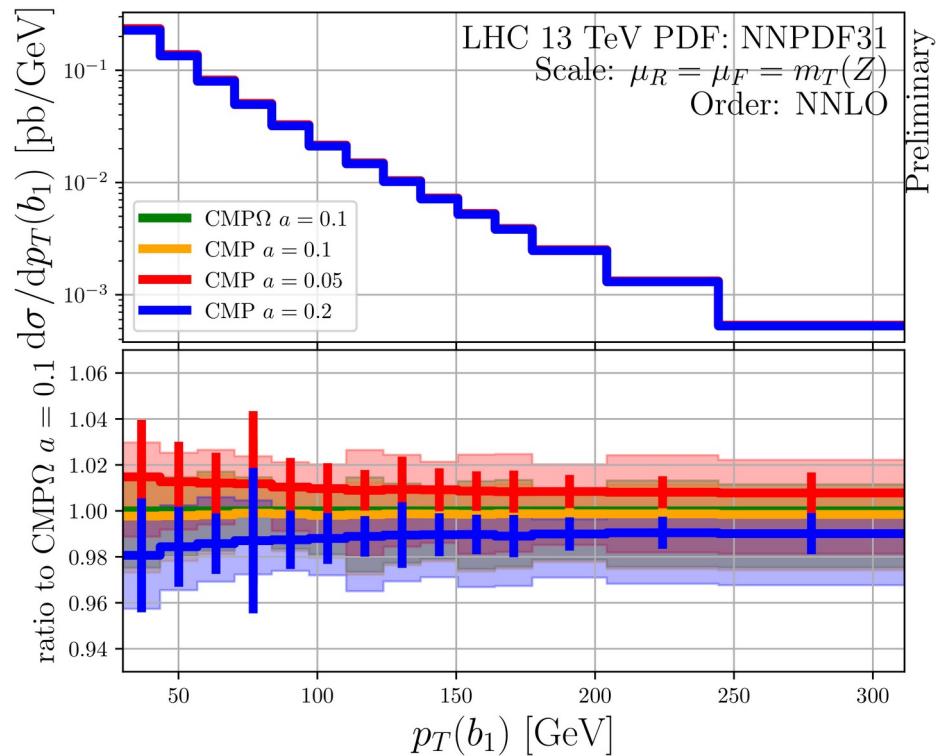
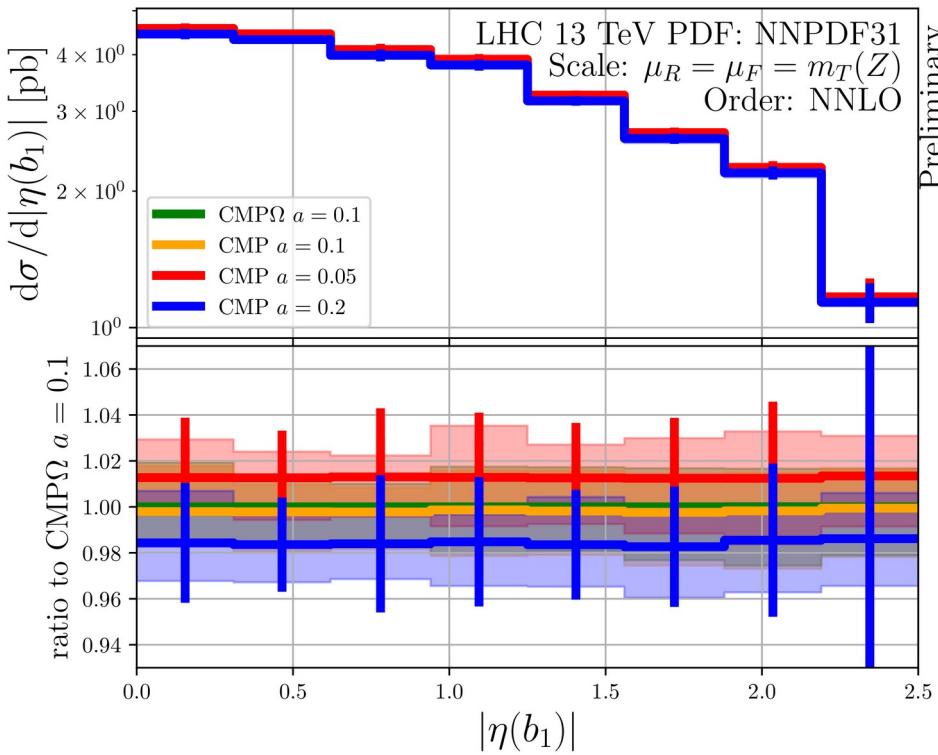
$$\mathcal{S}_{ij} \equiv 1 - \theta(1 - \kappa_{ij}) \cos\left(\frac{\pi}{2}\kappa_{ij}\right) \quad \text{with} \quad \kappa_{ij} \equiv \frac{1}{a} \frac{k_{T,i}^2 + k_{T,j}^2}{2k_{T,\max}^2}.$$

Their proposal:  $\mathcal{S}_{ij} \rightarrow \bar{\mathcal{S}}_{ij} = \mathcal{S}_{ij} \frac{\Omega_{ij}^2}{\Delta R_{ij}^2}$        $\Omega_{ik}^2 \equiv 2 \left[ \frac{1}{\omega^2} (\cosh(\omega \Delta y_{ik}) - 1) - (\cos \Delta \phi_{ik} - 1) \right]$

# Flavour anti-kT: impact of $\Omega_{ij}$

Calculations performed with sector-improved residue subtraction scheme  
1408.2500 & 1907.12911

Les Houches Jet Flavour WG



Negligible difference between  $\text{CMP}\Omega$  and  $\text{CMP}$

# Summary

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# Take home messages

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- 1) NNLO QCD effects in W+charm largely understood.  
First comparisons to data → steps towards W+charm in PDF fits
- 2) Flavoured jets require modified jet algorithms to avoid IR safety/sensitivity issues.  
Solutions exists for anti- $k_T$  jets and are implemented in FastJet: SDF, CMP, GHS, IFN, ...  
→ phenomenological applications @ NNLO QCD
- 3) Still open question regarding the best way of comparing state-of-the-art predictions and measurements with flavoured jets:  
→ Unfolding? How do the different algorithms compare?  
→ Which flavoured jet algorithm has the most favourable properties?

# Backup

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# LHC precision computations with flavoured jets

Associated Higgs production + decays in b-quarks:

**Associated production of a Higgs boson decaying into bottom quarks at the LHC in full NNLO QCD**  
Ferrera, Somogyi, Tramontano 1705.10304

**NNLO QCD corrections to associated WH production and  $H \rightarrow b\bar{b}$  decay**  
Caola, Luisoni, Melnikov, Röntsch 1712.06954

**Associated production of a Higgs boson decaying into bottom quarks and a weak vector boson decaying leptonically at NNLO in QCD**  
Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 1907.05836

**Bottom quark mass effects in associated WH production with the  $H \rightarrow b\bar{b}$  decay through NNLO QCD**  
Behring, Bizoń, Caola, Melnikov, Röntsch 2003.08321

**VH + jet production in hadron-hadron collisions up to order  $\alpha_s^3$  in perturbative QCD**  
Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 2110.12992

+Partonshower:

**NNLOPS accurate associated HZ production with  $H \rightarrow b\bar{b}$  decay at NLO**  
Astill, Bizoń, Re, Zanderighi 1804.08141

**NNLOPS description of the  $H \rightarrow b\bar{b}$  decay with MiNLO**  
Bizoń, Re, Zanderighi 1912.09982

**Next-to-next-to-leading order event generation for VH production with  $H \rightarrow b\bar{b}$  decay**  
Zanoli, Chiesa, Re, Wiesemann, Zanderighi 2112.04168

# LHC precision computations with flavoured jets

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Vector + flavoured jet(s) production:

**NLO QCD predictions for Wbbbar production in association with up to three light jets at the LHC**  
Anger, Cordero, Ita, Sotnikov 1712.05721

**Predictions for Z-Boson Production in Association with a b-jet at O( $\alpha_s^3$ )**  
Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 2005.03016

