

# Exercises CPM

## Course Seignosse 2018, day 4

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These exercises are meant to give you an intuition about the dynamics of the CPM. Feel free to explore any of the parameters of the model as much as you like, to see how they influence the behaviour. The questions are just there to guide you to some interesting places. It has been heavily inspired by exercises from the EMBO course organised by dr. Stan Marée and dr. Verônica Grieneisen at the John Innes Center in Norwich; they are also an excellent resource for anything CPM related.

## Getting started

### Linux basics

If Linux is new to you, using the terminal may be quite daunting. Here are some handy commands to get you started:

- `cd dirname` will move you into this directory (`cd`=“change directory”) Press tab after `cd` to see options and to autocomplete the `dirname`. `cd ..` will move you to a higher directory, and just `cd` will take you to the home dir.
- `ls` lists the files in the current directory.
- `gedit textfilename` will open a simple editor (handy for parameter files). If the file does not exist, it will create it for you (don't forget to save).
- `mkdir name` make a new directory.
- `cp filename filename2` make a copy of a file. For copies of directories, add the flag `-r` after `cp`
- `rm filename` remove file. Be careful with this command: files that are removed this way irretrievable. `rm *` will remove all files in the current directory, so be mindful of what you type.'
- `ctrl+C` to break off a running process in the terminal – handy if stuff gets stuck!
- for more handy commands, see <https://www.makeuseof.com/tag/an-a-z-of-linux-40-essential-commands-you-should-know/>

### Compiling and running the program

The code you are working with was mostly written by me and Prof. ten Tusscher for personal use, and is therefore very basic. For the questions in this tutorial, you will only have to modify flags and parameters in the parameter file, and look at the pictures of the simulation. You are of course welcome to dig into the code if you feel like; you can ask me for pointers.

Let's assume you already have a Linux Virtual Machine up and running. The code depends on a few extra libraries, to get them, type the following in the terminal (hit ENTER after each command):

```
sudo apt-get update
sudo apt-get install libgl0-dev libboost-all-dev freeglut3-dev libpng-dev
```

To compile the code, simply type `make` into the terminal, and wait for compilation to finish. Then run the program as follows (the executable is in the directory `bin`):

```
./bin/CPM -d DIRNAME -s SEED parfile.cfg
```

Where for `DIRNAME` you should substitute a nice name; this is the directory in which the pictures of your simulation will end up. If you rerun the program with the same `DIRNAME`, existing pictures will be overwritten. You can also remove the pictures in there (type `rm -rf DIRNAME/*`). For `SEED`, substitute any integer number. Change it once in a while to see differences between simulations with identical parameters.

To see the results of your simulations, you can either look at individual frames in `DIRNAME`, or browse through all of them with the following command:

```
eog DIRNAME/
```

Use the left/right arrow keys to browse through the pictures, and keep the right arrow key pressed to get a sort of movie of your simulation.

NOTE: if you like the outcome of a particular simulation, it may be a good idea to save a copy of your parameters in a separate file, using `cp`.

## 1 Differential Adhesion

Remember that CPM dynamics are governed by the Hamiltonian:

$$H = \sum_{\sigma} \lambda (a_{\sigma} - A_{\tau(\sigma)})^2 + \sum_{\text{all } \sigma, \sigma' \text{ neighbours}} \frac{J_{\sigma, \sigma'}}{2} + \sum_{\text{all } \sigma, \text{medium neighbours}} J_{\sigma, \text{medium}}$$

In the first part of the equation,  $A$  is the target volume of cell  $\sigma$  and  $\lambda$  is the resistance of the cell to changes in volume. The second part of the equation controls adhesion to other cells and to the surrounding medium. Remember that the algorithm is trying to minimise the total energy of the system  $H$ , so large deviations from the target volume become progressively less likely and cells with a high  $J$  value will likely reduce their contact area and not adhere. The dynamics result from the system trying to balance these sometimes opposing demands.

The following relationships link the  $J$  values between cell types to the surface tension ( $\gamma$ ) between tissues as a whole:

$$\begin{aligned} \gamma_{\tau a, \tau b} &= J_{\tau a, \tau b} - \frac{J_{\tau a, \tau a} + J_{\tau b, \tau b}}{2} \\ \gamma_{\tau a, med} &= J_{\tau a, med} - \frac{J_{\tau a, \tau a}}{2} \end{aligned} \tag{1}$$

Having positive surface tension means the two cell types will separate (like oil and water), while for negative surface tension the two types will intermingle.

Another important parameter of the model is the temperature,  $T$ . For one update step of the CPM, we ask for all points in the grid <sup>1</sup> whether a neighbouring point will copy into them. A copy is accepted with the following probability:

$$P_{1 \rightarrow 2} = \begin{cases} 1, & \text{if } \Delta H \leq 0. \\ e^{\frac{-\Delta H}{T}}, & \text{if } \Delta H > 0 \end{cases} \tag{2}$$

Here,  $\Delta H = H_{after} - H_{before}$ : whether this copy would increase or decrease the total energy  $H$  of the system. Copies that lower this energy are always accepted. The temperature  $T$  regulates the probability with which the algorithm accepts energetically unfavorable copies.

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<sup>1</sup>Actually, for one step we typically just randomly update  $L \times W$  points in the grid - so occasionally a point may be skipped or updated 2x. This makes no difference for the dynamics.

## 1.1 One cell type

Let's first look at the simplest case, where we have one cell and one celltype, so we only have to worry about the interaction between this cell and the surrounding medium.

