# Package 'jfa'

June 29, 2021

Title Bayesian and Classical Audit Sampling

Version 0.5.5

Date 2021-06-29
<b>Description</b> Implements the audit sampling workflow as discussed in Derks et al. (2019) <doi:10.31234 9f6ub="" osf.io="">. The package makes it easy for an auditor to plan a statistical sample, select the sample from the population, and evaluate the sample using various methods according to the International Standards on Auditing. Furthermore, the package implements Bayesian equivalents of these methods.</doi:10.31234>
BugReports https://github.com/koenderks/jfa/issues
<pre>URL https://koenderks.github.io/jfa/,https://github.com/koenderks/jfa</pre>
Imports graphics, stats
Suggests kableExtra, knitr, MUS, rmarkdown, testthat
Language en-US
License GPL-3
Encoding UTF-8
LazyData true
RoxygenNote 7.1.1
VignetteBuilder knitr
R topics documented:
auditBF
auditPrior
BuildIt
jfa-methods
planning
report
selection
Index 20

2 auditBF

auditBF	Function to compute Bayes factors for audit sampling	

# Description

This function computes Bayes factors for audit sampling from summary statistics of an audit sample. By default, the Bayes factor is computed using an impartial prior distribution on the misstatement (Derks et al. 2021b). However, the arguments nPrior and kPrior can be used to specify an alternative prior distribution (Derks et al. 2021a).

For more details on how to use this function, see the package vignette: vignette('jfa',package = 'jfa')

# Usage

```
\label{eq:auditBF} \mbox{ (materiality, n, k, expectedError = 0, likelihood = 'binomial', nPrior = NULL, kPrior = NULL, N = NULL, log = FALSE)
```

# Arguments

materiality	a numeric value between 0 and 1 specifying the performance materiality (i.e., the maximum upper limit) as a fraction of the total population size. Can be NULL for some methods.
n	an integer larger than 0 specifying the number of items in the sample.
k	a number larger than zero specifying the observed proportional error (i.e., sum of taints) in the sample.
expectedError	a numeric value between 0 and 1 specifying the expected errors in the sample relative to the total sample size, or a numeric value (>= 1) that represents the sum of expected errors in the sample. It is advised to set this value conservatively to minimize the probability of the observed errors exceeding the expected errors, which would imply that insufficient work has been done in the end.
likelihood	a character specifying the likelihood assumed when updating the prior distribution. This can be either binomial for the binomial likelihood and beta prior distribution, poisson for the Poisson likelihood and gamma prior distribution, or hypergeometric for the hypergeometric likelihood and beta-binomial prior distribution. See the details section for more information about the available likelihoods.
nPrior	numeric value larger than, or equal to, 0 specifying the sample size of the sample equivalent to the prior information.
kPrior	a numeric value larger than, or equal to, $0$ specifying the sum of errors in the sample equivalent to the prior information.
N	an integer larger than $0$ specifying the total population size. Only required when likelihood = 'hypergeometric'.
log	logical; if TRUE, the Bayes factor is given as log(bf).

auditBF 3

#### **Details**

The Bayes Factor  $BF_{-+}$  quantifies how much more likely the data are to be observed under  $H_-$ :  $\theta < \theta_{max}$  than under  $H_+$ :  $\theta > \theta_{max}$ . Therefore,  $BF_{-+}$  can be interpreted as the relative support in the observed data for  $H_-$  versus  $H_+$ . If  $BF_{-+}$  is 1, there is no preference for either  $H_-$  or  $H_+$ . If  $BF_{-+}$  is larger than 1,  $H_-$  is preferred. If  $BF_{-+}$  is between 0 and 1,  $H_+$  is preferred.

This section elaborates on the available likelihoods and corresponding prior distributions for the likelihood argument.

• binomial: The binomial likelihood is often used as a likelihood for attributes sampling *with* replacement. The likelihood function is defined as:

$$p(x) = \binom{n}{k} p^k (1-p)^{n-k}$$

The conjugate  $beta(\alpha, \beta)$  prior has probability density function:

$$f(x; \alpha, \beta) = \frac{1}{B(\alpha, \beta)} x^{\alpha - 1} (1 - x)^{\beta - 1}$$

• poisson: The Poisson likelihood is often used as a likelihood for monetary unit sampling (MUS). The likelihood function is defined as:

$$p(x) = \frac{\lambda^x e^{-\lambda}}{x!}$$

The conjugate  $gamma(\alpha, \beta)$  prior has probability density function:

$$f(x; \alpha, \beta) = \frac{\beta^{\alpha} x^{\alpha - 1} e^{-\beta x}}{\Gamma(\alpha)}$$

• hypergeometric: The hypergeometric likelihood is used as a likelihood for sampling *without* replacement. The likelihood function is defined as:

$$p(x=k) = \frac{\binom{K}{k} \binom{N-K}{n-k}}{\binom{N}{n}}$$

The conjugate beta-binomial $(\alpha, \beta)$  prior (Dyer and Pierce, 1993) has probability density function:

$$f(k|n, \alpha, \beta) = \binom{n}{k} \frac{B(k+\alpha, n-k+\beta)}{B(\alpha, \beta)}$$

#### Value

A value for the Bayes factor in favor of the hypothesis of tolerable misstatement against the hypothesis of intolerable misstatement.

