

# Main Results

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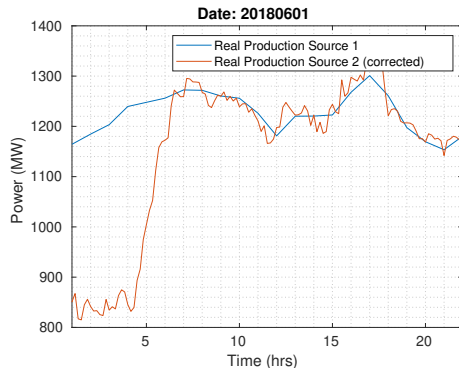
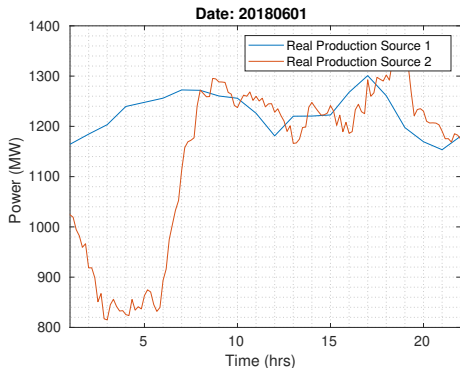
April 13, 2020

The rest can be found in: **Summary of Advances and Questions.**

About the data:

## Curtailing and Delay:

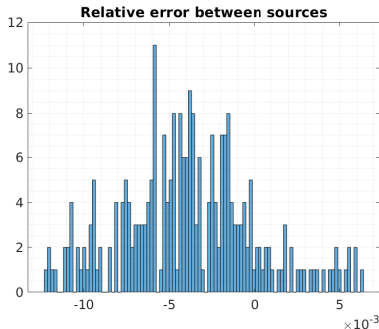
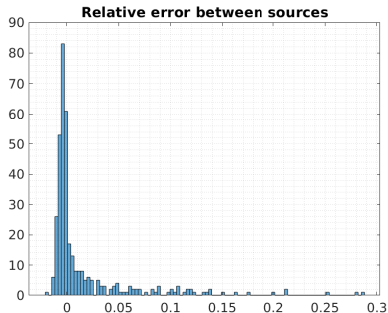
Files: **curt\_and\_error.eps** and **curt\_and\_error\_corr.eps** (dataConditioner.m, cell (2)).



Source 1 has the correct timing; source 2 shows the curtailing and has more frequency. From both sources, we can choose and construct an accurate real production for each day.

## Curtailing histograms:

Files: **all2019.eps** and **partially2019.eps** (dataConditioner.m, cell (8)).

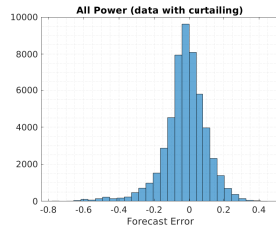
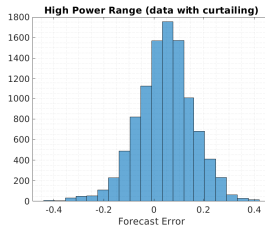
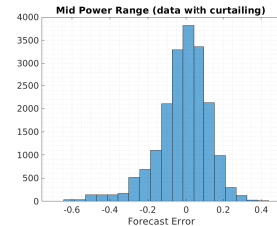
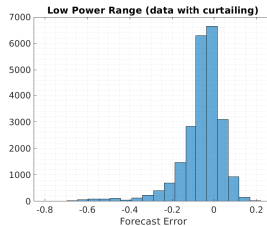


Histograms for the daily mean relative error. On the left, the 365 days. On the right, the corrected data (removed the days with curtailing or other errors).

# Error histograms WITH curtailing:

Files: **LP\_6.eps**, **MP\_6.eps**,  
**HP\_6.eps**, and **AP\_6.eps**  
(dataConditioner.m, cell (12)).

