

1. Chung, Garey, Tarjan (Strongly connected orientations of mixed multigraph)

connectivity: in an undirected graph is that every vertex can reach every other vertex via any path.

strong connectivity applies only to directed graphs.

strongly connected - directed graph, if there is path b/w every pair of vertices.

Orientation: assigning directions to edges in the undirected graph.

multigraph: graph with parallel edges or loops

mixed graph: some edges might be directed and undirected.

Robbin's work: 1. Orienting all the undirected edges of a mixed multigraph (partially oriented with loops or parallel edges in graph) preserving reachability or strong connectivity. (undirected graph is orientable iff it is strongly connected and has no

bridges.)

2. proof yields a linear-time algorithm for constructing a strongly connected orientation. his algorithm carry out:

a) DFS

b)orient every edge in the direction along which the search advances.

Boesch and Tindell: claimed that DFS can be used to find an appropriate orientation but provides no details.

Note:Results of above papers say nothing about how much distances between the vertices can increase in the process of orienting edges while preserving strong connectivity.

Chvatal and Thomassen: addresses above note in only undirected graph.

The oriented diameter of an (undirected) graph G is the smallest diameter among strong orientations of G . and is between $5d^2 + 5d$ and $2d^2 + 2d$ or at-most $r^2 + r$

This paper work: linear time algorithm of robbin's algo. and also improved chvatal and Thomassen' algo to atmost $4r^2 + 4r$

Note: these algos gives poly-time solvable.

Notations used:

undirected edges - $\{\}$

directed edges - $[]$

either directed or undirected - $()$

2.Chavatal and Thomassen (Distances in Orientations of Graphs)