#### Author(s)

Koen Derks, <k.derks@nyenrode.nl>

#### References

Derks, K., de Swart, J., van Batenburg, P. Wagenmakers, E.-J., & Wetzels, R. (2021a). Priors in a Bayesian audit: How integrating information into the prior distribution can improve audit transparency and efficiency. In Press.

Derks, K., de Swart, J., Wagenmakers, E.-J., & Wetzels, R. (2021b). A default Bayesian hypothesis test for audit sampling.

4 auditPrior

#### See Also

auditPrior planning selection evaluation report

#### **Examples**

```
# Compute a default Bayes factor from an impartial prior
auditBF(materiality = 0.05, n = 50, k = 1)
# Compute a Bayes factor from a negligible prior
auditBF(materiality = 0.05, n = 50, k = 1, nPrior = 0, kPrior = 0)
```

auditPrior

Create a prior distribution for audit sampling

#### **Description**

This function creates a prior distribution with audit information to be used in the planning() and evaluation() functions via their prior argument. The function returns an object of class jfaPrior which can be used with associated summary() and plot() methods.

For more details on how to use this function, see the package vignette: vignette('jfa',package = 'jfa')

#### Usage

# Arguments

method a character specifying the method by which the prior distribution is constructed.

Defaults to none which incorporates no existing information. Other options are arm, bram, median, hypotheses, sample, and factor. See the details section

for more information about the available methods.

likelihood a character specifying the likelihood assumed when updating the prior distribu-

tion. This can be either binomial for the binomial likelihood and beta prior distribution, poisson for the Poisson likelihood and gamma prior distribution, or hypergeometric for the hypergeometric likelihood and beta-binomial prior distribution. See the details section for more information about the available

likelihoods.

expectedError a numeric value between 0 and 1 specifying the expected errors in the sample

relative to the total sample size, or a numeric value (>= 1) that represents the sum of expected errors in the sample. It is advised to set this value conservatively to minimize the probability of the observed errors exceeding the expected errors,

which would imply that insufficient work has been done in the end.

confidence a numeric value between 0 and 1 specifying the confidence level to be used in

the planning. Defaults to 0.95 for 95% confidence.

auditPrior 5

materiality	a numeric value between 0 and 1 specifying the performance materiality (i.e., the maximum upper limit) as a fraction of the total population size. Can be NULL for some methods.
N	an numeric value larger than 0 specifying the total population size. Optional unless likelihood = 'hypergeometric'.
ir	if method = 'arm', a numeric value between 0 and 1 specifying the inherent risk in the audit risk model. Defaults to 1 for $100\%$ risk.
cr	if method = 'arm', a numeric value between 0 and 1 specifying the internal control risk in the audit risk model. Defaults to 1 for 100% risk.
ub	if method = 'bram', a numeric value between 0 and 1 specifying the upper bound for the prior distribution as a fraction of the population size.
pHmin	if method = 'hypotheses', a numeric value between 0 and 1 specifying the prior probability of the hypothesis $\theta <$ materiality.
pHplus	if method = 'hypotheses', a numeric value between 0 and 1 specifying the prior probability of the hypothesis $\theta >$ materiality.
sampleN	if method = 'sample' or method = 'factor', an integer larger than, or equal to, 0 specifying the sample size of the sample equivalent to the prior information.
sampleK	if sample or factor, a numeric value larger than, or equal to, 0 specifying the sum of errors in the sample equivalent to the prior information.
factor	if method = 'factor', a numeric value between 0 and 1 specifying the weighting factor for the results of the sample equivalent to the prior information.

#### **Details**

This section elaborates on the available options for the method argument.