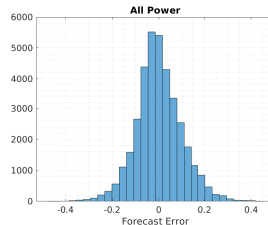
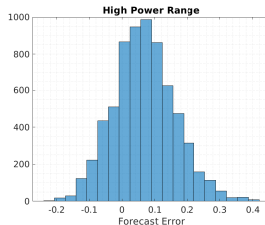
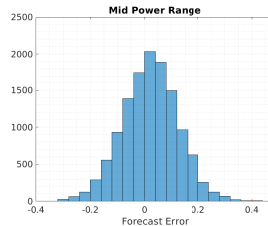
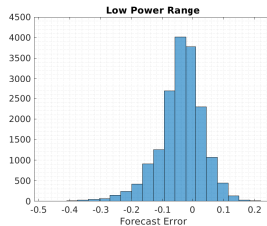
Forecast error for different values of  
the real production.  $LP = [0, 0.3)$ ,  
 $MP = [0.3, 0.6)$ , and  $HP = [0.6, 1]$ .  
We have also a histogram for all  
values of power.



# Error histograms WITHOUT curtailing:

Files: **LP.eps**, **MP.eps**, **HP.eps**, and **AP.eps** (dataConditioner.m, cell (11)).

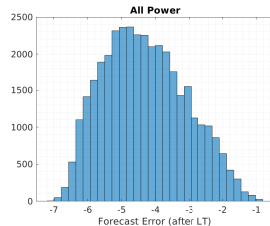
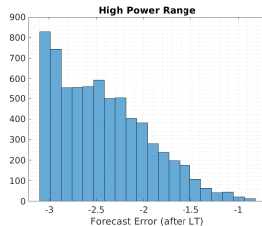
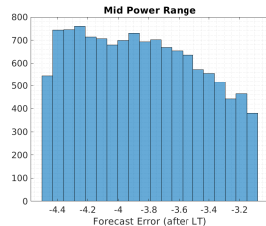
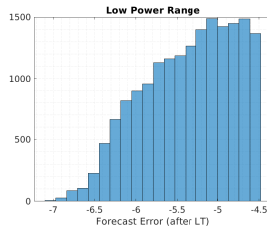
Forecast error after cleaning the data for different values of the real production.  $LP = [0, 0.3)$ ,  $MP = [0.3, 0.6)$ , and  $HP = [0.6, 1]$ . We have also a histogram for all values of power.



# Lamperti histograms WITHOUT curtailing:

Files: **LP\_LP.eps**, **MP\_LP.eps**,  
**HP\_LP.eps**, and **AP\_LP.eps**  
(dataConditioner.m, cell (11)).

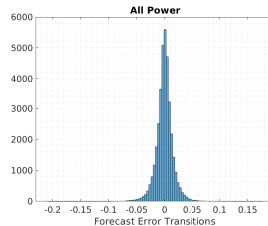
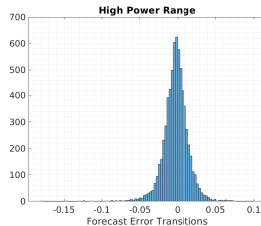
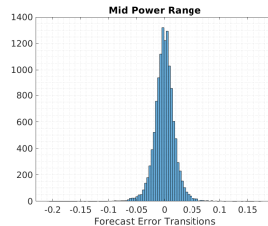
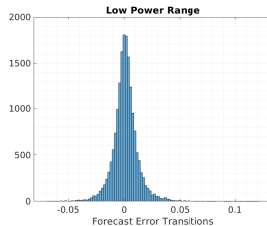
Lamperti after cleaning the data for  
different values of the real  
production.  $LP = [0, 0.3)$ ,  
 $MP = [0.3, 0.6)$ , and  $HP = [0.6, 1]$ .  
We have also a histogram for all  
values of power.



