

# PROJECT PROPOSAL :

## Optimization using Neural Networks

In this project, we want to approximate the result of a minimization problem using a neural network (NN). Our problem  $P(\cdot)$  is composed of a linear objective with linear and box constraints:

$$P(\mathbf{b}, \mathbf{d}, c) = \left[ \min_{\phi} [\phi^T \mathbf{d}] \quad \text{subject to} \quad \begin{cases} 0 \leq \phi \leq 1 \\ \phi^T \mathbf{b} = c \end{cases} \right], \quad (1)$$

where  $\phi, \mathbf{b}, \mathbf{d} \in \mathbb{R}^5$ ,  $c \in \mathbb{R}$ , and then,  $P : \mathbb{R}^{11} \rightarrow \mathbb{R}$ . We define the subset  $\mathcal{A} \subset \mathbb{R}^{11}$  as the set where the values of  $\mathbf{b}, \mathbf{d}$ , and  $c$  can exist.

We want to find an approximate function  $\tilde{P}(\cdot)$  such that

$$\|P - \tilde{P}\|_{L^\infty(\mathcal{A})} \leq C,$$

where  $C$  is an arbitrary positive constant, the idea is that evaluate  $\tilde{P}(\cdot)$  is faster than evaluate the original function  $P(\cdot)$ .

### Suggested approximation

The function  $\tilde{P}(\cdot)$  can be a trained NN using real solutions of (1).

### Suggested literature and tutorials

1. <https://scikit-learn.org/stable/>. It has tutorials, and it is suitable for standard NN.
2. <https://pytorch.org/>. It is useful if you want to design your architecture or to play with loss functions.
3. <https://www.fast.ai/>. It is more practical and friendly for people not familiar with math.

These links were suggested by a Ph.D. student researching AI during an AI summer school (<http://acai2019.tuc.gr/>).

## About the data

The data is in Matlab format, and they are cells. Each file has a cell with dimensions  $1 \times 225$ . Each one of these cells has inside a  $1 \times 5$  cell with 5 arrays. The arrays have dimensions 12, 1, 12, 1, and 1, respectively. These 5 arrays represent a single data point, where the first 4 arrays are the input, and the 5-th array is the output.