

$$T(m) = 2T(m/2) + m; \quad T(1) = 1$$

$$\therefore T(m/2) \rightarrow T(m) = 2(2T(m/4) + m/2) + m$$

$$T(m) = 4T(m/4) + 2m + m$$

$$T(m) = 4T(m/4) + 3m$$

$$\therefore T(m/4) \rightarrow T(m) = 4(2T(m/8) + m/4) + 3m$$

$$T(m) = 8T(m/8) + 7m$$

\vdots

$$T(m) = 2^k T\left(\frac{m}{2^k}\right) + (2^k - 1)m$$

Para k : $\frac{m}{2^k} = 1 \rightarrow 2^k = m \rightarrow k = \log_2(m)$

Reemplazo:

$$2^{\log_2(m)} T\left(\frac{m}{2^{\log_2(m)}}\right) + (2^{\log_2(m)} - 1)m$$

$$T(m) = m \cdot T(1) + m \log_2 m = m \log_2 m + m$$

$$T(m) = m + m \log_2(m)$$

$$T(m) = O(m \log(m))$$