**NNLO QCD predictions for W+c-jet production at the LHC,**  
Czakon, Mitov, Pellen, Poncelet 2011.01011

**NNLO QCD corrections to Wbbbar production at the LHC,**  
Hartanto, Poncelet, Popescu, Zoia 2205.01687

**A detailed investigation of W+c-jet at the LHC,**  
Czakon, Mitov, Pellen, Poncelet 2212.00467

**Associated production of a W boson and massive bottom  
quarks at next-to-next-to-leading order in QCD,**  
Buonocore, Devoto, Kallweit, Mazzitelli, Rottoli, Savoini, 2212.04954

**NNLO QCD predictions for Z-boson production in association with a charm jet within the LHCb fiducial region**  
Gauld, Gehrmann-De Ridder, Glover, Huss, Rodriguez Garcia, Stagnitto 2302.12844

**Precise QCD predictions for W-boson production  
in association with a charm jets**  
Gehrmann-De Ridder, Gehrmann, Glover, Huss, Garcia, Stagnitto, 2311.14991

# Benchmark process: Z+b-jet

Well studied up to  $\mathcal{O}(\alpha_s^3)$ :

Predictions for Z-Boson Production in Association with a b-jet at  $\mathcal{O}(\alpha_s^3)$ ,

Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 2005.03016

- Flavour-kT algorithm
- Unfolding of experimental data (RooUnfold, bin-by-bin unfolding)
- Matching between four- and five-flavour schemes (FONLL)

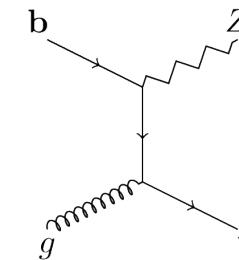
$$d\sigma^{\text{FONLL}} = d\sigma^{5\text{fs}} + (d\sigma_{m_b}^{4\text{fs}} - d\sigma_{m_b \rightarrow 0}^{4\text{fs}})$$

- CMS measurement @ 8 TeV

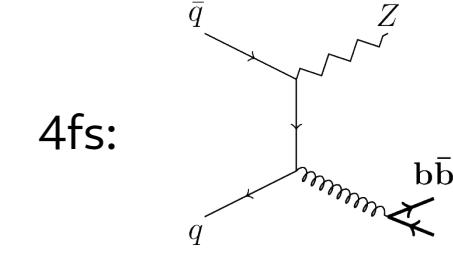
Measurements of the associated production of a Z boson and b jets in pp collisions at  $\sqrt{s} = 8 \text{ TeV}$ , CMS 1611.06507

→ Ideal testing ground for flavour anti-kT

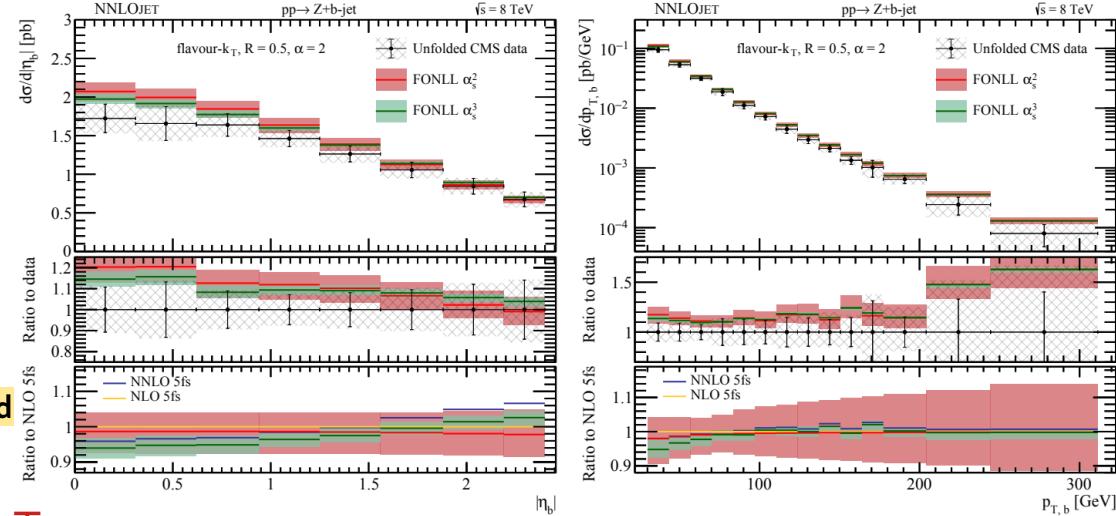
$pp \rightarrow Z(l\bar{l}) + b\text{-jet}$



5fs:



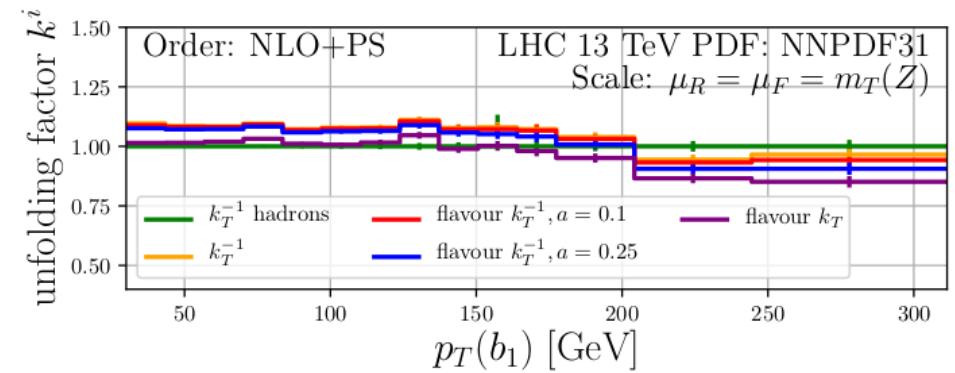
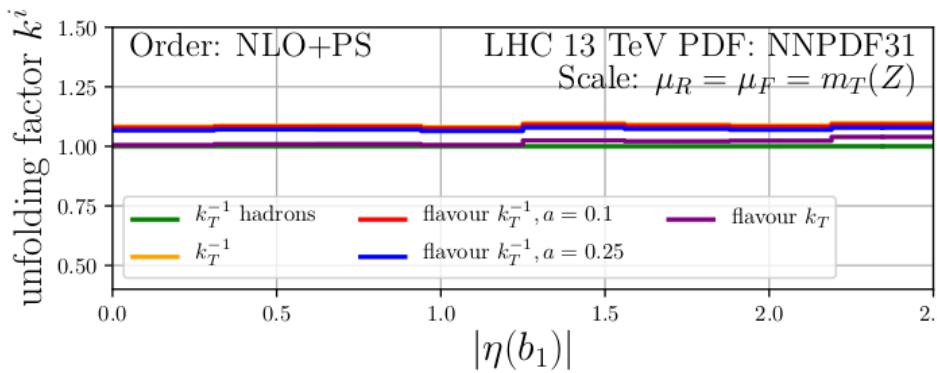
4fs:



# Bin-by-bin unfolding

Estimation of hadronisation and experimental tagging corrections  
→ NLO + PS (Madgraph+Pythia8)

Unfolding factor = NLO+PS (had = Off) / NLO+PS (had = On)



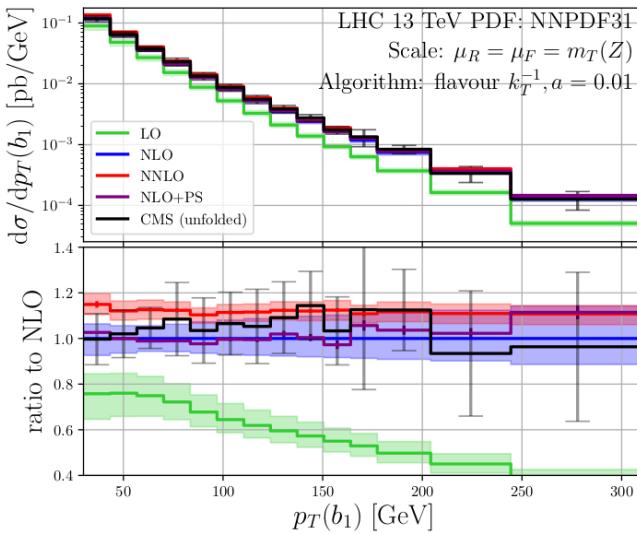
# Z+b-jet Phenomenology: Tunable parameter