# Error transitions histograms WITHOUT curtailing:

Files: **LP\_t.eps**, **MP\_t.eps**,  
**HP\_t.eps**, and **AP\_t.eps**  
(dataConditioner.m, cell (11)).

Forecast error transitions after  
cleaning the data for different values  
of the real production.  $LP = [0, 0.3)$ ,  
 $MP = [0.3, 0.6)$ , and  $HP = [0.6, 1]$ .  
We have also a histogram for all  
values of power.



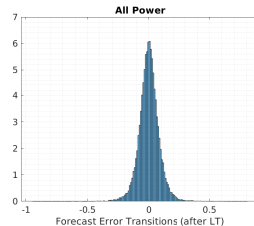
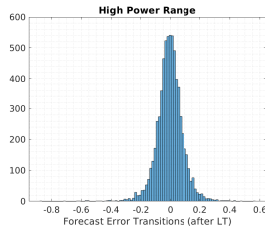
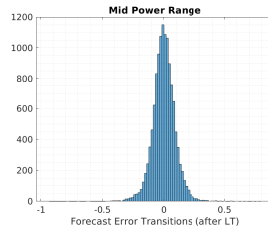
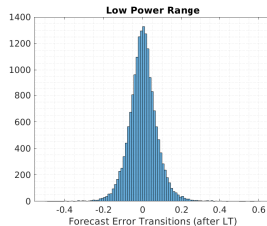


# Lamperti error transitions histograms WITHOUT curtailing:

Files: **LP\_t\_LP.eps**, **MP\_t\_LP.eps**,  
**HP\_t\_LP.eps**, and **AP\_t\_LP.eps**  
(dataConditioner.m, cell (11)).

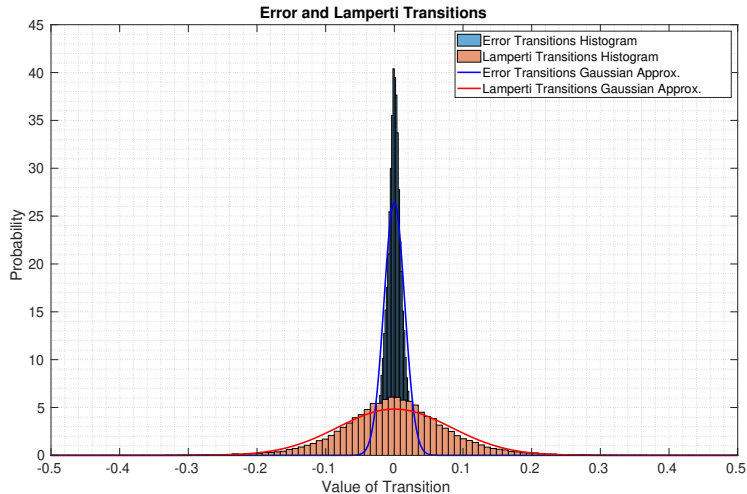
Lamperti error transitions after  
cleaning the data for different values  
of the real production.  $LP = [0, 0.3)$ ,  
 $MP = [0.3, 0.6)$ , and  $HP = [0.6, 1]$ .  
We have also a histogram for all  
values of power.

We transformed using the initial  
guesses.



