# Assignment 1

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### Theory

#### Problem 1

we can derive how many steps are needed from this equation:

$$2\gamma^i/(1-\gamma)||Q0-Q*|| \le \epsilon \tag{1}$$

because  $2\gamma^i/(1-\gamma)||Q0-Q*||$  is the distance between  $v^{\pi i}(s)$  and  $v^*(s)$ .

First of all we know both Q0 and  $Q* \in [0, 1/(1-\gamma)]$  By the infinity norm, the maximum value is  $1/(1-\gamma)$ .

$$2\gamma^i/(1-\gamma)^2 \le \epsilon \tag{2}$$

Then we add and subtract 1

$$2(1 - (1 - \gamma))^{i} / (1 - \gamma)^{2} \le \epsilon \tag{3}$$

Then we substitute  $-(1-\gamma)$  with  $e^-(1-\gamma)^2$  because it makes solving it easier even if it makes the approximation less accurate

$$2e^{-(1-\gamma)i}/(1-\gamma)^2 \le \epsilon \tag{4}$$

Then we divide by 2 and multiply by  $(1 - \gamma)^2$  and get

$$e^{-(1-\gamma)i} \le (1-\gamma)^2/2$$
 (5)

Then we take the log of both sides

$$-i(1-\gamma) \le -\log(2/(\epsilon(1-\gamma)^2)) \tag{6}$$

In the end we divide by  $-(1-\gamma)$  (so changing also the  $\leq$  in  $\geq$ )

$$i \ge \log(2/(\epsilon(1-\gamma)^2))/(1-\gamma) \tag{7}$$

#### Problem 2

MDP

S1, ..., S7 r(S,a) 
$$\left\{ \begin{array}{c} 1/2S = S_1 5S = S_7 0 otherwhise \end{array} \right. \tag{8}$$
 
$$P(S_6|S_6,a_1) = 0.3 P(S_7|S_6,a_1) = 0.7$$
 
$$\pi(s) = a_1 \forall sv^1 = [0.5,0,0,0,0,0,5] \gamma = 0.9$$
 We calculate the discounted reward from S\_6 and additto the current reward of s\_6 to get the value of s\_6 V(S\_6) = r(S\_6) + \gamma(V(S')) = \\ = 0 + 0.9(P(S\_6|S\_6,a\_1)V(S\_6) + P(S\_7|S\_6,a\_1)V(S\_7)) = 0.9(0.3\*0 + 0.7\*5) = \\ 0.9\*3.5 = 3.15

## Code

#### Policy iteration

To implement the reward function I used an if to check if i was in the goal state and return 1 and an else to return 0 in all other cases

To check if the transition was feasibile I used a couple of ifs, one to check if it was trying to go out of the grid and the second to check if it's going against an obstacle

To return the transition probability i first checked if the transition was feasibile and then I assigned 1/3 to each transition (if the transition isn't feasibile with the action it would would just remain the state it was)

# $\mathbf{iLQR}$

for iLQR i just implemented the formulas being careful about which operator i was using between \* and @.