Benchmark process:  $\text{pp} \rightarrow Z(\text{ll}) + \text{b-jet}$

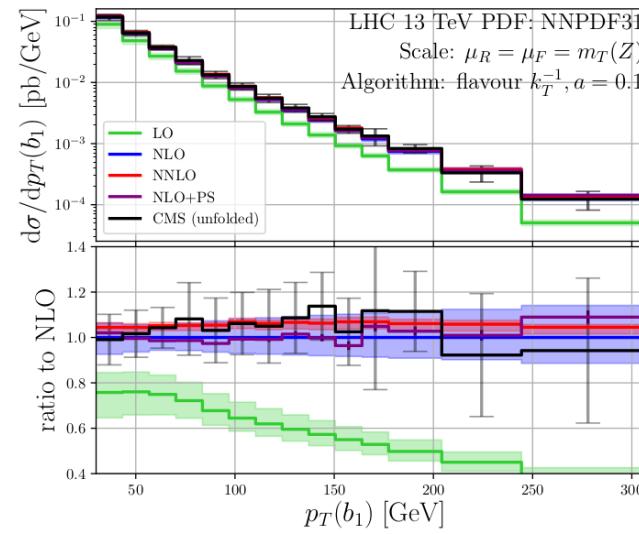
Tunable parameter a:

- Limit  $a \rightarrow 0 \Leftrightarrow$  original anti- $k_T$  (IR unsafe)
- Large  $a \Leftrightarrow$  large modification of cluster sequence

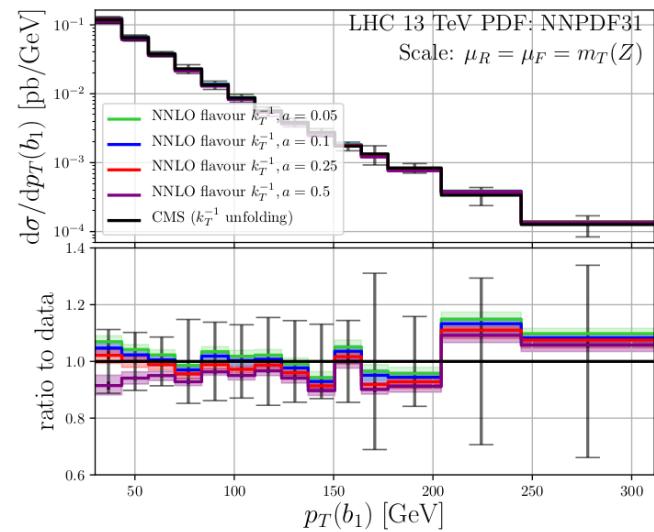
Flavour anti- $k_T$  ( $a=0.01$ ):



Flavour anti- $k_T$  ( $a=0.1$ ):

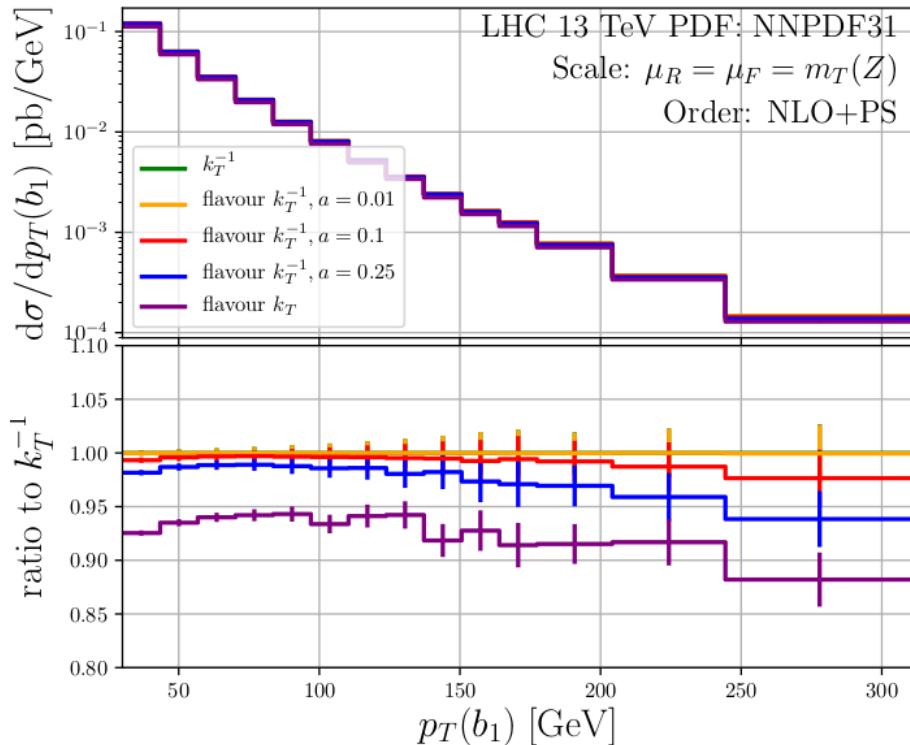


Comparison of different parameter a to data:



# Z+b-jet Phenomenology: Tunable parameter II

What happens in the presence of many flavoured partons? → NLO PS



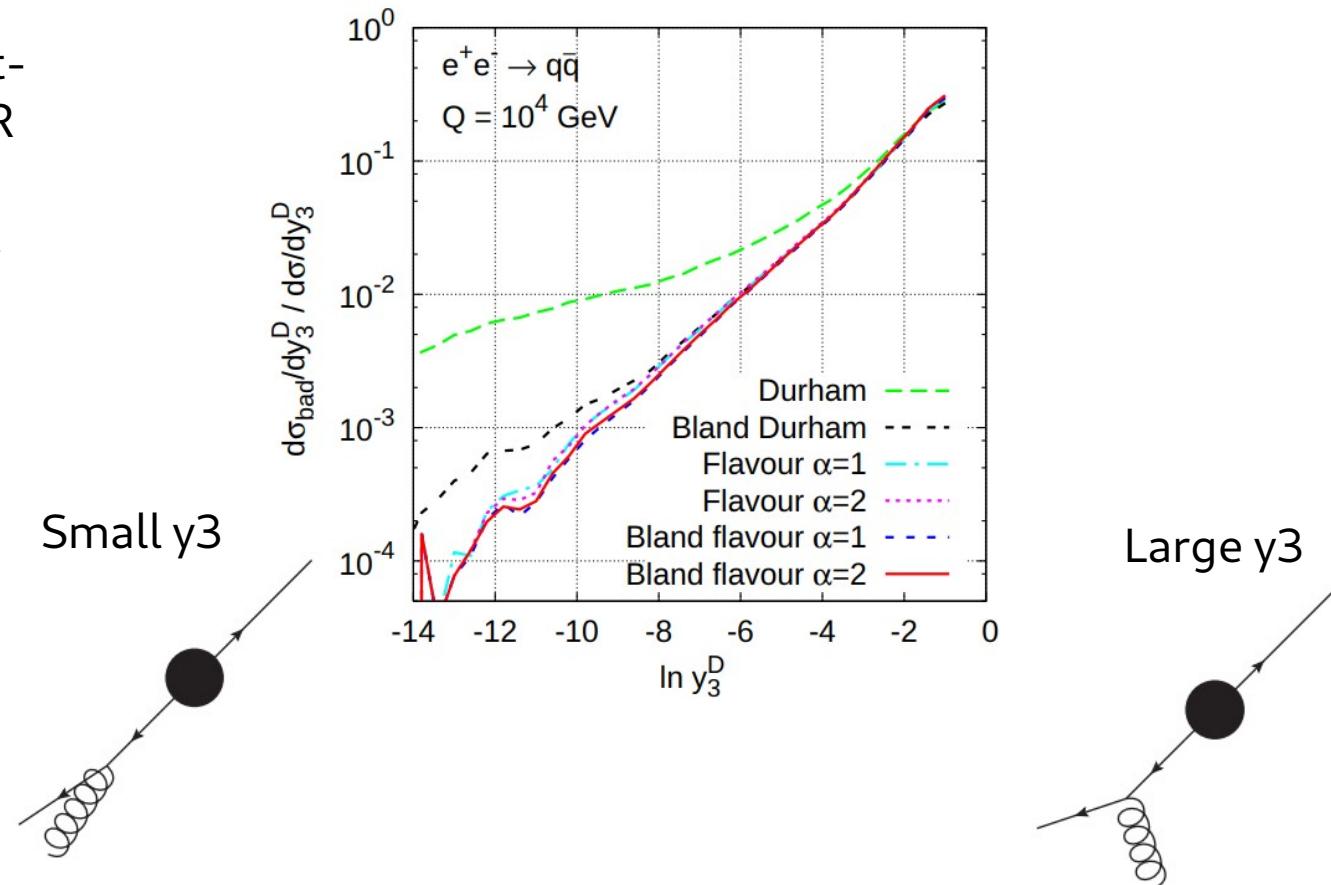
Tunable parameter a:

- Small a: Flavour anti- $k_T$  results are more similar to standard anti- $k_T$
- Larger a: Larger modification of clustering

Good FO perturbative convergence +  
Small difference to standard anti- $k_T$   
→ a~0.1 is a good candidate

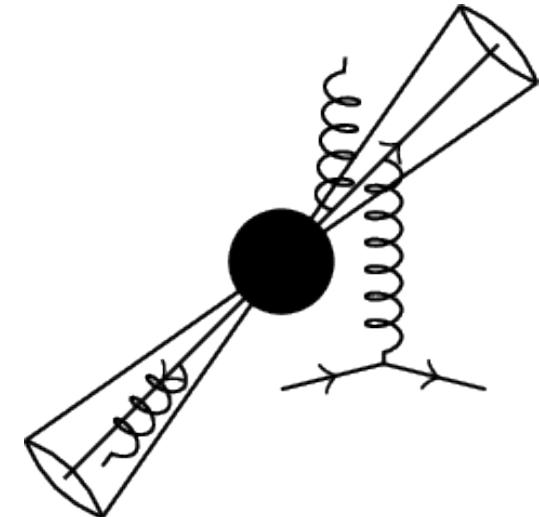
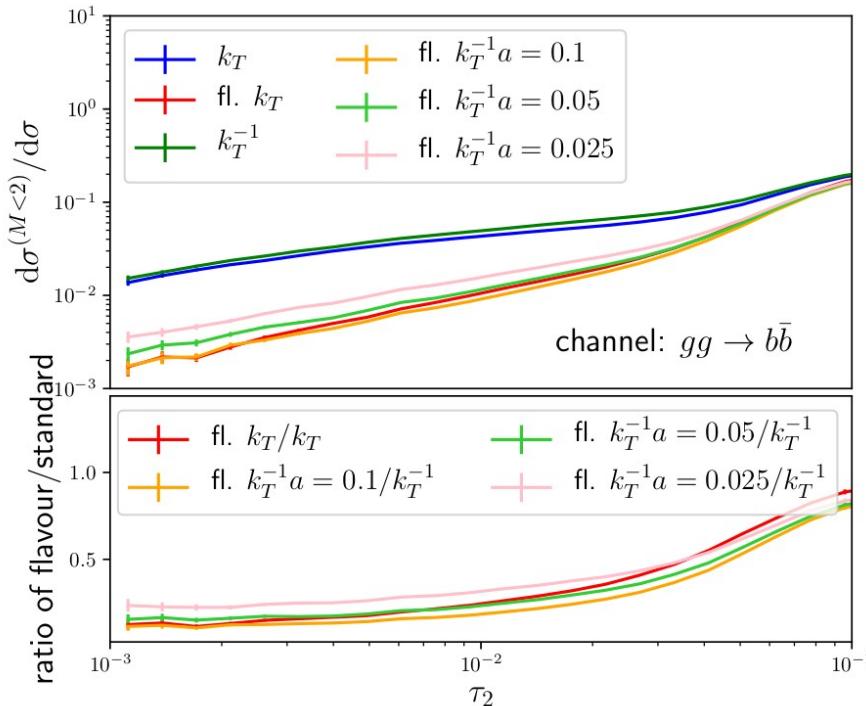
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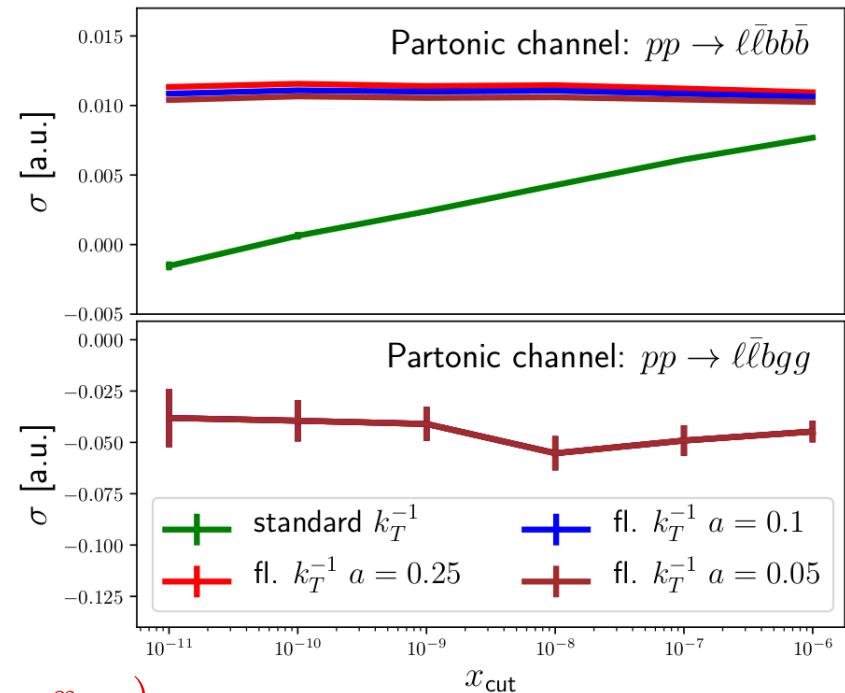
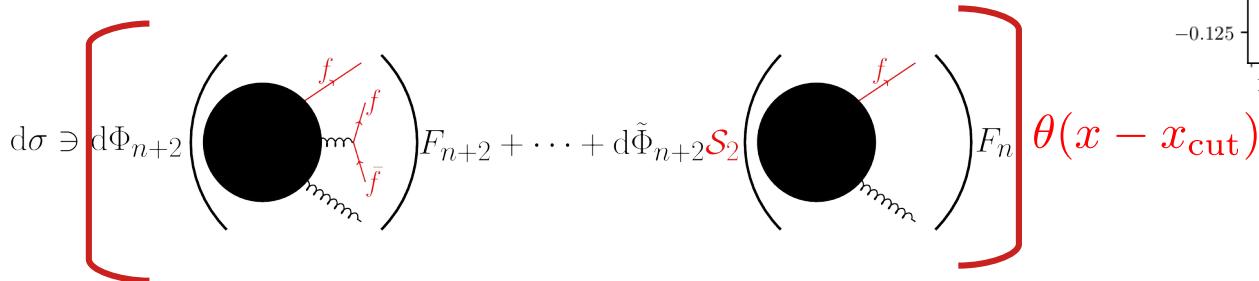
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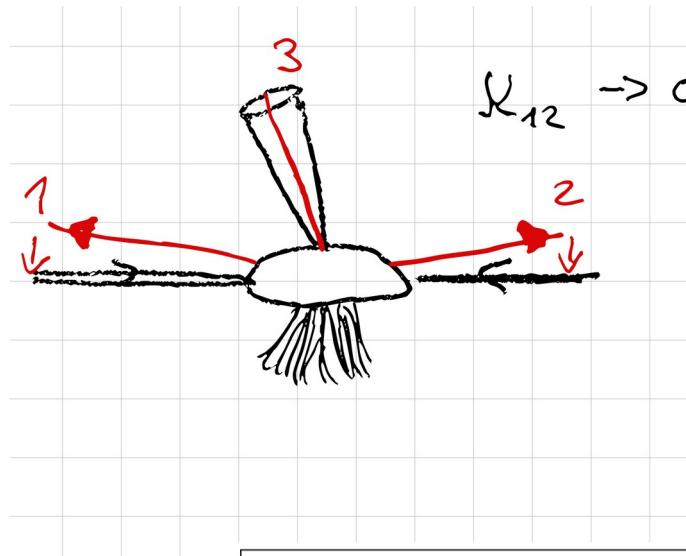
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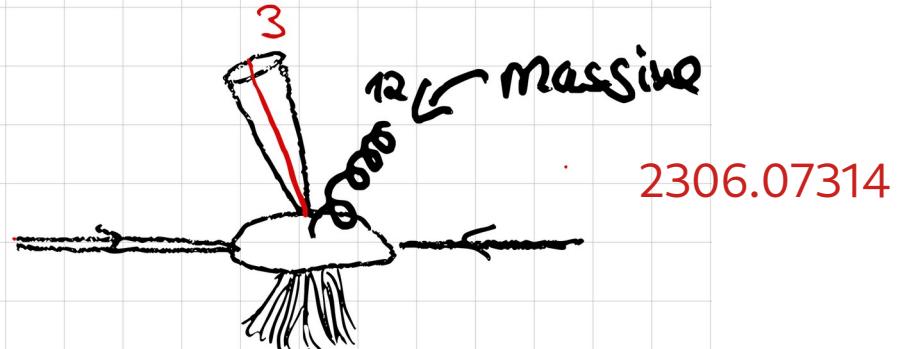


