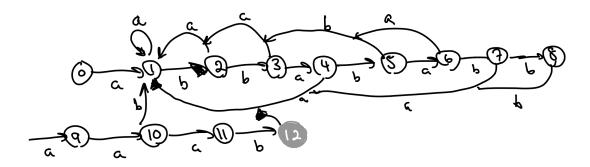
## CS 457, Data Structures and Algorithms I Fourth Problem Set

## November 22, 2016

## Due on December 2. Collaboration is not allowed. Contact me directly with any questions.

- - a) Construct the string matching automaton for P, and illustrate its operation on T.



b) Compute the prefix function  $\pi$  for P, and illustrate the operation of the KMP algorithm on T.

i 1 2 3 4 5 6 7 8 9 10 11 12 
$$P[i]$$
 a b b a b a b b a a a b  $\pi$  0 0 0 1 2 1 0 3 4 1 1 2

Given T = aaababaabaabaabaababbaabbaaabbabab

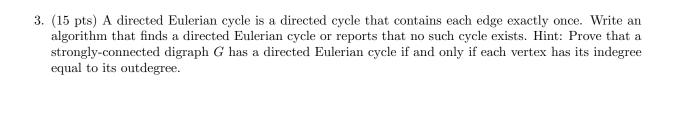
The algorithm then checks if the prefix and suffix are the same. Since they aren't a match, it will continue to do so until it reaches a comparison where it doesn't match and the prefix function is greater than 0. It will use the non-matching string as a pivot point where the character after the prefix is compared. If they are valid, it continues to do so until it either reaches a non match, in which it starts its comparison over again from that point or finds the match seen below.

(There aren't 2 b's until it actually reaches the string, thus the string matching isn't used until then, which in this case it reaches the match)

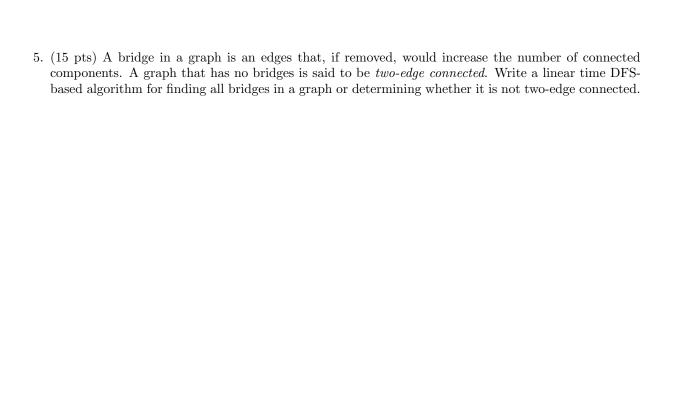
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2. (15 pts) Write an algorithm that reads characters one at a time and reports at each instant if the

current string is a palindrome. Hint: Use the Rabin-Karp hashing idea.



4. (15 pts) Given a DAG and two vertices v and w, find a shortest ancestral path between v and w. An ancestral path between v and w is a common ancestor x along with a shortest directed path from v to x and a shortest directed path from w to x. A shortest ancestral path in the ancestral path whose total length is minimized. Warmup: Find a DAG where the shortest ancestral path goes to a common ancestor x that is not LCA.



6. (15 pts) Given a connected edge-weighted graph G and a specified set of edges S that contains no cycles, provide an algorithm that finds a minimum-weight spanning tree among all the spanning trees that contain all the edges in S. Also, provide an upper bound on the running time of your algorithm, and prove its correctness.

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7. (15 pts) Design an algorithm that, given two strings, determines whether one is a cyclic rotation of the other (e.g., "example" and "leexamp").