- none: This method constructs a prior distribution that incorporates negligible information about the possible values of the misstatement.
- arm: This method constructs a prior distribution by translating the risks of material misstatement (inherent risk and internal control risk) from the audit risk model to an implicit sample.
   The method requires specification of the ir (inherent risk) and cr (internal control risk) arguments.
- bram: This method constructs a prior distribution using the Bayesian audit risk assessment model (BRAM) in which the expected most likely error and expected upper bound of the misstatement must be specified. The method requires specification of the ub argument.
- median: This method constructs a prior distribution so that the prior probability of tolerable misstatement ( $\theta$  < materiality) is equal to the prior probability of intolerable misstatement ( $\theta$  > materiality).
- hypotheses: This method constructs a prior distribution with custom prior probabilities for the hypotheses of tolerable misstatement ( $\theta <$  materiality) and intolerable misstatement ( $\theta >$  materiality). This method requires specification of the pHmin and pHplus arguments.
- sample: This method constructs a prior distribution on the basis of an earlier sample. This method requires specification of the sampleN and sampleK arguments.
- factor: This method constructs a prior distribution on the basis of an earlier sample in combination with a weighting factor. This method requires specification of the sampleN, sampleK, and factor arguments.

This section elaborates on the available likelihoods and corresponding prior distributions for the likelihood argument.

6 auditPrior

• binomial: The binomial likelihood is often used as a likelihood for attributes sampling *with* replacement. The likelihood function is defined as:

$$p(x) = \binom{n}{k} p^k (1-p)^{n-k}$$

The conjugate  $beta(\alpha, \beta)$  prior has probability density function:

$$f(x; \alpha, \beta) = \frac{1}{B(\alpha, \beta)} x^{\alpha - 1} (1 - x)^{\beta - 1}$$

• poisson: The Poisson likelihood is often used as a likelihood for monetary unit sampling (MUS). The likelihood function is defined as:

$$p(x) = \frac{\lambda^x e^{-\lambda}}{x!}$$

The conjugate  $gamma(\alpha, \beta)$  prior has probability density function:

$$f(x; \alpha, \beta) = \frac{\beta^{\alpha} x^{\alpha - 1} e^{-\beta x}}{\Gamma(\alpha)}$$

• hypergeometric: The hypergeometric likelihood is used as a likelihood for sampling *without* replacement. The likelihood function is defined as:

$$p(x=k) = \frac{\binom{K}{k} \binom{N-K}{n-k}}{\binom{N}{n}}$$

The conjugate beta-binomial( $\alpha, \beta$ ) prior (Dyer and Pierce, 1993) has probability density function:

$$f(k|n,\alpha,\beta) = \binom{n}{k} \frac{B(k+\alpha,n-k+\beta)}{B(\alpha,\beta)}$$

#### Value

An object of class jfaPrior containing:

confidence a numeric value between 0 and 1 indicating the confidence level used. if materiality is specified, a numeric value between 0 and 1 indicating the materiality materiality used to construct the prior distribution. a numeric value larger than, or equal to, 0 indicating the input for the number of expectedError expected errors. method a character indicating the method by which the prior distribution is constructed. likelihood a character indicating the assumed likelihood. if N is specified, an integer larger than 0 indicating the population size. a list containing a description of the prior distribution, including the parameters description of the prior distribution and the implicit sample on which the prior distribution is based. a list containing statistics of the prior distribution, including the mean, mode, statistics median, and upper bound of the prior distribution. a list containing specifics of the prior distribution that vary depending on the specifics

hypotheses if materiality is specified, a list containing information about the hypotheses, including prior probabilities and odds for the hypothesis of tolerable misstatement (H-) and the hypothesis of intolerable misstatement (H+).

BuildIt 7

#### Author(s)

Koen Derks, <k.derks@nyenrode.nl>

#### References

Derks, K., de Swart, J., Wagenmakers, E.-J., Wille, J., & Wetzels, R. (2019). JASP for audit: Bayesian tools for the auditing practice.

Derks, K., de Swart, J., van Batenburg, P. Wagenmakers, E.-J., & Wetzels, R. (2021). Priors in a Bayesian audit: How integrating information into the prior distribution can improve audit transparency and efficiency. In Press.

#### See Also

planning selection evaluation report auditBF

#### **Examples**

```
# Translate inherent risk (ir) and control risk (cr) to a prior distribution auditPrior(method = 'arm', likelihood = 'binomial', expectedError = 0.025, materiality = 0.05, ir = 1, cr = 0.6)
```

BuildIt

BuildIt Construction financial statements

# Description

Fictional data from a construction company in the United States, containing 3500 observations identification numbers, book values, and audit values. The audit values are added for illustrative purposes, as these would need to be assessed by the auditor in the execution stage of the audit.

# Usage

data(BuildIt)

#### **Format**

A data frame with 3500 rows and 3 variables.

**ID** unique record identification number.

book Value book value in US dollars (\$14.47–\$2,224.40).

auditValue true value in US dollars (\$14.47-\$2,224.40).