# New developments...

Issue for double collinear limits wrt. to initial states



Many thanks to  
Caola, Grabarczyk, Hutt, Salam, Scyboz, Thaler



if  $y_{12} - y_3 < R$

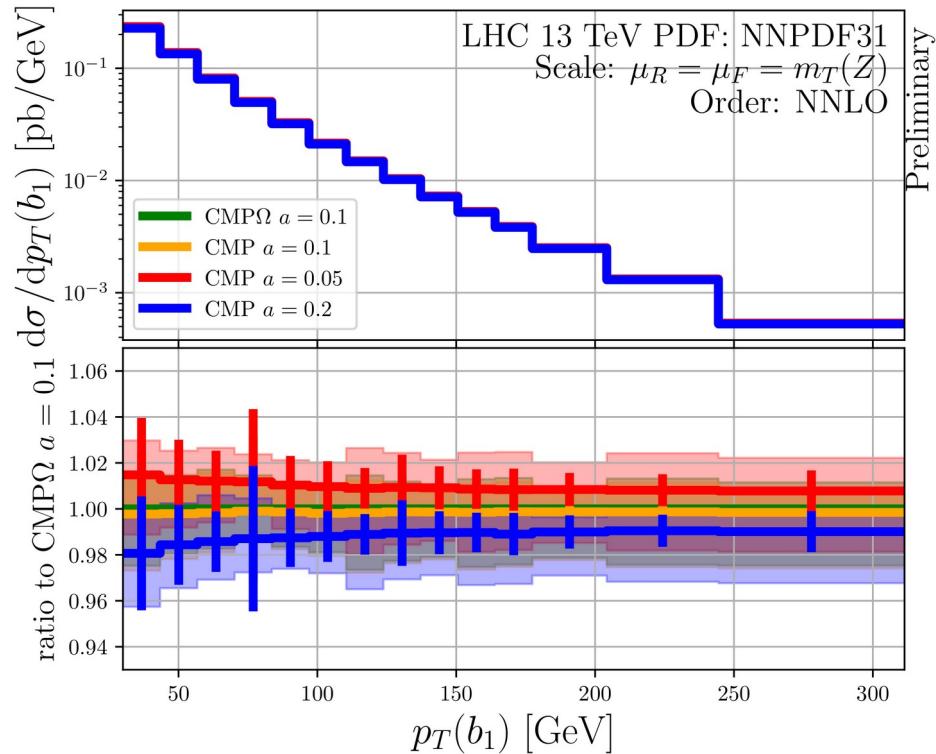
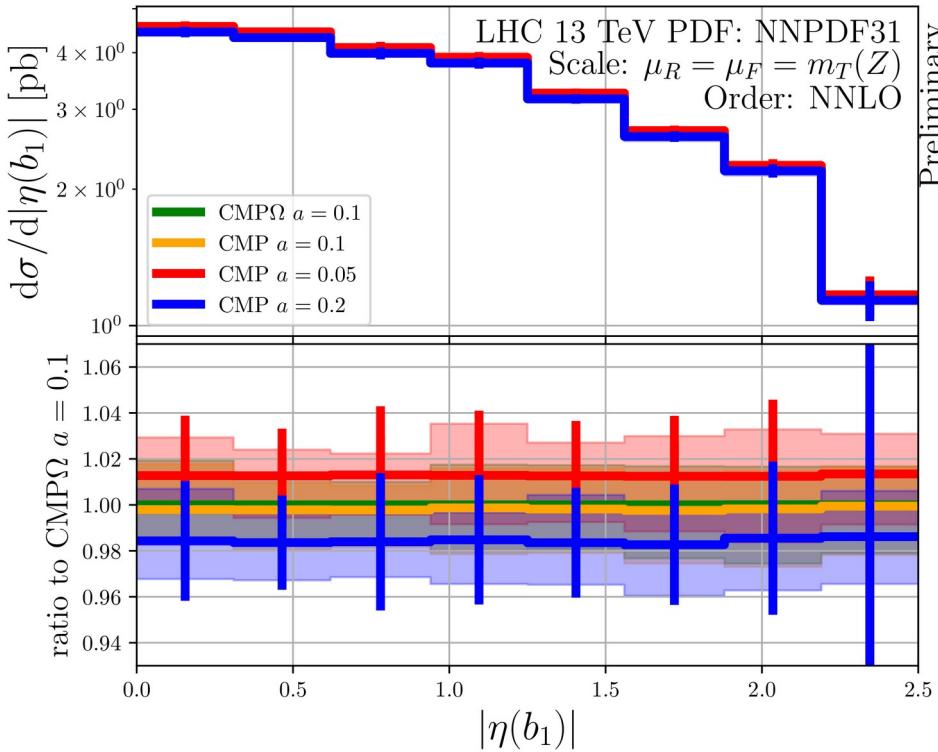
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1408.2500 & 1907.12911

Les Houches Jet Flavour WG



Negligible difference between  $\text{CMP}\Omega$  and  $\text{CMP}$

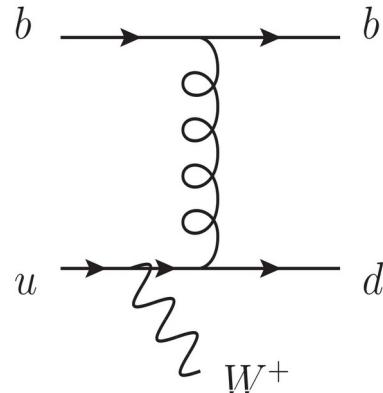
# W + bottom-pairs

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# $W + b$ - jets

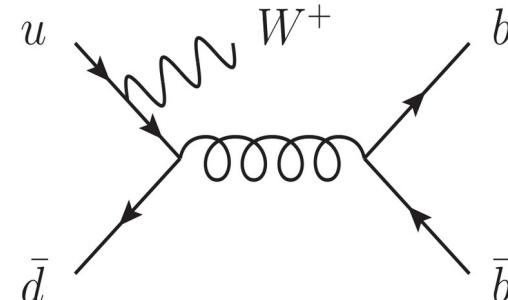
Motivation: → testing perturbative QCD: large NLO QCD corrections, 4FS vs. 5 FS  
→ modelling of flavoured jets

$W + 1b$ -jet



→ probe b quark PDFs

$W + 2b$ -jet



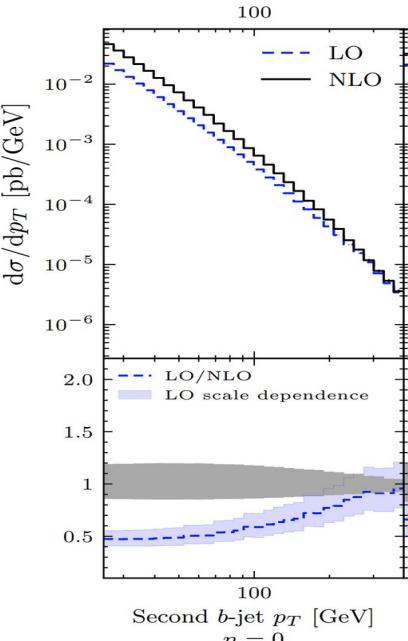
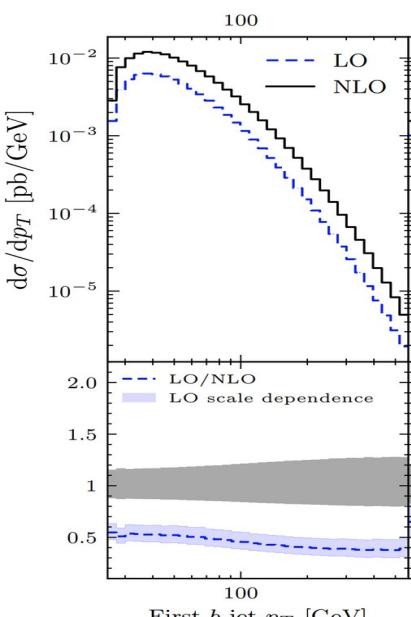
background for:  
→  $WH(H \rightarrow bb)$   
→ single top

