

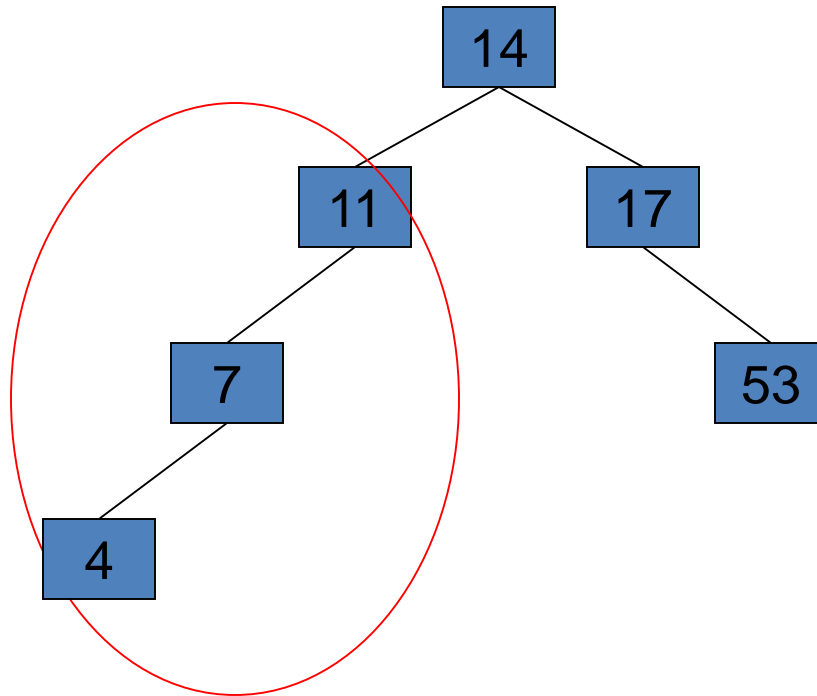


AVL TREE

:: EJERCICIOS ::

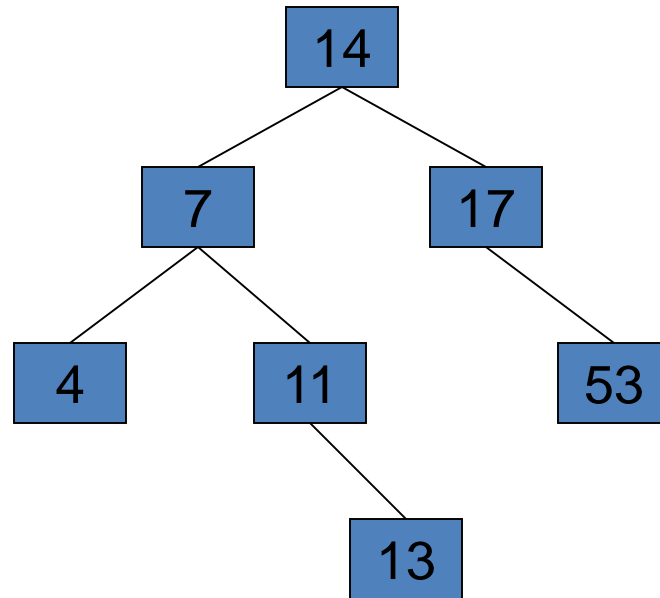
AVL Tree Example:

- Insert 14, 17, 11, 7, 53, 4, 13 into an empty AVL tree



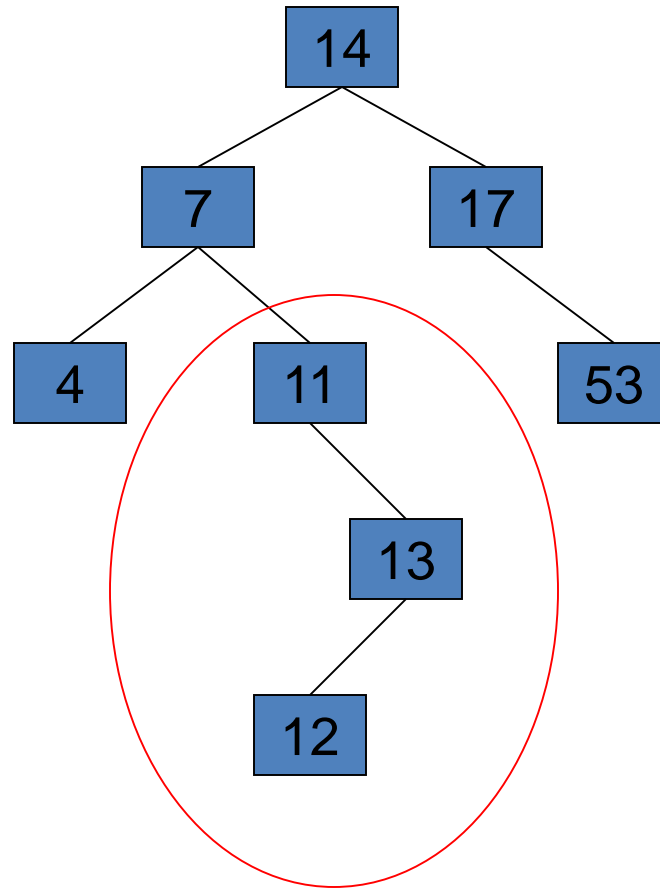
AVL Tree Example:

- Insert 14, 17, 11, 7, 53, 4, 13 into an empty AVL tree



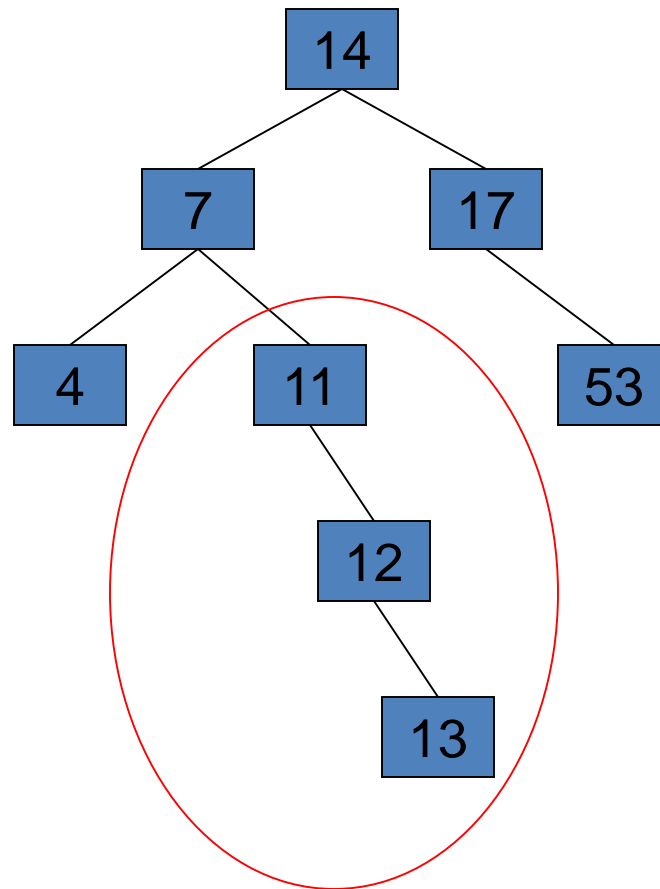
AVL Tree Example:

- Now insert 12



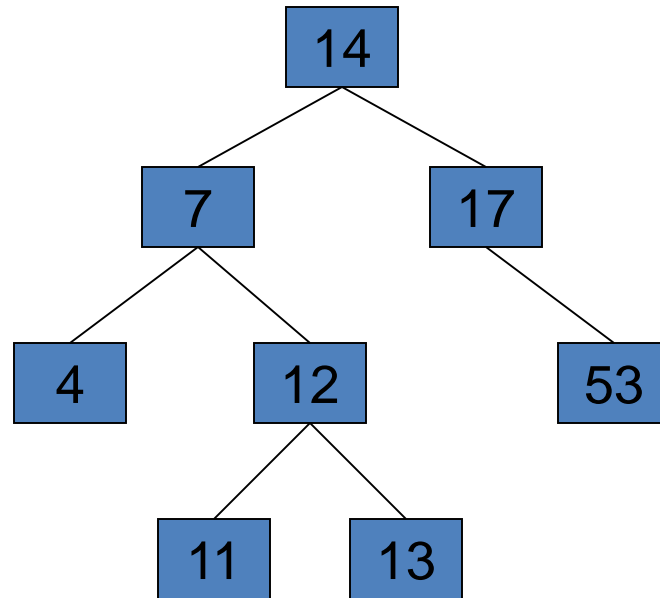
AVL Tree Example:

- Now insert 12



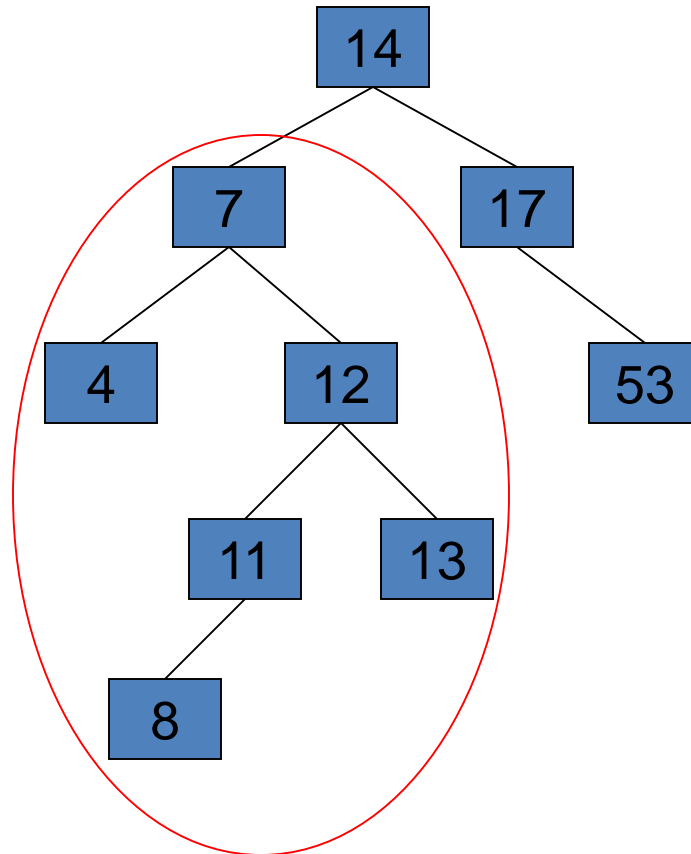
AVL Tree Example:

- Now the AVL tree is balanced.



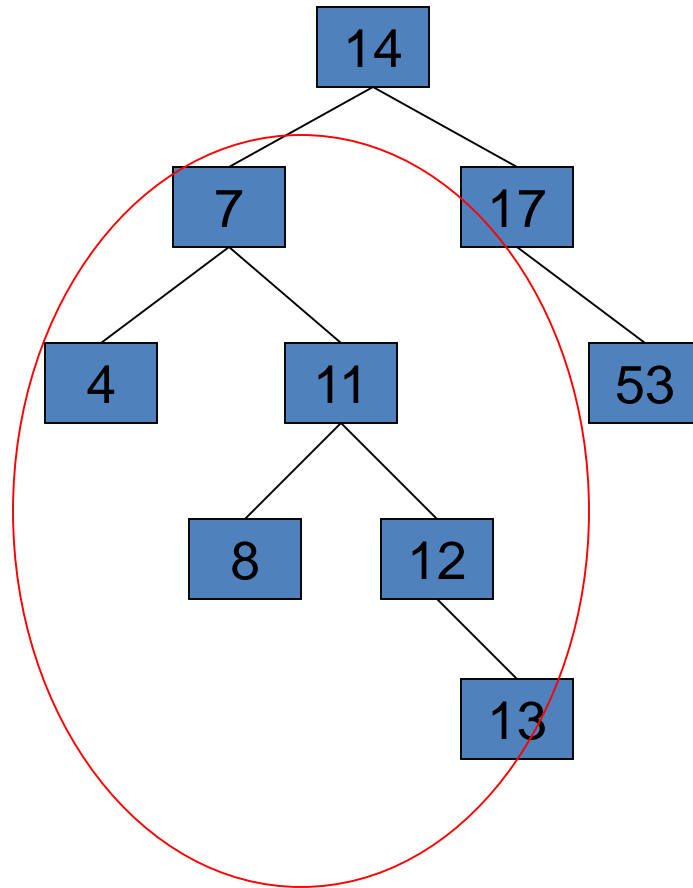
AVL Tree Example:

- Now insert 8



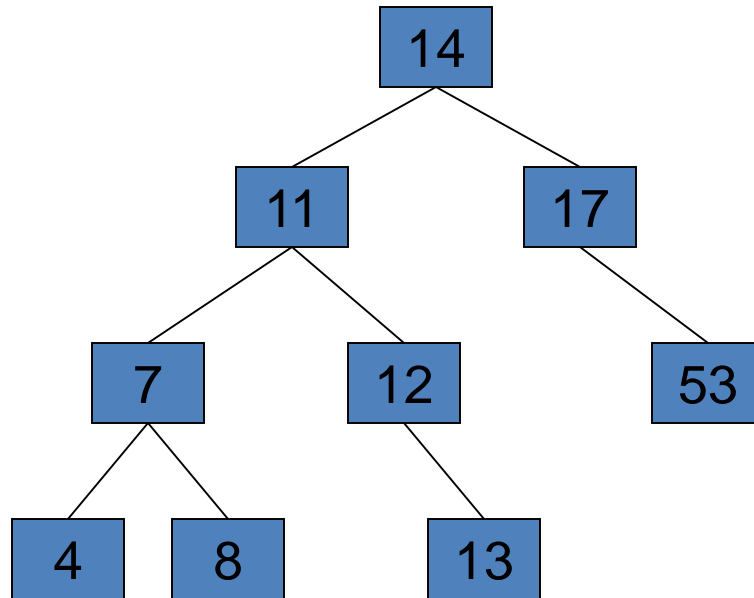
AVL Tree Example:

- Now insert 8



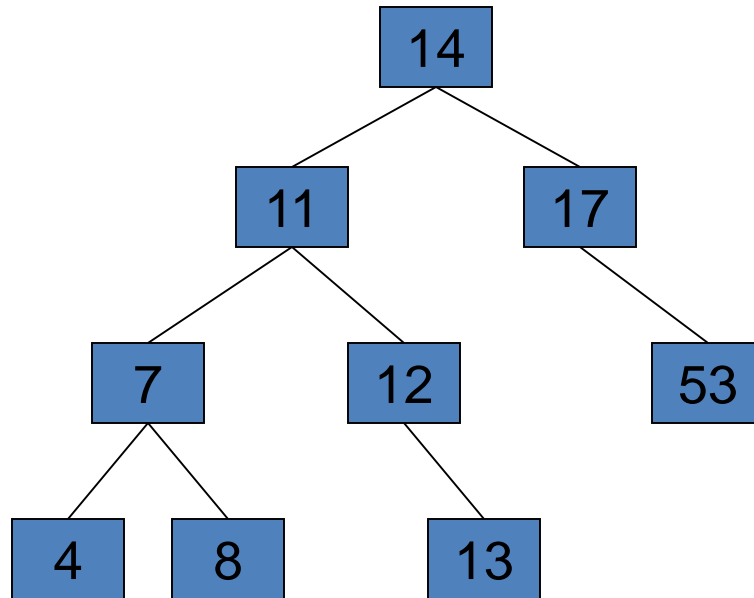
AVL Tree Example:

- Now the AVL tree is balanced.



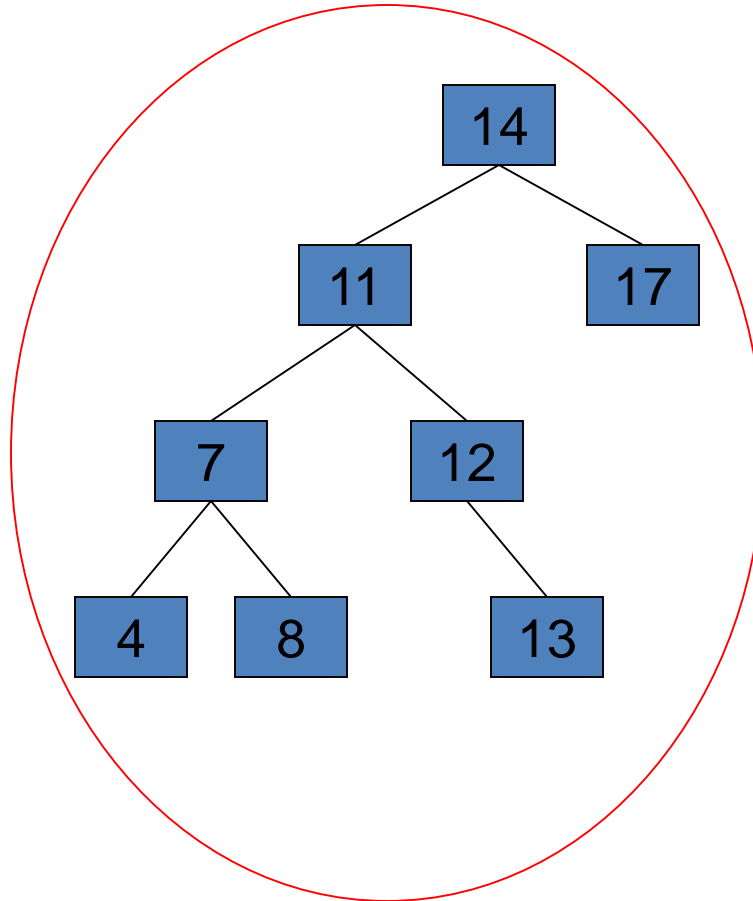
AVL Tree Example:

- Now remove 53



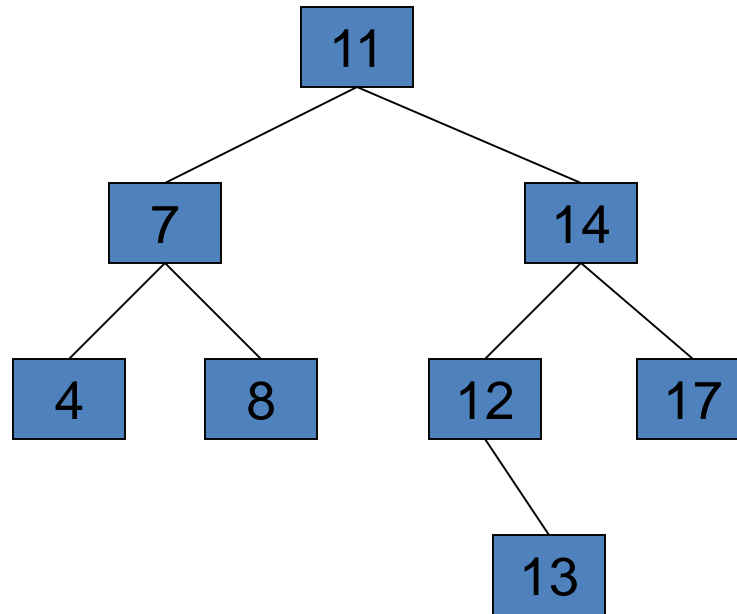
AVL Tree Example:

- Now remove 53, unbalanced



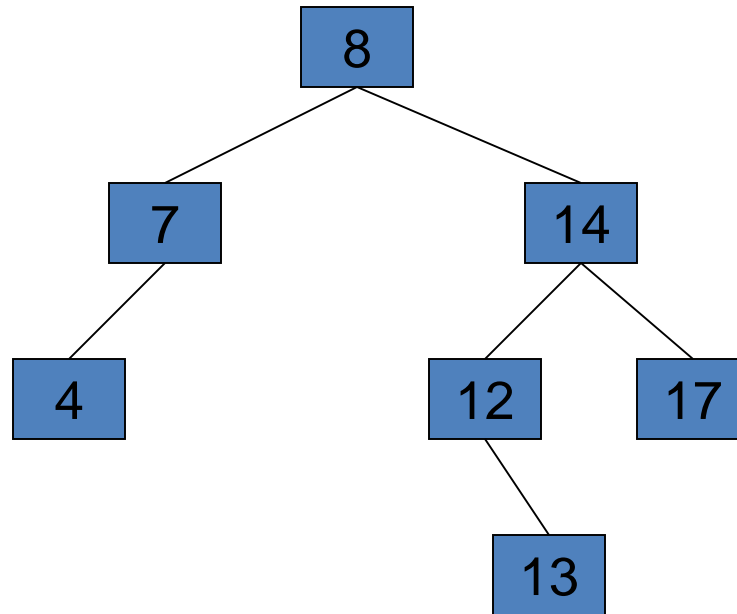
AVL Tree Example:

- **Balanced! Remove 11**



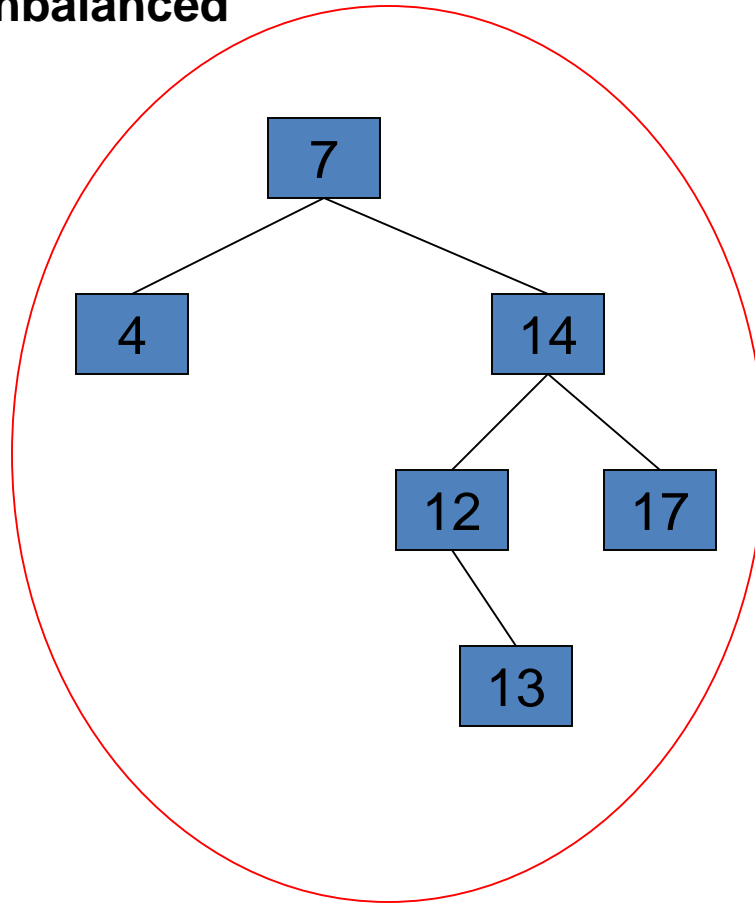
AVL Tree Example:

- Remove 11, replace it with the largest in its left branch



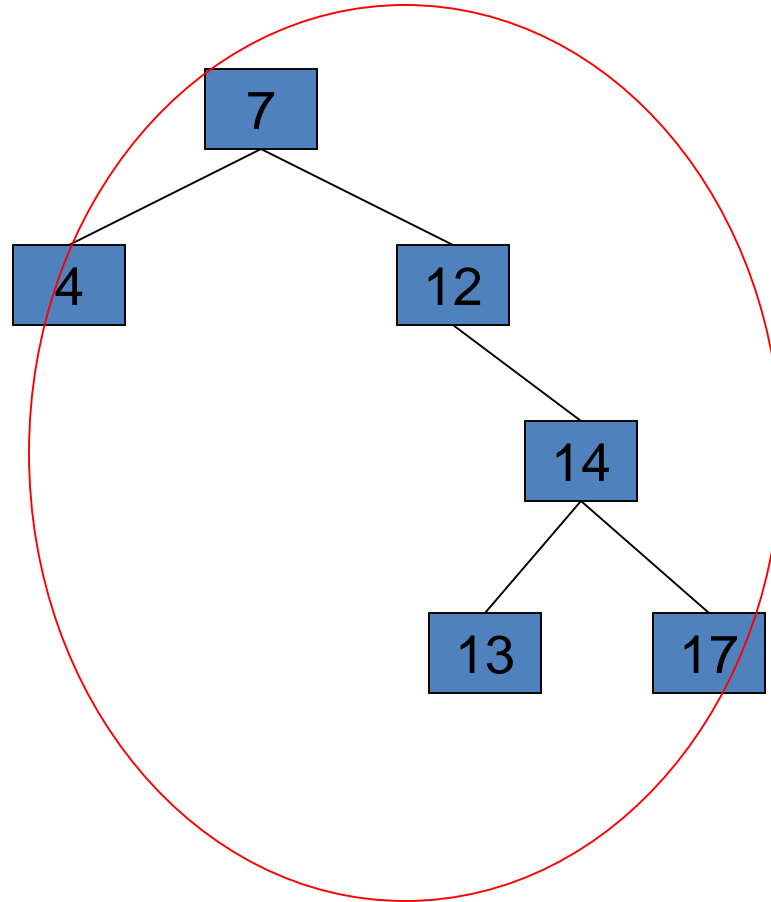
AVL Tree Example:

- Remove 8, unbalanced



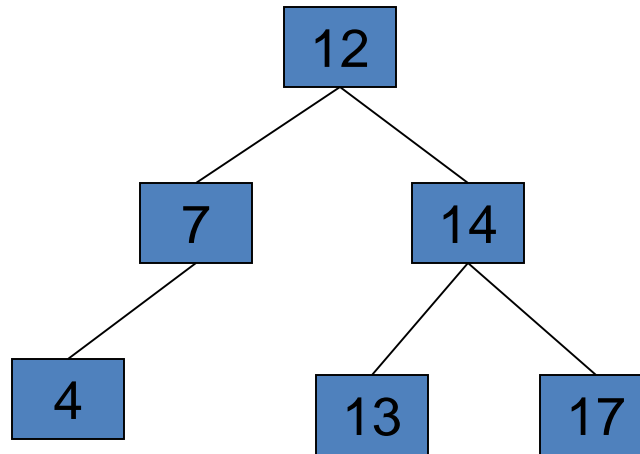
AVL Tree Example:

- Remove 8, unbalanced



AVL Tree Example:

- **Balanced!!**

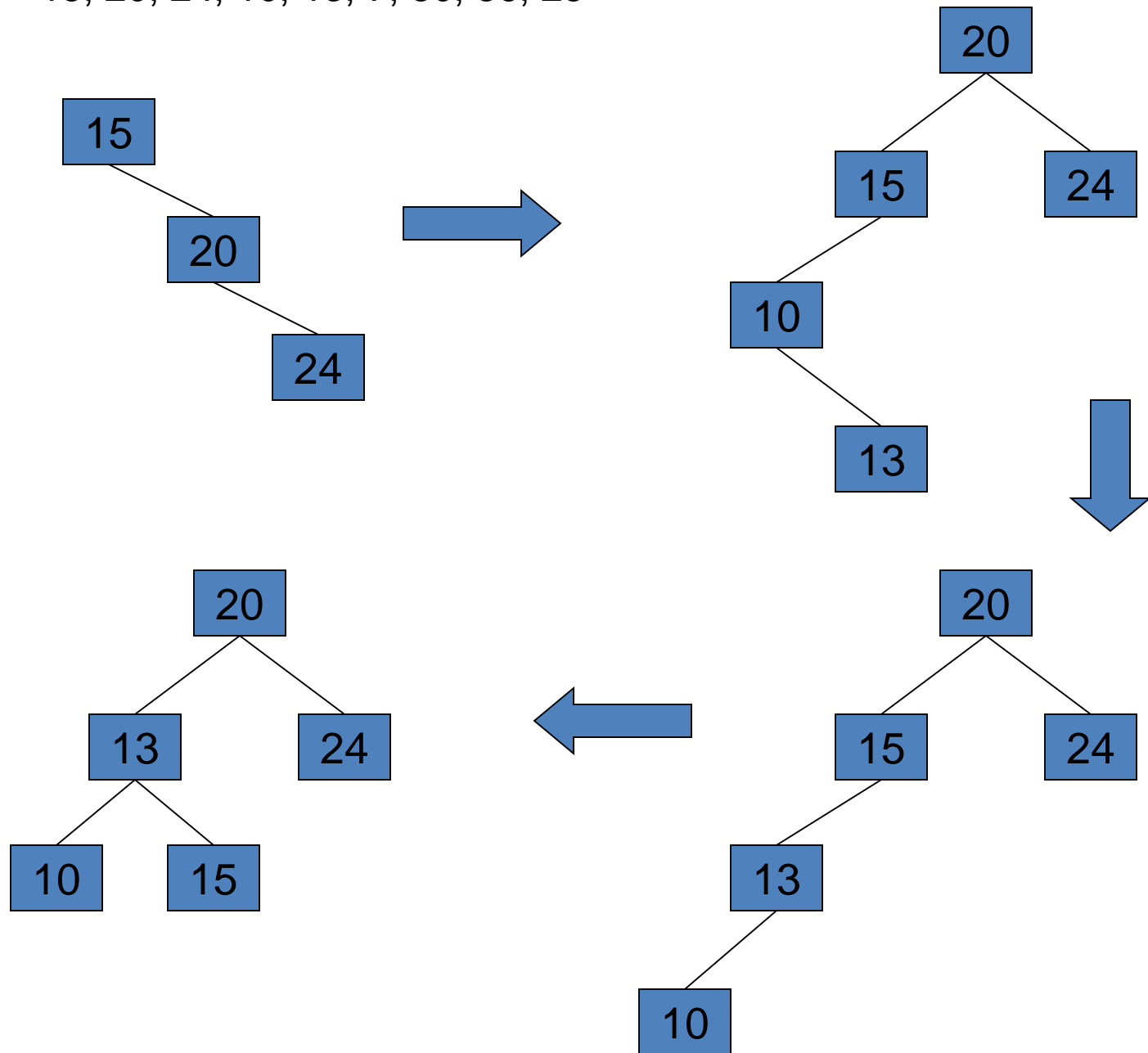


In Class Exercises

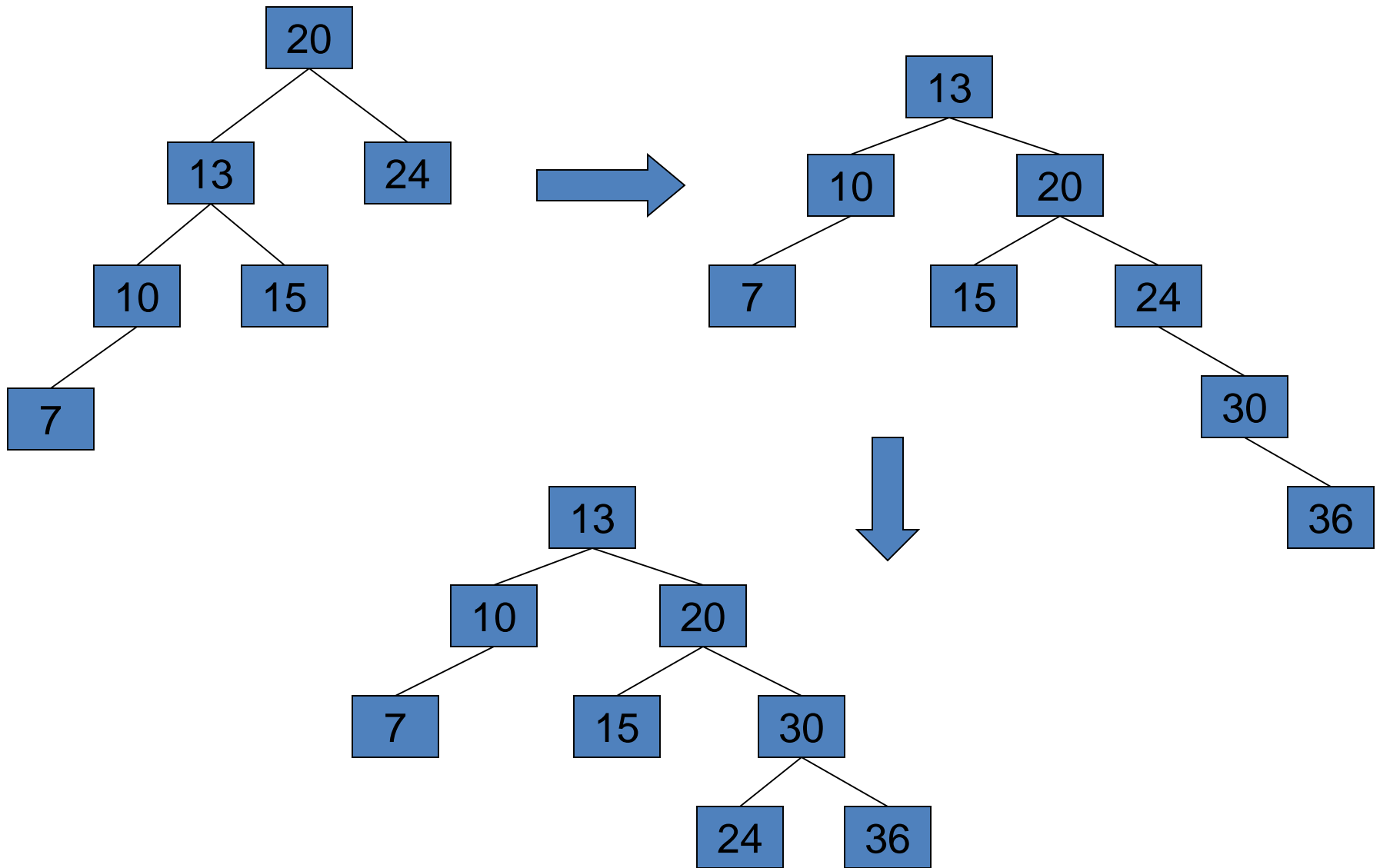
❖ Build an AVL tree with the following values:

15, 20, 24, 10, 13, 7, 30, 36, 25

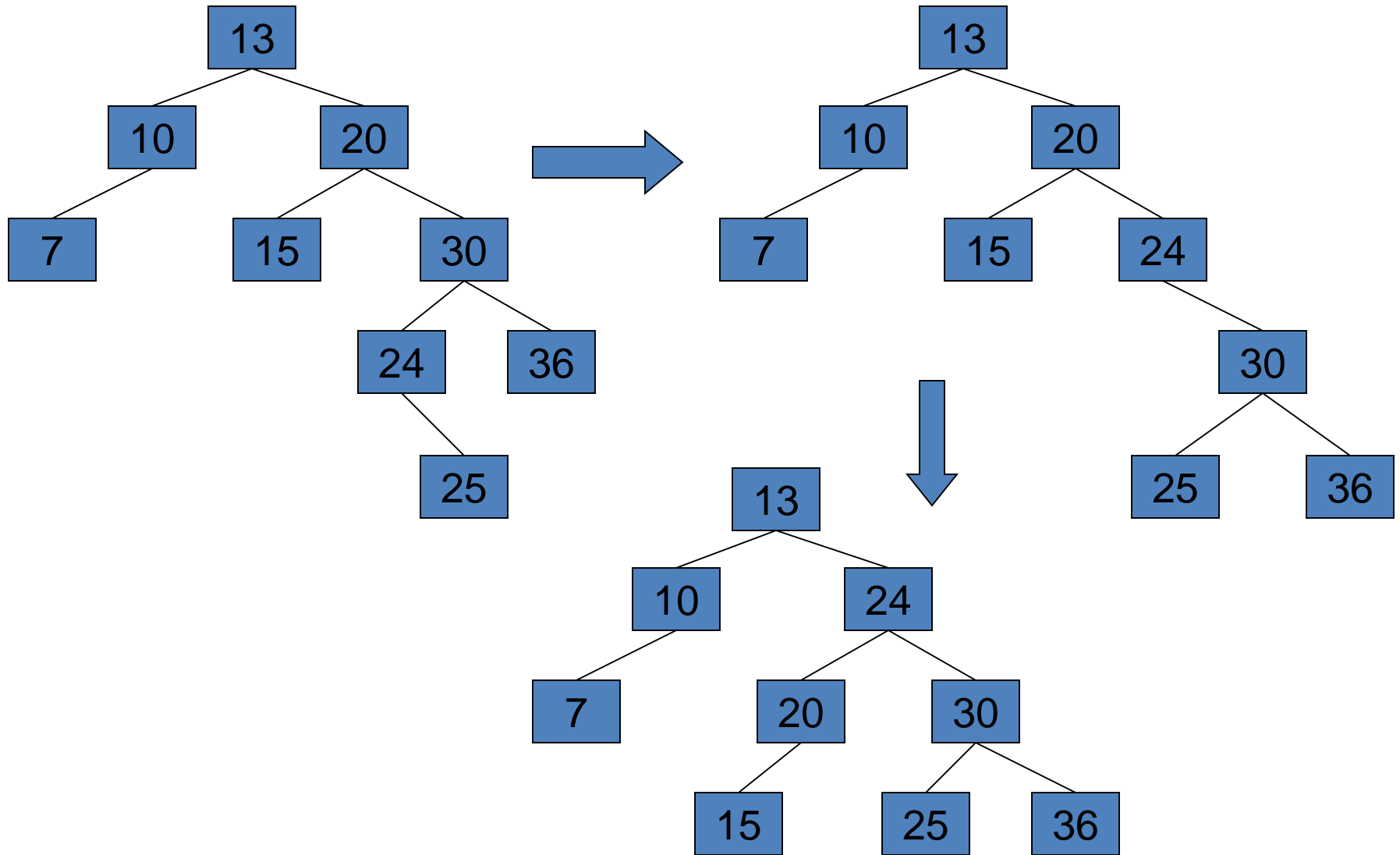
15, 20, 24, 10, 13, 7, 30, 36, 25



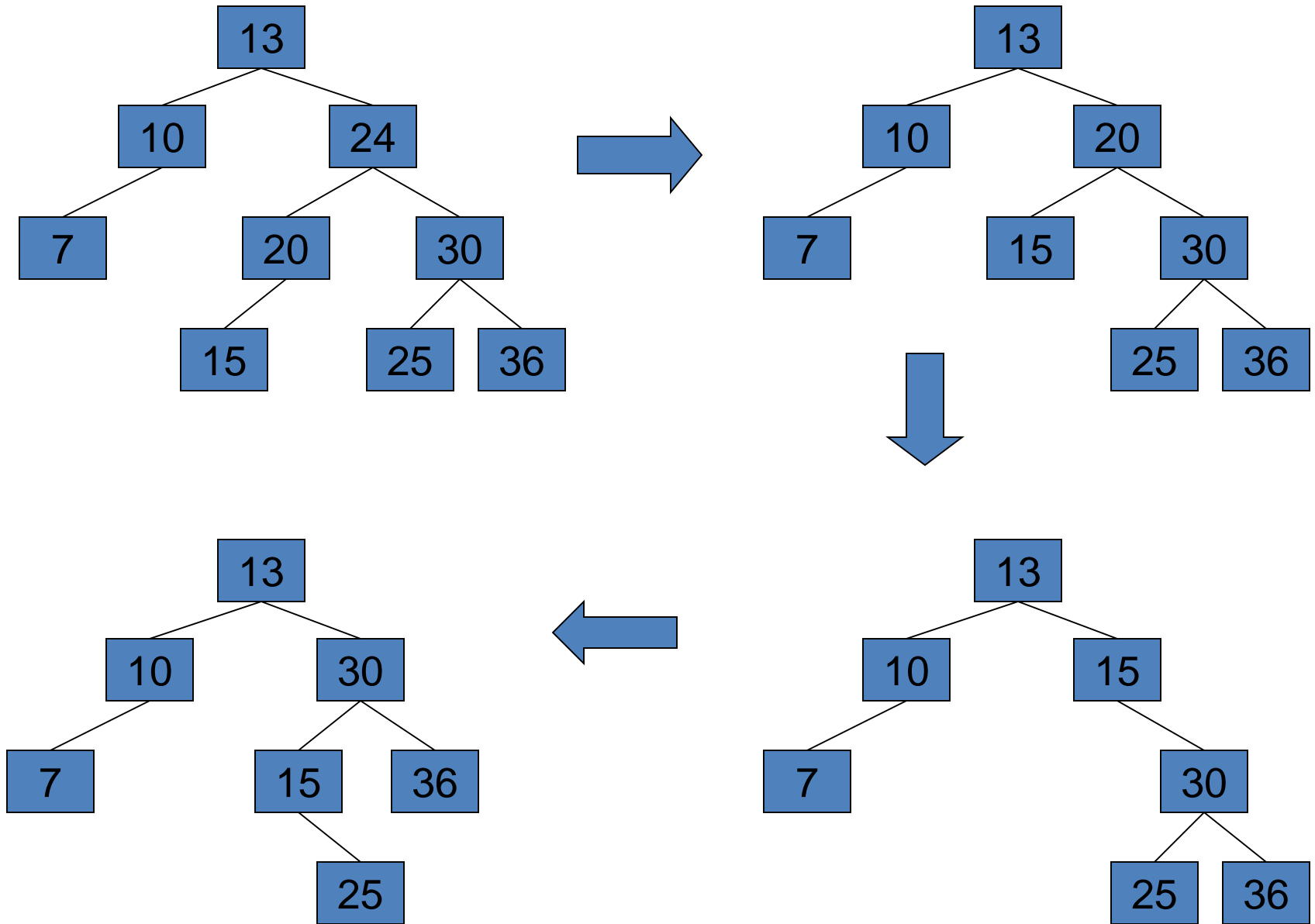
15, 20, 24, 10, 13, 7, 30, 36, 25



15, 20, 24, 10, 13, 7, 30, 36, 25



Remove 24 and 20 from the AVL tree.





AVL TREE

:: IMPLEMENTATIONS - AVLSolution2::

```

1  #ifndef __AVL_H__
2  #define __AVL_H__
3
4  #include <functional>
5  #include <algorithm>
6
7  template <typename T, typename R=T>
8  class AVLTree {
9      struct Node {
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25         Node*          root;
26         int             length;
27         std::function<R(T)> key;
28
29     private:
30         void destroy(Node* n) {
31             if (n != nullptr) {
32
33
34             }
35
36         void rotAB(Node*& n) {
37
38
39
40
41
42
43
44         void rotBA(Node*& n) {
45
46
47
48
49
50
51
52         void balance(Node*& n) {
53
54
55
56
57
58
59
60
61
62
63
64
65
66         void add(Node*& n, T e) {
67
68
69
70
71
72
73
74
75
76
77
78     public:
79         AVLTree(std::function<R(T)> key = [](T a) { return a; })
80             : root(nullptr), length(0), key(key) {}
81         ~AVLTree() { destroy(root); }
82
83         int Height() {
84
85
86         int Size() {
87
88
89         void Add(T e) {
90
91
92
93
94     };
95
96 #endif

```

```

7  template <typename T, typename R=T>
8  class AVLTree {
9      struct Node {
10         T      e;
11         Node* l;
12         Node* r;
13         int    h;
14
15         Node(T e) : e(e), l(nullptr), r(nullptr), h(0) {}
16
17         static int height(Node* n) {
18             return n == nullptr? -1 : n->h;
19         }
20         void updateH() {
21             h = std::max(Node::height(l), Node::height(r)) + 1;
22         }
23     };

```



```

7  template <typename T, typename R=T>
8  class AVLTree {
9  public:
24     struct Node {
25         Node*          root;
26         int             length;
27         std::function<R(T)> key;
28
29     private:
30         void destroy(Node* n) {
31             if (n != nullptr) {
32                 destroy(n->l);
33                 destroy(n->r);
34             }
35         }
36         void rotAB(Node*& n) {