#### References

Derks, K., de Swart, J., Wagenmakers, E.-J., Wille, J., & Wetzels, R. (2019). JASP for audit: Bayesian tools for the auditing practice.

```
data(BuildIt)
```

-		
eval	uation	

Evaluate a statistical audit sample

# Description

This function takes a data frame (using sample, bookValues, and auditValues) or summary statistics (using nSumstats and kSumstats) and performs inference on the misstatement in the sample. The function returns an object of class jfaEvaluation which can be used with associated summary() and plot() methods.

For more details on how to use this function, see the package vignette: vignette('jfa',package = 'jfa')

### Usage

### **Arguments**

•	3	
	materiality	a numeric value between 0 and 1 specifying the performance materiality (maximum tolerable error) as a fraction of the total size of the population. If specified, the function also returns the conclusion of the analysis with respect to the performance materiality. The value is discarded when direct, difference, quotient, or regression method is chosen.
	minPrecision	a numeric value between 0 and 1 specifying the required minimum precision (upper bound minus most likely error) as a fraction of the total size of the population. If specified, the function also returns the conclusion of the analysis with respect to the required minimum precision.
	method	a character specifying the method to be used in the evaluation. Possible options are poisson, binomial (default), hypergeometric, mpu, stringer, stringer-meikle, stringer-lta, stringer-pvz, rohrbach, moment, direct, difference, quotient, or regression. See the details section for more information.
	confidence	a numeric value between 0 and 1 specifying the confidence level used in the evaluation. Defaults to 0.95 for 95% confidence.
	sample	a data frame containing the sample to be evaluated. The sample must at least contain a column of book values and a column of audit (true) values.
	bookValues	a character specifying the column name for the book values in the sample.
	auditValues	a character specifying the column name for the audit values in the sample.
	counts	a integer vector specifying the number of times each item in the sample should be counted in the evaluation (due to it being selected multiple times for the

sample).

nSumstats an integer larger than 0 specifying the number of items in the sample. If spec-

ified, overrides the sample, bookValues and auditValues arguments and assumes that the data come from summary statistics specified by both nSumstats

and kSumstats.

kSumstats a numeric value larger than 0 specifying the sum of errors found in the sam-

ple. If specified, overrides the sample, bookValues and auditValues arguments and assumes that the data come from summary statistics specified by both

kSumstats and nSumstats.

N an integer larger than 0 specifying the total number of items in the population.

populationBookValue

if method is one of direct, difference, quotient, or regression, a numeric value specifying the total value of the items in the population. This argument is

optional otherwise.

prior a logical specifying if a prior distribution must be used, or an object of class

jfaPrior or jfaPosterior containing the prior distribution. Defaults to FALSE for frequentist planning. If TRUE, a negligible prior distribution is chosen by default, but can be adjusted using the 'kPrior' and 'nPrior' arguments. Chooses a conjugate gamma distribution for the Poisson likelihood, a conjugate beta distribution for the binomial likelihood, and a conjugate beta-binomial distribution

for the hypergeometric likelihood.

nPrior if prior = TRUE, a numeric value larger than, or equal to, 0 specifying the sample

size of the sample equivalent to the prior information.

kPrior if prior = TRUE, a numeric value larger than, or equal to, 0 specifying the sum

of errors in the sample equivalent to the prior information.

rohrbachDelta  $\,$  if method = 'rohrbach', a numeric value specifying  $\Delta$  in Rohrbach's aug-

mented variance bound (Rohrbach, 1993).

momentPoptype if method = 'moment', a character specifying the type of population (Dworin

and Grimlund, 1984). Possible options are accounts and inventory. This

argument affects the calculation of the central moments in the bound.

csA if method = "coxsnell", a numeric value specifying the  $\alpha$  parameter of the

prior distribution on the mean taint. Defaults to 1 as recommended by Cox and

Snell (1979).

csB if method = "coxsnell", a numeric value specifying the  $\beta$  parameter of the

prior distribution on the mean taint. Defaults to 3 as recommended by Cox and

Snell (1979).

csMu if method = "coxsnell", a numeric value between 0 and 1 specifying the mean

of the prior distribution on the mean taint. Defaults to 0.5 as recommended by

Cox and Snell (1979).

# **Details**

This section lists the available options for the methods argument.

- poisson: Evaluates the sample with the Poisson distribution. If combined with prior = TRUE, performs Bayesian evaluation using a *gamma* prior and posterior.
- binomial: Evaluates the sample with the binomial distribution. If combined with prior = TRUE, performs Bayesian evaluation using a *beta* prior and posterior.
- hypergeometric: Evaluates the sample with the hypergeometric distribution. If combined with prior = TRUE, performs Bayesian evaluation using a *beta-binomial* prior and posterior.