- Open the parameter file, and make sure `NrCellTypes` and `InitNrCells` are set to 1. Run the simulation with different `temperature` and `labdavo1` ( $\lambda$ ) values, and observe the differences.
- Change the `Jcell1med` parameter, while keeping `temperature` and `labdavo1` constant.  
How do the membrane dynamics change?  
What happens when this parameter becomes negative?
- Add more cells (say 50), and change `Jcell1cell1` (it's typically kept to even values).  
Do you see the difference when it is larger or smaller than `Jcell1med*2`, and how can you explain this via the surface tension?  
What happens when this parameter is negative?  
How do the dynamics depend on other parameters?
- There is an option to spread cells randomly in the grid: set `CellPlace` to 0, then set `Jcell1cell1 < Jcell1med*2`.  
Do you get the same configuration as before?  
Make the grid bigger (parameters `L` and `W`), how does that change things?

## 1.2 Two cell types

The dynamics now depend on more parameters: `Jcell1cell1`, `Jcell1cell2`, `Jcell2cell2`, and the `J` values of the two celltypes with the medium. Don't set the temperature too low: between 10 and 20 is typically ok. Start with a clumped configuration and `NrCellTypes=2`. It may also be a good idea to run the simulation for longer (`NrDevSteps`; also increase the `picinterval`, otherwise it takes forever to look at the movie!

- First change `Jcell1cell2` while keeping `Jcell1med` and `Jcell2med` equal, and `Jcell1cell1` and `Jcell2cell2` too (smaller than `Jcell1med*2`).  
When does the behaviour change, and why?
- Try to get one cell type to engulf another. What `J` values did you use, and why?  
Make sure to run your simulations for long enough.
- Try to find as many configurations as possible with two cell types. Also consider qualitative differences: in the case of sorted tissues, how does the contact angle between tissues depend on the `J` values?
- Would differential adhesion be a suitable mechanism for development, such as cell sorting?

## 1.3 Three cell types

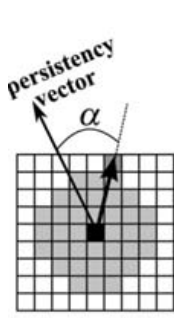
With three cell types, there are even more `J` values to play around with. Try different combinations; first predict what configuration will follow and why, then test with the model. If necessary, run for longer to see if the configuration changes further. Do you always reach your predicted configuration, and why (not)? Are you necessarily wrong in your prediction? What does this mean for the biological questions you're trying to answer? Save some of the parameter files of interesting configurations for the next section.

## 2 Cell migration

Cell migration is an important part of an organism's toolkit, e.g during embryonic development and immune responses. Migrating cells have a distinct front and back: they are more likely to keep moving forward at the front, while retracting in the back.

A very simple form of migration can be implemented in CPM as follows:

$$\Delta H = H_{t+1} - H_t - \mu \cos(\alpha)$$



Here,  $\alpha$  is the angle between the direction the cell wants to move in (the “targetvector”) and the direction of the pixel copy being considered, as considered from the center of mass of the cell.  $\mu$  modifies the strength of migration. First consider why the equation looks like this. Why the cosine? What happens for different directions of possible pixel copy events?

In addition to extending the Hamiltonian, cells in the model now have to keep track of their preferred direction of motion. Of course, they will often encounter obstacles, like other cells, and won’t be able to move exactly in that direction. Rather than doggedly trying to keep moving there, cells will pause, change their course and continue in a different direction. The pause is thought to be caused by rearrangements of the actin cytoskeleton involved in migration. We implement this by changing the targetvector every `perstime` time steps to the actual direction in which the cell has been moving during that period.

For these exercises, use a bigger grid to give cells plenty of space to move. 400x400, with smaller cells (e.g. 30-50 for `targetvo10` will do. Note that there is an initialisation period (300 steps) during which cells will not migrate yet!

- Set `NrCellTypes` and `InitNrCells` to 1, and gradually increase  $\mu(\mu)$  and `perstime`. What do you notice about this lonely cell’s pattern of movement?
- Add more cells of the same cell type, and play with the initial configuration and the adhesion between cells: either scattered randomly or clumped and either adhering to each other or not. What do you observe about their patterns of motion? How would this be relevant for e.g. collective cell migration in development, or T cell migration in lymph nodes?
- Go back to some of the configurations you were trying to make in the previous section, but now add a bit of active migration (keep  $\mu$  and `perstime` somewhat small). What do you observe, and why is that? How would this be relevant for development?

Handy resources if you’re interested in knowing more:

## References

- [1] A. R. A. Anderson, M. A. J. Chaplain, and K. A. Rejniak, editors. *Single-Cell-Based Models in Biology and Medicine*. Birkhäuser Verlag, Basel, 2007.
- [2] James A. Glazier and François Graner. Simulation of the differential adhesion driven rearrangement of biological cells. *Phys. Rev. E*, 47:2128–2154, Mar 1993.
- [3] François Graner and James A. Glazier. Simulation of biological cell sorting using a two-dimensional extended Potts model. *Phys. Rev. Lett.*, 69:2013–2016, Sep 1992.
- [4] Ramiro Magno, Verónica A. Grieneisen, and Athanasius F.M. Marée. The biophysical nature of cells: potential cell behaviours revealed by analytical and computational studies of cell surface mechanics. *BMC Biophysics*, 2015.