# NLO QCD corrections

Experiment: [D0,1210.0627,0410062] [ATLAS,1109.1470,1302.2929][CMS,1312.6608,1608.07561]

Theory W+1 b-jet: [Campbell et al,0611348,0809.3003][Caola et.al.,1107.3714]

Theory W+2 b-jet:  
mb=0 [Ellis et al,9810489] onshell W: [Cordero et al,0606102 ]W(lv)bb: [Campbell et al,1011.6647]  
NLO+PS: [Oleari et al,1105.4488][Frederix et al,1110.5502] W(lv)bb: [Luisoni et al,1502.01213 ]  
W(lv)bb+ $\leq$ 3]: [Anger et al, 1712.05721]



- Large NLO QCD corrections + scale dependence
- Opening of qg-channel
- NNLO QCD corrections required!  
Main challenges:
  - Twoloop amplitudes [Bager'21,Hartanto'22]
  - Subtraction for high-multiplicity processes → Stripper [Czakon'10'14'19]

# Setup

**NNLO QCD corrections to Wbb production at the LHC**  
 Hartanto, Poncelet, Popescu, Zoia 2205.01687

- LHC @ 8 TeV in 5 FS, NNPDF31, scale:  $H_T = E_T(lv) + pT(b1) + pT(b2)$
- Phasespace definition to model [CMS, 1608.07561]:  
 $pT(l) \geq 30 \text{ GeV } |y(l)| < 2.1 \text{ } pT(j) \geq 25 \text{ GeV, } |y(j)| < 2.4$
- Inclusive (at least 2 b-jets) and exclusive (exactly 2 b-jets, no other jets) jet phase spaces  
 (defined by the flavour-kT jet algorithm [Banfi'06])

- Inclusive :  
 ~ +20% corrections  
 ~ 7% scale dependence
- Exclusive:  
 ~ + 6% corrections  
 ~ 2.5% scale dependence (7-pt)  
 Compare decorrelated model: [Steward'12]  
 ~ 11% scale dependence

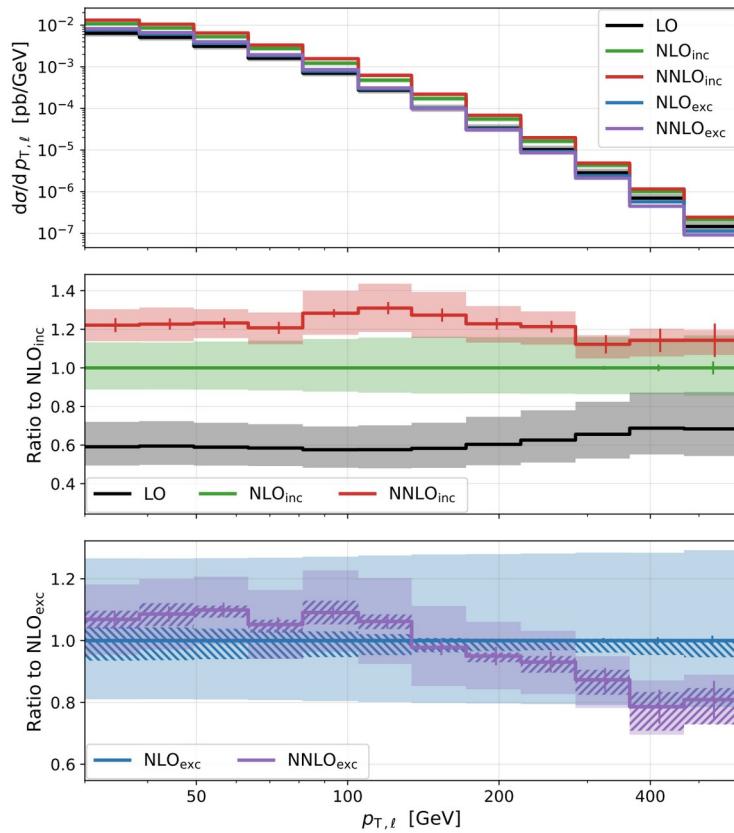
	inclusive [fb]	$\mathcal{K}_{\text{inc}}$	exclusive [fb]	$\mathcal{K}_{\text{exc}}$
$\sigma_{\text{LO}}$	$213.2(1)^{+21.4\%}_{-16.1\%}$	-	$213.2(1)^{+21.4\%}_{-16.1\%}$	-
$\sigma_{\text{NLO}}$	$362.0(6)^{+13.7\%}_{-11.4\%}$	1.7	$249.8(4)^{+3.9(+27)\%}_{-6.0(-19)\%}$	1.17
$\sigma_{\text{NNLO}}$	$445(5)^{+6.7\%}_{-7.0\%}$	1.23	$267(3)^{+1.8(+11)\%}_{-2.5(-11)\%}$	1.067

$$\sigma_{Wb\bar{b},\text{excl.}} = \sigma_{Wb\bar{b},\text{incl.}} - \sigma_{Wb\bar{b}j,\text{incl.}}$$

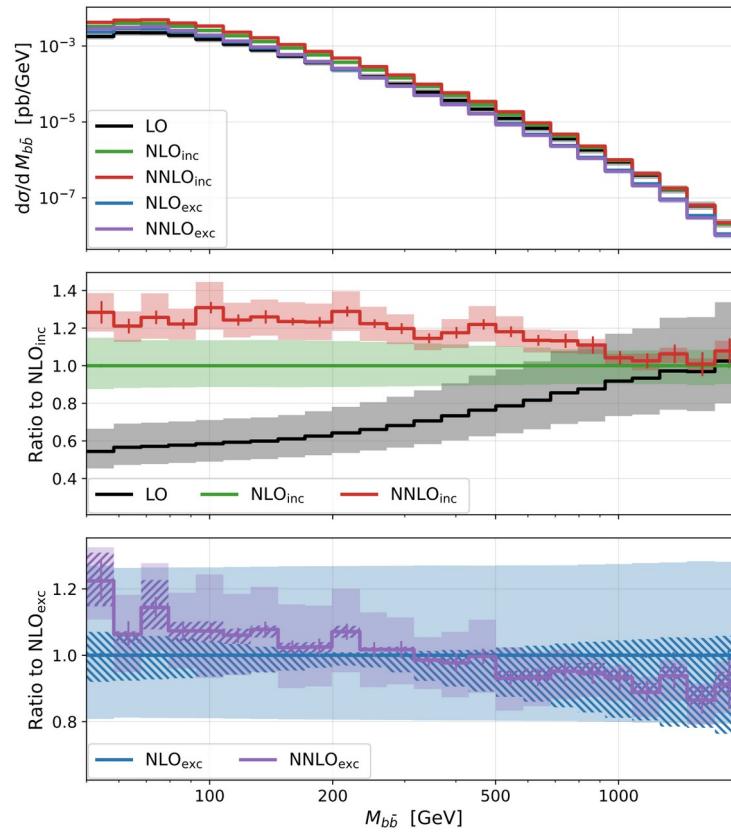
$$\Delta\sigma_{Wb\bar{b},\text{excl.}} = \sqrt{(\Delta\sigma_{Wb\bar{b},\text{incl.}})^2 + (\Delta\sigma_{Wb\bar{b}j,\text{incl.}})^2}$$