- mpu: Evaluates the sample with the mean-per-unit estimator.
- stringer: Evaluates the sample with the Stringer bound (Stringer, 1963).
- stringer-meikle: Evaluates the sample with the Stringer bound with Meikle's correction for understatements (Meikle, 1972).
- stringer-lta: Evaluates the sample with the Stringer bound with LTA correction for understatements (Leslie, Teitlebaum, and Anderson, 1979).
- stringer-pvz: Evaluates the sample with the Stringer bound with Pap and van Zuijlen's correction for understatements (Pap and van Zuijlen, 1996).
- rohrbach: Evaluates the sample with Rohrbach's augmented variance bound (Rohrbach, 1993).
- moment: Evaluates the sample with the modified moment bound (Dworin and Grimlund, 1984).
- coxsnell: Evaluates the sample with the Cox and Snell bound (Cox and Snell, 1979).
- direct: Evaluates the sample with the direct estimator (Touw and Hoogduin, 2011).
- difference: Evaluates the sample with the difference estimator (Touw and Hoogduin, 2011).
- quotient: Evaluates the sample with the quotient estimator (Touw and Hoogduin, 2011).
- regression: Evaluates the sample with the regression estimator (Touw and Hoogduin, 2011).

#### Value

An object of class jfaEvaluation containing:

confidence	a numeric value between 0 and 1 indicating the confidence level.
materiality	if materiality is specified, a numeric value between $0$ and $1$ indicating the performance materiality as a fraction of the total population size.
minPrecision	if minPrecision is specified, a numeric value between 0 and 1 indicating the minimum required precision as a fraction of the total population size.
method	a character indicating the evaluation method.
N	if N is specified, in integer larger than 0 indicating the population size.
n	an integer larger than 0 indicating the sample size.
k	an integer larger than, or equal to, $0$ indicating the number of items in the sample that contained an error.
t	a value larger than, or equal to, 0, indicating the sum of observed taints.
mle	a numeric value between $0$ and $1$ indicating the most likely error in the population as a fraction of its total size.
precision	a numeric value between 0 and 1 indicating the difference between the most likely error and the upper bound in the population as a fraction of the total population size.
popBookvalue	if populationBookValue is specified, a numeric value larger than $0$ indicating the total value of the population.
pointEstimate	if method is one of direct, difference, quotient, or regression, a numeric value indicating the point estimate of the population misstatement as a fraction the total population size.
lowerBound	if method is one of direct, difference, quotient, or regression, a numeric

ment as a fraction the total population size.

value indicating the lower bound of the interval around the population misstate-

upperBound if method is one of direct, difference, quotient, or regression, a numeric value indicating the upper bound of the interval around the population misstatement as a fraction the total population size. confBound a numeric value indicating the upper bound on the population misstatement as a fraction the total population size. conclusion if materiality is specified, a character indicating the conclusion about whether to approve or not approve the population with respect to the performance materiality. populationK if method = 'hypergeometric', an integer indicating the assumed total errors in the population. an object of class 'jfaPrior' that contains the prior distribution. prior an object of class 'jfaPosterior' that contains the posterior distribution. posterior a data frame containing the relevant columns from the sample. data

#### Author(s)

Koen Derks, <k.derks@nyenrode.nl>

#### References

Cox, D. and Snell, E. (1979). On sampling and the estimation of rare errors. *Biometrika*, 66(1), 125-132.

Dworin, L. D. and Grimlund, R. A. (1984). Dollar-unit sampling for accounts receivable and inventory. *The Accounting Review*, 59(2), 218–241

Leslie, D. A., Teitlebaum, A. D., & Anderson, R. J. (1979). *Dollar-unit Sampling: A Practical Guide for Auditors*. Copp Clark Pitman; Belmont, Calif.: distributed by Fearon-Pitman.

Meikle, G. R. (1972). *Statistical Sampling in an Audit Context: An Audit Technique*. Canadian Institute of Chartered Accountants.

Pap, G., and van Zuijlen, M. C. (1996). On the asymptotic behavior of the Stringer bound. *Statistica Neerlandica*, 50(3), 367-389.

Rohrbach, K. J. (1993). Variance augmentation to achieve nominal coverage probability in sampling from audit populations. *Auditing*, 12(2), 79.

Stringer, K. W. (1963). Practical aspects of statistical sampling in auditing. *In Proceedings of the Business and Economic Statistics Section* (pp. 405-411). American Statistical Association.

Touw, P., and Hoogduin, L. (2011). *Statistiek voor Audit en Controlling*. Boom uitgevers Amsterdam.

### See Also

auditPrior planning selection report auditBF

12 jfa-methods

jfa-methods

Methods for jfa objects

### **Description**

Methods defined for objects returned from the auditPrior, planning, selection, and evaluation functions.