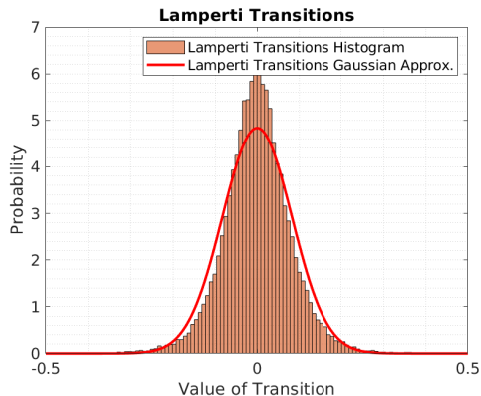
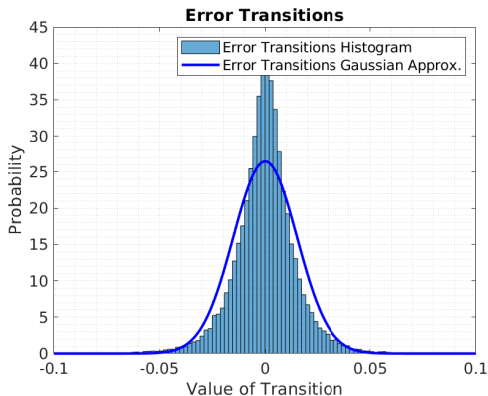
## Gaussian approximation for the transitions:

Files: **Gauss\_Approx.eps** (dataConditioner.m, cell (11)).



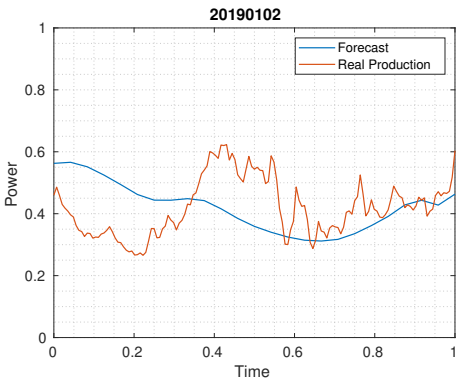
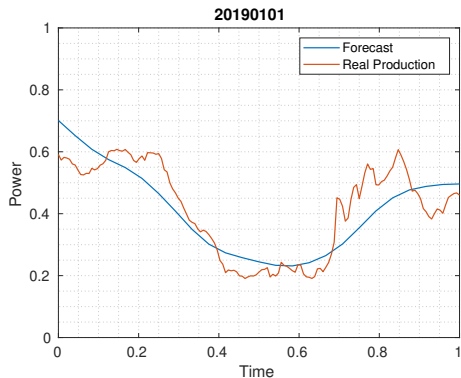
## Gaussian approximation for the transitions:

Files: **Gauss\_Approx\_Err.eps**, and **Gauss\_Approx\_Lam.eps** (dataConditioner.m, cell (11)).



## Forecast and production:

Files: **allDaysPlots/1.eps**, and **allDaysPlots/2.eps** (dataConditioner.m, cell (11)).

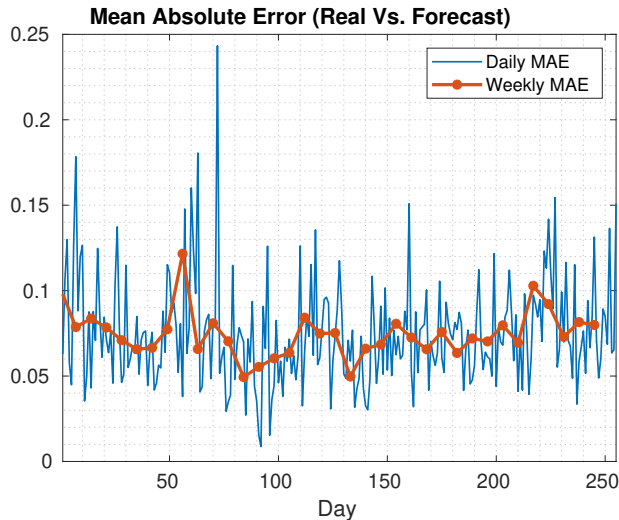


We have this forecast and production plots for the 255 days.

## Seasonality effect:

Files: **seasons.eps**  
(dataConditioner.m, cell (11)).