# Differential cross sections

Transverse momentum of lepton



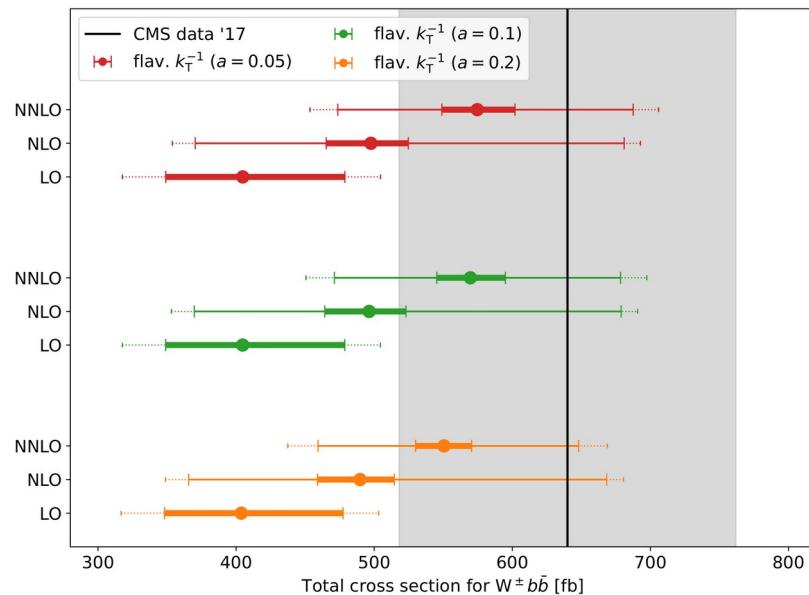
Invariant mass b-jet pair



# $W+2\text{ b jets}$ : flavour anti- $k_T$

Flavour anti- $k_T$  algorithm applied to  $Wbb$  production at the LHC

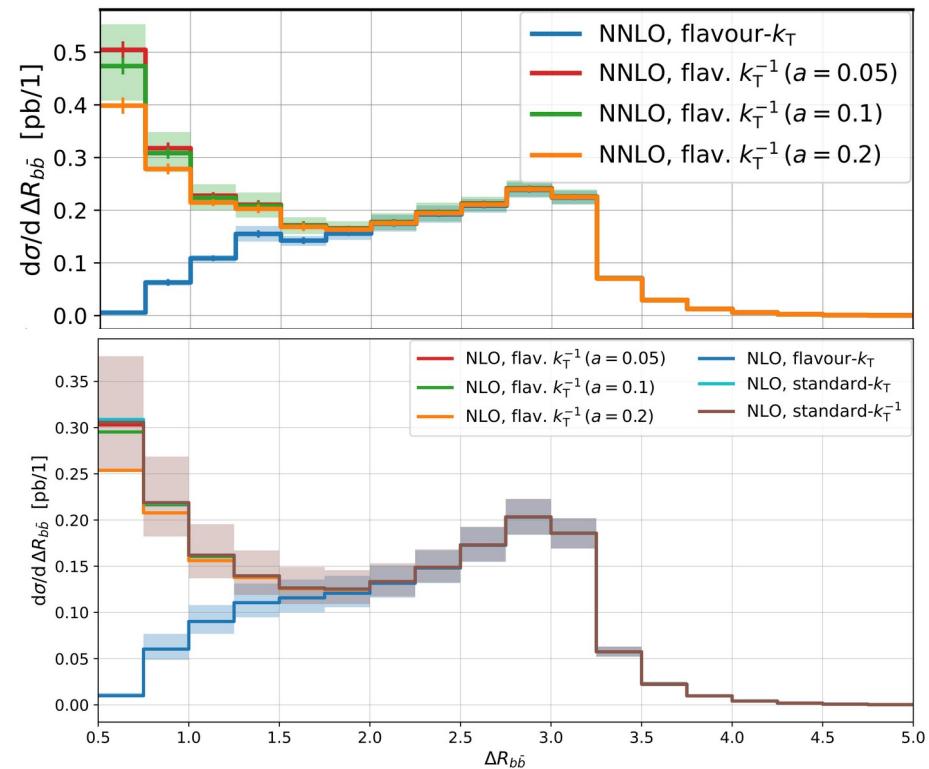
Hartanto, Poncelet, Popescu, Zoaia 2209.03280



Comparison to data

Measurement of the production cross section of a  $W$  boson in association with two  $b$  jets in  $pp$  collisions at  $\sqrt{s} = 8 \text{ TeV}$ , CMS 1608.07561

(assumes small unfolding corrections → wip)



Significant differences between  $k_T$  and anti- $k_T$   
In small  $\Delta R(b\bar{b})$  region? Beam-function?!

# Computation in 4FS

Associated production of a W boson and massive bottom  
quarks at next-to-next-to-leading order in QCD,  
Buonocore, Devoto, Kallweit, Mazzitelli, Rottoli, Savoini, 2212.04954

Credit: Luca Buonocore  
RadCor23

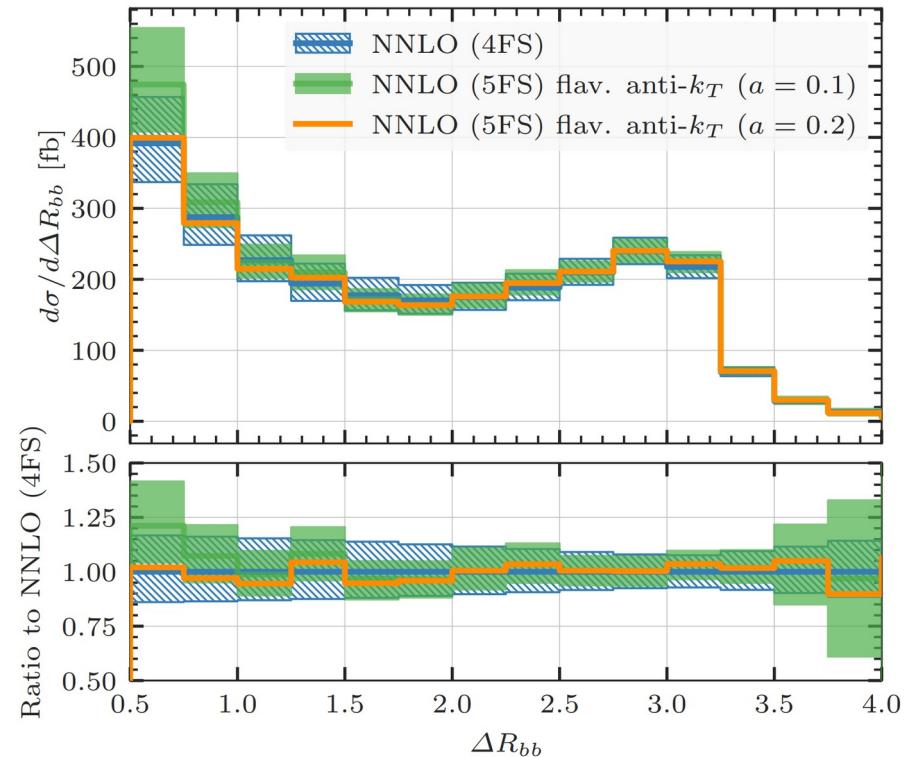
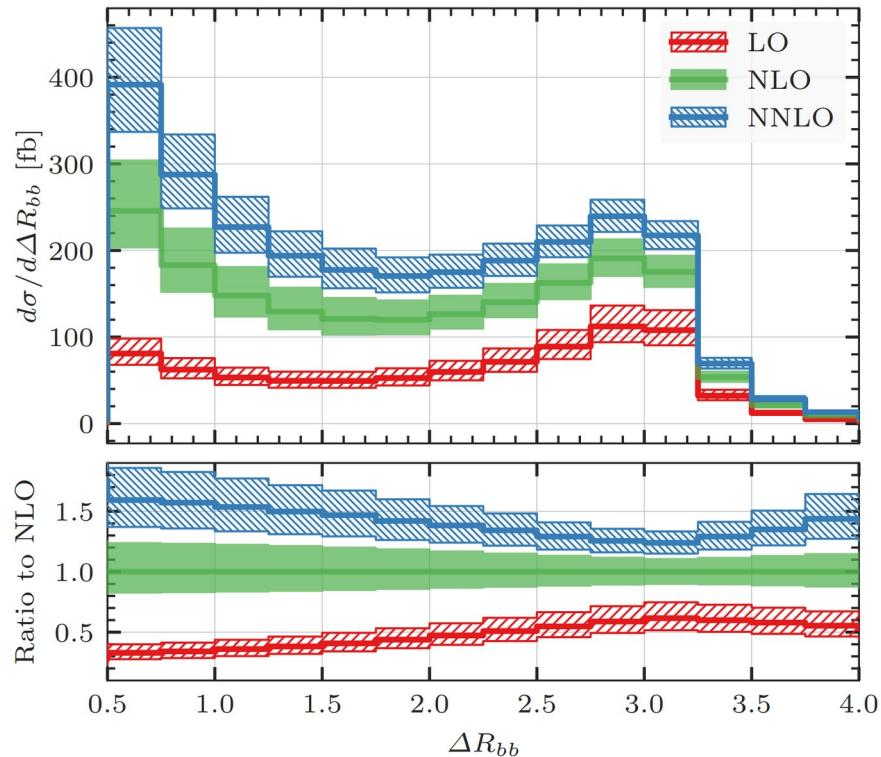
	2209.03280	2212.04954
$\alpha_s$ and PDF scheme	5FS	4FS
Jet clustering algorithm	flavour $k_T$ and flavour anti- $k_T$ algorithm ( $R=0.5$ )	$k_T$ and anti- $k_T$ algorithm ( $R=0.5$ )
pdf sets	NNPDF31_as_0118 (LO, NLO, NNLO)	NNPDF30_as_0118_nf_4 (LO) NNPDF31_as_0118_nf_4 (NLO, NNLO)