#### Usage

```
## S3 method for class 'jfaPrior'
print(x, ...)
## S3 method for class 'jfaPosterior'
print(x, ...)
## S3 method for class 'jfaPlanning'
print(x, ...)
## S3 method for class 'jfaSelection'
print(x, ...)
## S3 method for class 'jfaEvaluation'
print(x, ...)
## S3 method for class 'summary.jfaPrior'
print(x, ...)
## S3 method for class 'summary.jfaPosterior'
print(x, ...)
## S3 method for class 'summary.jfaPlanning'
print(x, ...)
## S3 method for class 'summary.jfaSelection'
print(x, ...)
## S3 method for class 'summary.jfaEvaluation'
print(x, ...)
## S3 method for class 'jfaPrior'
summary(object, digits = 3, ...)
## S3 method for class 'jfaPosterior'
summary(object, digits = 3, ...)
```

planning 13

```
## S3 method for class 'jfaPlanning'
summary(object, digits = 3, ...)
## S3 method for class 'jfaSelection'
summary(object, digits = 3, ...)
## S3 method for class 'jfaEvaluation'
summary(object, digits = 3, ...)
## S3 method for class 'jfaPrior'
plot(x, xmax = 0.5, ...)
## S3 method for class 'jfaPosterior'
plot(x, xmax = 0.5, ...)
## S3 method for class 'jfaPlanning'
plot(x, xmax = 0.5, ...)
## S3 method for class 'jfaSelection'
plot(x, ...)
## S3 method for class 'jfaEvaluation'
plot(x, xmax = 0.5, ...)
```

#### **Arguments**

	further arguments, currently ignored.
object, x	an object of class jfaPrior, jfaPosterior, jfaPlanning, jfaSelection, or jfaEvaluation.
digits	an integer specifying the number of digits to which output should be rounded. Used in summary.
xmax	a number between 0 and 1 specifying the x-axis limits of the plot. Used in plot.

## Value

The summary methods return a data. frame which contains the input and output.

The print methods simply print and return nothing.

planning	Plan a statistical audit sample	

# **Description**

This function calculates the minimum sample size for a statistical audit sample based on the binomial, Poisson, or hypergeometric likelihood. The function returns an object of class jfaPlanning which can be used with associated summary() and plot() methods.

For more details on how to use this function, see the package vignette: vignette('jfa',package = 'jfa')

14 planning

#### Usage

#### **Arguments**

materiality a numeric value between 0 and 1 specifying the performance materiality (i.e.,

maximum upper limit) as a fraction of the total population size. Can be NULL,

but minPrecision should be specified in that case.

minPrecision a numeric value between 0 and 1 specifying the minimum precision (i.e., upper

bound minus most likely error) as a fraction of the total population size. Can be

NULL, but materiality should be specified in that case.

expectedError a numeric value between 0 and 1 specifying the expected errors in the sample

relative to the total sample size, or a number (>= 1) that represents the number of expected errors in the sample. It is advised to set this value conservatively to minimize the probability of the observed errors exceeding the expected errors,

which would imply that insufficient work has been done in the end.

likelihood a character specifying the likelihood assumed in the calculation. This can be

either binomial for the binomial likelihood, poisson for the Poisson likelihood, or hypergeometric for the hypergeometric likelihood. See the details section

for more information about the available likelihoods.

confidence a numeric value between 0 and 1 specifying the confidence level used in the

planning. Defaults to 0.95 for 95% confidence.

N an integer larger than 0 specifying the total population size. Only required when

likelihood = 'hypergeometric'.

prior a logical specifying whether to use a prior distribution when planning, or an ob-

ject of class jfaPrior or jfaPosterior containing the prior distribution. Defaults to FALSE for frequentist planning. If TRUE, a negligible prior distribution is chosen by default, but can be adjusted using the kPrior and nPrior arguments. Chooses a conjugate gamma distribution for the Poisson likelihood, a conjugate beta distribution for the binomial likelihood, and a conjugate beta-binomial

distribution for the hypergeometric likelihood.

nPrior if prior = TRUE, a numeric value larger than, or equal to, 0 specifying the sample

size of the sample equivalent to the prior information.

kPrior if prior = TRUE, a numeric value larger than, or equal to, 0 specifying the sum

of errors in the sample equivalent to the prior information.

increase an integer larger than 0 specifying the desired increase step for the sample size

calculation.

maxSize an integer larger than 0 specifying the maximum sample size that is considered

in the calculation. Defaults to 5000 for efficiency. Increase this value if the sample size cannot be found due to it being too large (e.g., for a low materiality).