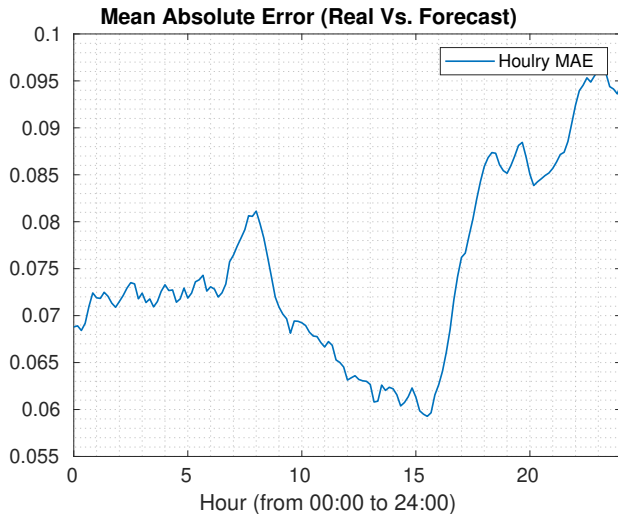
Daily and weakly mean absolute error between the forecast and the real production. We can see no significant seasonality effect.



## Hourly effect:

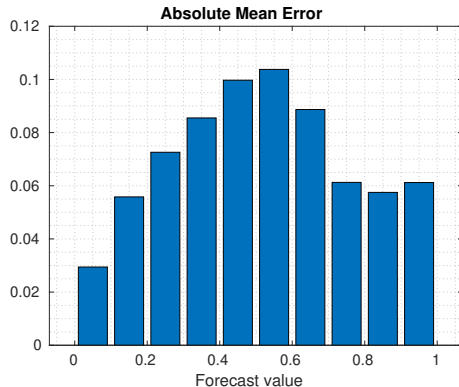
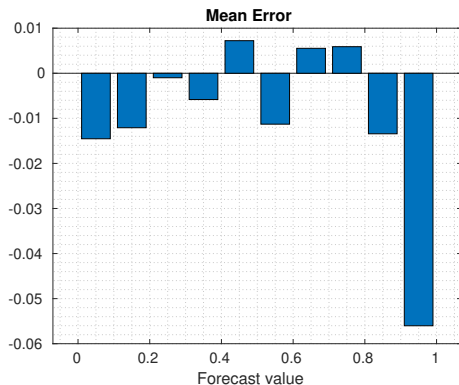
Files: **hourlyEffect.eps**  
(dataConditioner.m, cell (11)).

Hourly mean absolute error between the forecast and the real production. We can see a significant reduction in the error during the day.



## ME and AME for different intervals of forecast:

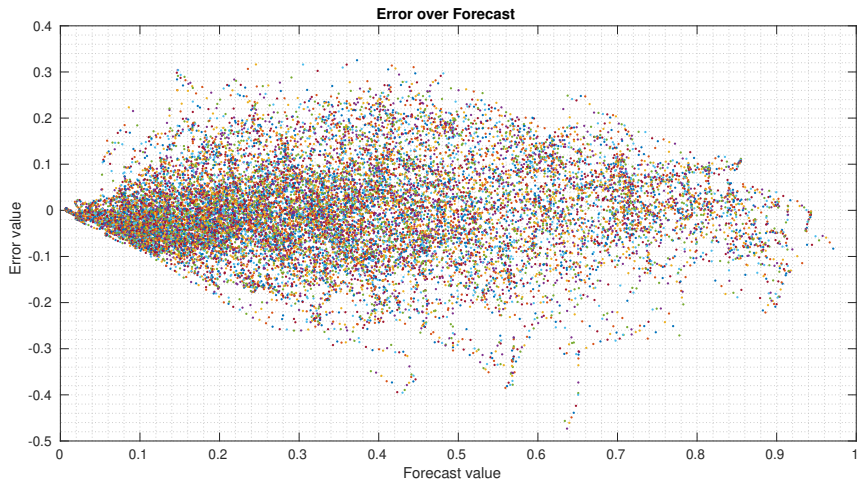
Files: `mean_error.eps` and `mean_abs_error.eps` (erroVsForecast.m).



