

# Problem Set 2: Fastest way to get around

## Introduction

In this problem set you will solve a simple optimization problem on a graph. Specifically, you will find the shortest route from one building to another on the map given that you wish to constraint the amount of time you spend walking outdoors.

## Getting Started

Download ProblemSet2.zip from IVY

Please do not rename the files, change any of the provided helper functions, change function/method names. You will need to keep ps2.py, graph.py and map.txt in the same folder.

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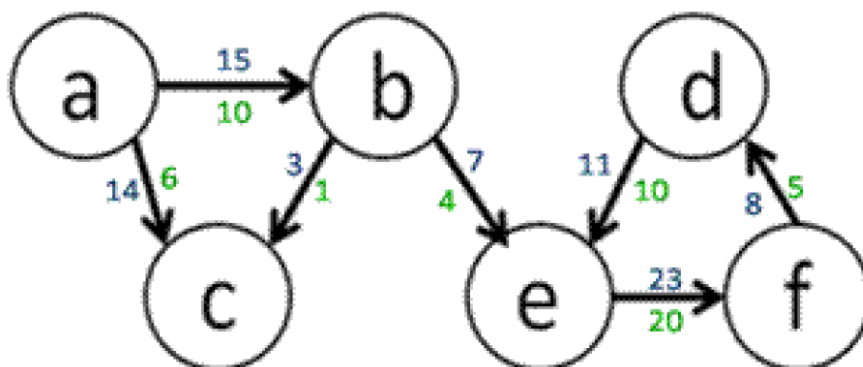
From the text input file, map.txt, you will build a representation of this map in Python using the graph-related data structure that is provided. Each line in map.txt has 4 pieces of data in it in the following order separated by a single space (space-delimited): the start building, the destination building, the distance in meters between the two buildings that are not sheltered. For example, suppose the map text file contained the following line:

10 32 200 40

This means that the map contains an edge from building 10 (start location) to building 32 (end location) that is 200 meters long, where 40 of those 200 meters are spent unsheltered. **During the day, routes are crowded and only allow for you to travel in one direction.**

## Problem 1: Creating the Data Structure Representation [6 Marks]

In this problem set, we are dealing with edges that have different weights. In the figure below, the blue numbers show the cost of traversing an edge in terms of total distance traveled, while the green numbers show the cost of traversing an edge in terms of distance spent unsheltered. Note that the distance spent unsheltered for a single edge is always less than or equal to the total distance it takes to traverse that edge. Now the cost of going from “a” to “b” to “e” is a total distance traveled of 22 meters, where 14 of those meters are spent unsheltered.



In graph.py, you will find the Node, and Edge classes, which do not store information about weights associated with each edge. You will also find skeletons of the WeightedEdge and Digraph classes, which we will use in the rest of this problem set. **Complete the WeightedEdge and Digraph classes** such that the unit tests at the bottom of graph.py pass. Your WeightedEdge class will need to implement the \_\_str\_\_ method (which is called when we use str() on a WeightedEdge object) as follows:

Suppose we have a `WeightedEdge` object `e` containing by the following information:

- source node name: 'a'
- destination node name: 'b'
- total distance along the edge: 15
- unsheltered distance along the edge: 10

Then `str(e)` with the above information should yield:

```
a -> b (15,10)
```

For `Digraph`, you will need to implement the `add_node` and `add_edge` methods.

## Problem 2: Building up the map

For this problem, you will be implementing the `load_map(map_filename)` function in `ps2.py`, which reads in data from a file and builds a directed graph to properly represent the map according to the data. Think about how you plan on representing your graph before implementing `load_map`.

### Problem 2a: Designing your graph [3 Marks]

Decide how the map problem can be modeled as a graph. Write a description of your design approach as a comment under the Problem #2 heading in `ps2.py`. What do the graph's nodes represent in this problem? What do the graph's edges represent in this problem? Where are the distances represented?

```
# Problem 2: Building up the Map
#
# Problem 2a: Designing your graph
#
# What do the graph's nodes represent in this problem? What
# do the graph's edges represent? Where are the distances
# represented?
#
# Answer:
#
```

### Problem 2b: Implementing `load_map` [6 Marks]

### Problem 2c: Testing `load_map` [5 Marks]

Test whether your implementation of `load_map` is correct by creating a text file, `test_load_map.txt`, using the same format as ours, loading your txt file using your `load_map` function, and checking to see if your directed graph has the nodes and edges it should. You can add your call to `load_map` directly below where `load_map` is defined, and comment out the line when you are done testing (It may also help to comment out the `__main__` code block to clean up your output while testing this function). Your test case should have at least 3 nodes and 3 edges. For example, if you had Nodes "a", "b", and "c" and edges `WeightedEdge(a,b,10,9)`, `WeightedEdge(a,c,12,2)`, and `WeightedEdge(b,c,1,1)`, if you were to print out your graph, you would see something like:

```
Loading map from file...
```

```
a->b (10,0)
```

```
a->c (12,2)
```

```
b->c (1,1)
```

Submit `test_load_map.txt`. Also, include the lines used to test `load_map` at the location specified in `ps2.py`, but comment them out.