# Details

This section elaborates on the available likelihoods and corresponding prior distributions for the likelihood argument.

planning 15

• binomial: The binomial likelihood is often used as a likelihood for attributes sampling *with* replacement. The likelihood function is defined as:

$$p(x) = \binom{n}{k} p^k (1-p)^{n-k}$$

The conjugate  $beta(\alpha, \beta)$  prior has probability density function:

$$f(x; \alpha, \beta) = \frac{1}{B(\alpha, \beta)} x^{\alpha - 1} (1 - x)^{\beta - 1}$$

• poisson: The Poisson likelihood is often used as a likelihood for monetary unit sampling (MUS). The likelihood function is defined as:

$$p(x) = \frac{\lambda^x e^{-\lambda}}{x!}$$

The conjugate  $gamma(\alpha, \beta)$  prior has probability density function:

$$f(x; \alpha, \beta) = \frac{\beta^{\alpha} x^{\alpha - 1} e^{-\beta x}}{\Gamma(\alpha)}$$

• hypergeometric: The hypergeometric likelihood is used as a likelihood for sampling *without* replacement. The likelihood function is defined as:

$$p(x=k) = \frac{\binom{K}{k} \binom{N-K}{n-k}}{\binom{N}{n}}$$

The conjugate beta-binomial( $\alpha, \beta$ ) prior (Dyer and Pierce, 1993) has probability density function:

$$f(k|n,\alpha,\beta) = \binom{n}{k} \frac{B(k+\alpha,n-k+\beta)}{B(\alpha,\beta)}$$

#### Value

An object of class jfaPlanning containing:

confidence a numeric value between 0 and 1 indicating the confidence level.

materiality a numeric value between 0 and 1 indicating the specified materiality. Can be

NULL.

minPrecision a numeric value between 0 and 1 indicating the minimum precision to be ob-

tained. Can be NULL.

expectedError a numeric value larger than, or equal to, 0 indicating the expected errors input.

likelihood a character indicating the specified likelihood.

N an integer larger than 0 indicating the population size (only returned if N is spec-

ified).

sampleSize an integer larger than 0 indicating the required sample size.

errorType a character indicating whether the expected errors where specified as a percent-

age or as an integer.

expectedSampleError

a numeric value larger than, or equal to, 0 indicating the number of errors that are allowed in the sample.

16 report

expectedBound a numeric value between 0 and 1 indicating the expected upper bound if the sample goes according to plan.

expectedPrecision

a numeric value between 0 and 1 indicating the expected precision if the sample

goes according to plan.

populationK if likelihood = 'hypergeometric', an integer larger than 0 indicating the as-

sumed population errors.

prior if a prior distribution is specified, an object of class jfaPrior that contains

information about the prior distribution.

expectedPosterior

if a prior distribution is specified, an object of class jfaPosterior that contains

information about the expected posterior distribution.

#### Author(s)

Koen Derks, <k.derks@nyenrode.nl>

#### References

Dyer, D. and Pierce, R.L. (1993). On the choice of the prior distribution in hypergeometric sampling. *Communications in Statistics - Theory and Methods*, 22(8), 2125 - 2146.

#### See Also

auditPrior selection evaluation report auditBF

# **Examples**

report

Create a statistical audit sampling report

#### **Description**

This function takes an object of class jfaEvaluation as returned by the evaluation() function automatically generates a html or pdf report containing the analysis results and their interpretation.

For more details on how to use this function, see the package vignette: vignette('jfa',package = 'jfa')

selection 17

#### Usage

```
report(object, file = 'report.html', format = 'html_document')
```

#### **Arguments**

object an object of class jfaEvaluation as returned by the evaluation() function.

file a character specifying the name of the report (e.g. report.html). By default,

the report is created in your current working directory.

format a character specifying the output format of the report. Possible options are

html\_document (default) and pdf\_document, but compiling to pdf format re-

quires a local version of MikTex.

#### Value

A html or pdf file containing a report of the evaluation.

#### Author(s)

Koen Derks, <k.derks@nyenrode.nl>

#### See Also

auditPrior planning selection evaluation auditBF

18 selection

#### **Description**

This function takes a data frame and performs statistical sampling according to one of three algorithms: random sampling, cell sampling, and fixed interval sampling. Sampling is done on the level of two possible sampling units: records or monetary units. The function returns an object of class jfaSelection which can be used with associated summary() and a plot() methods.

For more details on how to use this function, see the package vignette: vignette('jfa',package = 'jfa')

#### Usage

# **Arguments**

population	a data frame containing the population of items the auditor wishes to sample from.	
sampleSize	an integer larger than 0 specifying the number of sampling units that need to be selected from the population. Can also be an object of class jfaPlanning.	
units	a character specifying the sampling units used. Possible options are records (default) for selection on the level of items or mus for selection on the level of monetary units.	
algorithm	a character specifying the sampling algorithm used. Possible options are random (default) for random sampling, cell for cell sampling, or interval for fixed interval sampling.	
bookValues	a character specifying the name of the column in the population that contains the book values of the items.	
intervalStarti	ngPoint	
	if algorithm = 'interval', an integer larger than 0 specifying the starting point of the algorithm.	
ordered	a logical specifying whether to first order the items in the population according to the value of their bookValues. Defaults to TRUE.	
ascending	if ordered = TRUE, a logical specifying whether to order the population bookValues from smallest to largest. Defaults to TRUE.	
withReplacement		
	if algorithm = 'random', a logical specifying whether sampling should be performed with replacement. Defaults to FALSE.	
seed	if algorithm = 'random' or algorithm = 'cell', an integer specifying a seed to reproduce results. Defaults to 1.	