Simplification of massive 2-loop amplitude (Massification) [Mitov, Moch '07]:

$$|\mathcal{M}^{[p],(m)}\rangle = \prod_i \left[ Z_{[i]} \left( \frac{m^2}{\mu^2}, \alpha_s(\mu^2), \epsilon \right) \right]^{1/2} \times |\mathcal{M}^{[p]}\rangle + \mathcal{O}\left(\frac{m^2}{Q^2}\right)$$

# Comparison 4FS(+PS) vs 5FS

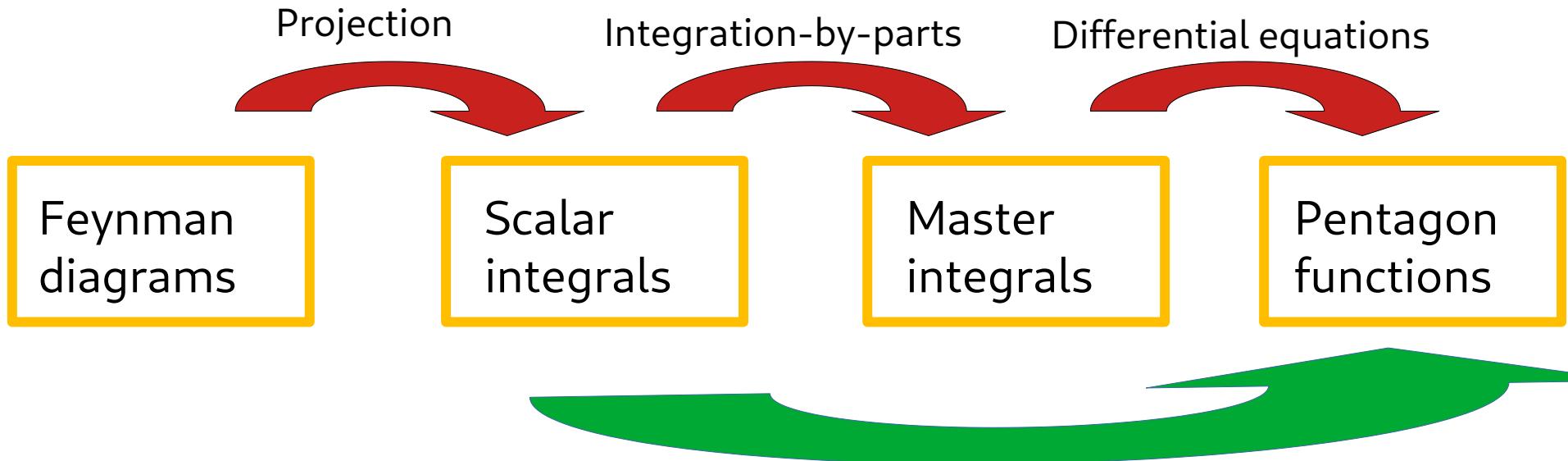
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# Overview

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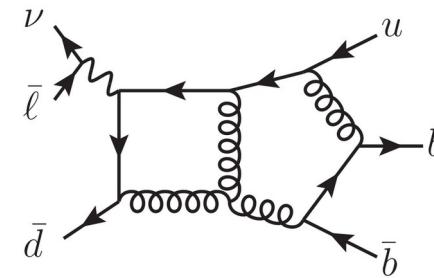
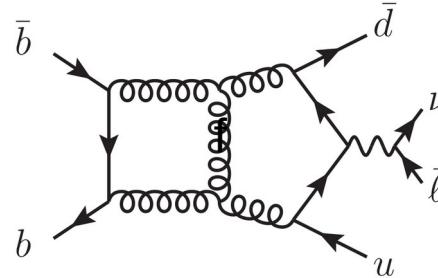
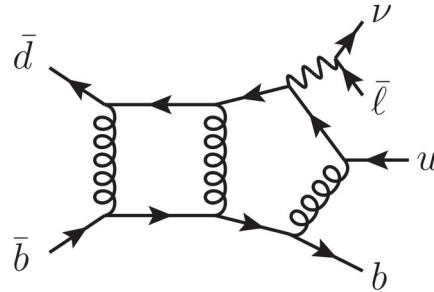
Old school approach:



Automated framework using finite fields  
to avoid expression swell based on  
FiniteFlow [Peraro'19]

# Projection to scalar integrals

Generate diagrams (contributing to leading-colour) with QGRAF



Factorizing decay:  $A_6^{(L)} = A_5^{(L)\mu} D_\mu P$        $M_6^{2(L)} = \sum_{\text{spin}} A_6^{(0)*} A_6^{(L)} = M^{(L)\mu\nu} D_{\mu\nu} |P|^2$

Projection on scalar functions (FORM+Mathematica):  
→ anti-commuting  $\gamma_5$  + Larin prescription

$$M_5^{(L)} = \sum_{i=1}^{16} a_i^{(L)} v_i^{\mu\nu}$$



$$a_i^{(L)} = a_i^{(L),\text{even}} + \text{tr}_5 a_i^{(L),\text{odd}}$$

$$a_i^{(L),p} = \sum_i c_{j,i}(\{p\}, \epsilon) \mathcal{I}(\{p\}, \epsilon)$$

# Integration-By-Parts reduction

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$$a_i^{(L),p} = \sum_i c_{j,i}(\{p\}, \epsilon) \mathcal{I}(\{p\}, \epsilon)$$

Prohibitively large number of integrals

$$\mathcal{I}_i(\{p\}, \epsilon) \equiv \mathcal{I}(\vec{n}_i, \{p\}, \epsilon) = \int \frac{d^d k_1}{(2\pi)^d} \frac{d^d k_2}{(2\pi)^d} \prod_{k=1}^{11} D_k^{-n_{i,k}}(\{p\}, \{k\})$$

Integration-By-Parts identities connect different integrals  $\rightarrow$  system of equations  
 $\rightarrow$  only a small number of independent “master” integrals

$$0 = \int \frac{d^d k_1}{(2\pi)^d} \frac{d^d k_2}{(2\pi)^d} l_\mu \frac{\partial}{\partial l^\mu} \prod_{k=1}^{11} D_k^{-n_{i,k}}(\{p\}, \{k\}) \quad \text{with} \quad l \in \{p\} \cap \{k\}$$

LiteRed (+ Finite Fields)



$$a_i^{(L),p} = \sum_i d_{j,i}(\{p\}, \epsilon) \text{MI}(\{p\}, \epsilon)$$

# Master integrals & finite remainder

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Differential Equations:  $d\vec{\text{MI}} = dA(\{p\}, \epsilon)\vec{\text{MI}}$

[Remiddi, 97]

[Gehrmann, Remiddi, 99]

[Henn, 13]

Canonical basis:  $d\vec{\text{MI}} = \epsilon d\tilde{A}(\{p\})\vec{\text{MI}}$

Simple iterative solution



$$\text{MI}_i = \sum_w \epsilon^w \tilde{\text{MI}}_i^w \quad \text{with} \quad \tilde{\text{MI}}_i^w = \sum_j c_{i,j} m_j$$

Chen-iterated integrals

"Pentagon"-functions

[Chicherin, Sotnikov, 20]

[Chicherin, Sotnikov, Zoia, 21]

Putting everything together (and removing of IR poles):

$$f_i^{(L),p} = a_i^{(L),p} - \text{poles}$$

$$f_i^{(L),p} = \sum_j c_{i,j}(\{p\}) m_j + \mathcal{O}(\epsilon)$$