### Problem 3: Find the Shortest Path using Optimized Depth First Search

We can define a valid path from a given start to end node in a graph as an ordered sequence of nodes  $[n_1, n_2, \dots, n_k]$ , where  $n_1$  to  $n_k$  are existing nodes in the graph and there is an edge from  $n_i$  to  $n_{i+1}$  for  $i = 1$  to  $k - 1$ . In Figure 2, each edge is unweighted, so you can assume that each edge has distance 1, and then the total distance traveled on the path is 4.

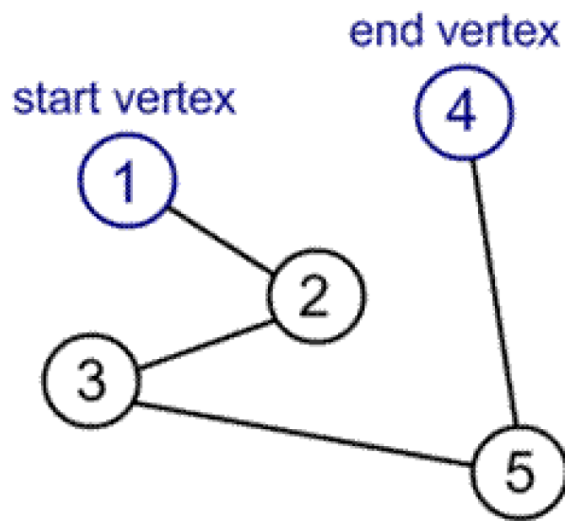


Figure 2. Example of a path from start to end node.

In our map problem, the total distance traveled on a path is equal to the sum of all total distances traveled between adjacent nodes on this path. Similarly, the distance spent unsheltered on the path is equal to the sum of all distances spent unsheltered on the edges in the path.

Depending on the number of nodes and edges in a graph, there can be multiple valid paths from one node to another, which may consist of varying distances. We define the shortest path between two nodes to be the path with the least total distance traveled. You are trying to minimize the distance traveled while not exceeding the maximum distance unsheltered.

How do we find a path in the graph? Work off the depth-first traversal algorithm covered in lesson to discover each of the nodes and their children nodes to build up possible paths. Note that you will have to adapt the algorithm to fit this problem.

#### Problem 3a: Objective function [2 Marks]

Write a sentence describing what is the objective function for this problem.

```
# Problem 3: Finding the Shorest Path using Optimized Search Method
#
# Problem 3a: Objective function
#
# What is the objective function for this problem? What are the constraints?
#
# Answer:
#
```

#### Problem 3b: Implement `get_best_path` [6 Marks]

Implement the helper function `get_best_path`. Assume that any variables you need have been set correctly in `directed_dfs`. Below is some pseudocode to help get you started.

```
if start and end are not valid nodes:
    raise an error
elif start and end are the same node:
    update the global variables appropriately
```

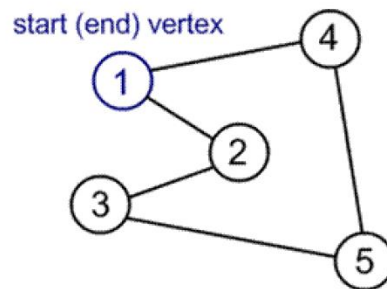
```

else:
    for all the child nodes of start
        construct a path including the node
        recursively solve the rest of the path, from the child node to
the end node
return the shortest path

```

#### Notes:

- Graphs can contain cycles. A cycle occurs in a graph if the path of nodes leads you back to a node that was already visited in the path. When building up possible paths, if you reach a cycle without knowing it, you could get stuck indefinitely by extending the path with the same nodes that have already been added to the path.



- If you come across a path that is longer than your shortest path found so far, then you know that this longer path cannot be your solution, so there is no point in continuing to traverse its children and discover all paths that contain this sub-path. You must include this optimization in your solution in order to receive full credit.

### Problem 3c: Implement directed\_dfs [6 Marks]

Implement the function

`directed_dfs(digraph, start, end, max_total_dist, max_dist_unsheltered)` that uses this optimized depth first search to find the shortest path in a directed graph from start node to end node under the following constraints: the total distance travelled is less than or equal to `max_total_dist`, and the total distance spent unsheltered is less than or equal to `max_dist_unsheltered`. If multiple paths are still found, then return any one of them. If no path can be found to satisfy these constraints, then raise a `ValueError` exception.

All you are doing in this function is initializing variables, calling your recursive function, and returning the appropriate path. Do not write too much code. Test your code by uncommenting the code at the bottom of `ps2.py`.