#### Details

The first part of this section elaborates on the two possible options for the units argument:

- records: In record sampling each item in the population is seen as a sampling unit. An item of \$5000 is therefore equally likely to be selected as an item of \$500.
- mus: In monetary unit sampling each monetary unit in the population is seen as a sampling unit. An item of \$5000 is therefore ten times more likely to be selected as an item of \$500.

selection 19

The second part of this section elaborates on the three possible options for the algorithm argument:

• random: In random sampling each sampling unit in the population is drawn with equal probability.

- cell: In cell sampling the sampling units in the population are divided into a number (equal to the sample size) of intervals. From each interval one sampling unit is selected with equal probability.
- interval: In fixed interval sampling the sampling units in the population are divided into a number (equal to the sample size) of intervals. From each interval one sampling unit is selected according to a fixed starting point (specified by intervalStartingPoint).

#### Value

An object of class jfaSelection containing:

population a data frame containing the input population.

sample a data frame containing the selected sample of items.

units a character indicating the sampling units that were used to create the selection.

algorithm a character indicating the the algorithm that was used to create the selection.

bookValues if bookValues is specified, a character indicating the name of the book value

column.

### Author(s)

Koen Derks, <k.derks@nyenrode.nl>

#### References

Leslie, D. A., Teitlebaum, A. D., & Anderson, R. J. (1979). *Dollar-unit Sampling: A Practical Guide for Auditors*. Copp Clark Pitman; Belmont, Calif.: distributed by Fearon-Pitman.

Wampler, B., & McEacharn, M. (2005). Monetary-unit sampling using Microsoft Excel. *The CPA journal*, 75(5), 36.

# See Also

auditPrior planning evaluation report auditBF

# **Index**

```
* Bayes
                                                 jfa-methods, 12
    auditBF, 2
                                                 planning, 4, 7, 11, 12, 13, 17, 19
* audit
                                                 plot.jfaEvaluation(jfa-methods), 12
    auditBF, 2
                                                 plot.jfaPlanning(jfa-methods), 12
    auditPrior, 4
                                                 plot.jfaPosterior(jfa-methods), 12
    evaluation, 8
                                                 plot.jfaPrior(jfa-methods), 12
    planning, 13
                                                 plot.jfaSelection(jfa-methods), 12
    report, 16
                                                 print.jfaEvaluation(jfa-methods), 12
    selection, 17
                                                 print.jfaPlanning(jfa-methods), 12
* bound
                                                 print.jfaPosterior(jfa-methods), 12
    evaluation, 8
                                                 print.jfaPrior(jfa-methods), 12
* confidence
                                                 print.jfaSelection(jfa-methods), 12
    evaluation, 8
                                                 print.summary.jfaEvaluation
* datasets
                                                          (jfa-methods), 12
    BuildIt. 7
                                                 print.summary.jfaPlanning
* distribution
                                                          (jfa-methods), 12
    auditBF. 2
                                                 print.summary.jfaPosterior
    auditPrior, 4
                                                          (jfa-methods), 12
* evaluation
                                                 print.summary.jfaPrior(jfa-methods), 12
    evaluation, 8
                                                 print.summary.jfaSelection
    report, 16
                                                          (jfa-methods), 12
* factor
    auditBF. 2
                                                 report, 4, 7, 11, 16, 16, 19
* planning
    planning, 13
                                                 selection, 4, 7, 11, 12, 16, 17, 17
* prior
                                                 summary.jfaEvaluation(jfa-methods), 12
    auditBF, 2
                                                 summary.jfaPlanning(jfa-methods), 12
    auditPrior, 4
                                                 summary.jfaPosterior(jfa-methods), 12
* report
                                                 summary.jfaPrior(jfa-methods), 12
    report, 16
                                                 summary.jfaSelection(jfa-methods), 12
* sample
    planning, 13
    selection, 17
* selection
    selection, 17
* size
    planning, 13
auditBF, 2, 7, 11, 16, 17, 19
auditPrior, 4, 4, 11, 12, 16, 17, 19
BuildIt, 7
evaluation, 4, 7, 8, 12, 16, 17, 19
```