37             Node* aux = n->l;
38             n->l = aux->r;
39             n->updateH();
40             aux->r = n;
41             n = aux;
42             n->updateH();
43         }
44         void rotBA(Node*& n) {
45             Node* aux = n->r;
46             n->r = aux->l;
47             n->updateH();
48             aux->l = n;
49             n = aux;
50             n->updateH();

```

```

52 void balance(Node*& n) {
53     int delta = Node::height(n->l) - Node::height(n->r);
54     if (delta < -1) {
55         if (Node::height(n->r->l) > Node::height(n->r->r)) {
56             rotAB(n->r);
57         }
58         rotBA(n);
59     } else if (delta > 1) {
60         if (Node::height(n->l->r) > Node::height(n->l->l)) {
61             rotBA(n->l);
62         }
63         rotAB(n);
64     }
65 }
66 void add(Node*& n, T e) {
67     if (n == nullptr) {
68         n = new Node(e);
69         return;
70     } else if (key(e) < key(n->e)) {
71         add(n->l, e);
72     } else {
73         add(n->r, e);
74     }
75     balance(n);
76     n->updateH();
77 }
78 public:
79     AVLTree(std::function<R(T)> key = [](T a) { return a; })
80         : root(nullptr), length(0), key(key) {}
81     ~AVLTree() { destroy(root); }

```

```

66     void add(Node*& n, T e) {
67         if (n == nullptr) {
68             n = new Node(e);
69             return;
70         } else if (key(e) < key(n->e)) {
71             add(n->l, e);
72         } else {
73             add(n->r, e);
74         }
75         balance(n);
76         n->updateH();
77     }
78 public:
79     AVLTree(std::function<R(T)> key = [](T a) { return a; })
80         : root(nullptr), length(0), key(key) {}
81     ~AVLTree() { destroy(root); }
82
83     int Height() {
84         return Node::height(root);
85     }
86     int Size() {
87         return length;
88     }
89     void Add(T e) {
90         add(root, e);
91         ++length;
92     }

```

```
1  #include <iostream>
2  #include "avl.hpp"
3
4  using namespace std;
5
6  = int main() {
7      AVLTree<int>* t = new AVLTree<int>();
8
9      = for (int i = 0; i < 1e6; ++i) {
10         t->Add(i);
11     }
12
13     cout << t->Height() << endl;
14
15     delete t;
16     return 0;
17 }
18
```