What we are seeing is the **mean error** and **mean absolute error** as a function of the forecast. This is, for each interval with length 0.1 (i.e.,  $[0,0.1)$ ,  $[0.1,0.2)$ , etc.), we average all the errors corresponding to measurement where the forecast was in that intervals, and after we average over the number of elements in each interval.

## Error Vs. Forecast for all training days (scatter plot):

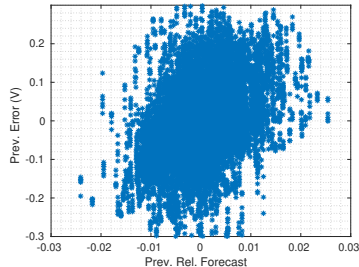
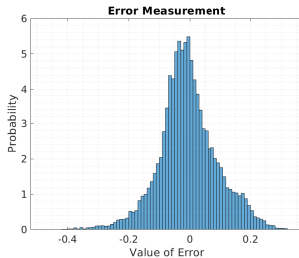
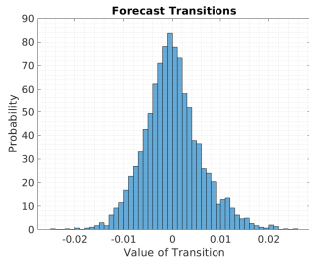
Files: **error\_over\_forecast.eps** (erroVsForecast.m).





## Forecast and error histograms:

Files: **MATLAB\_Files/Results/histograms/others** (some\_histograms.m).



From here we can see that the errors are approximately in the interval  $[-0.3, 0.3]$ , and the forecast transitions in the interval  $[-0.03, 0.03]$ .

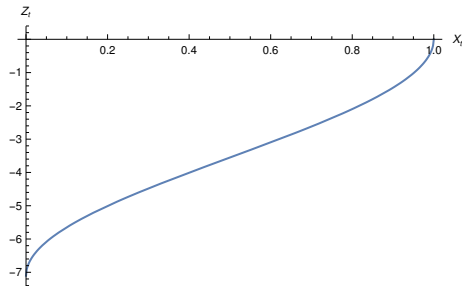
Then, we want to ensure that the moments are well approximated in the rectangle  $[-0.3, 0.3] \times [-0.03, 0.03]$  (for  $V \times \Delta p$ ).

# Simulations and Results:

## Lamperti transform plot:

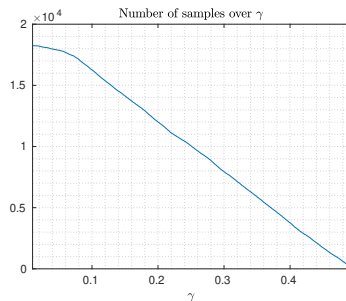
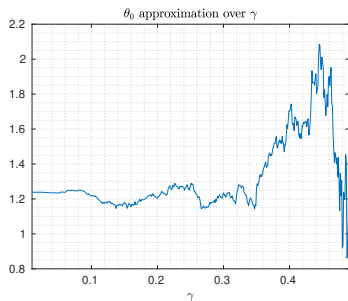
Files: **Mathematica\_Files/Range\_Z.pdf**  
(Range\_Z.nb).

Plot of  $Z_t$  as a function of  $X_t$  from 0 to 1. We choose  $\alpha = 0.06$ , and  $\theta_t = 1.63$  (initial guess).



## Estimation of $(\theta_0, \alpha, \varepsilon)$ : $\theta_0^*$ using LSM over different sets

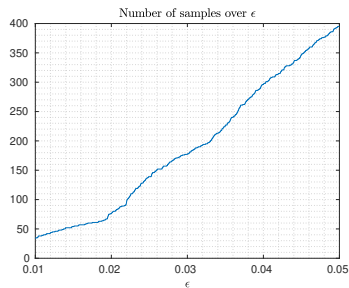
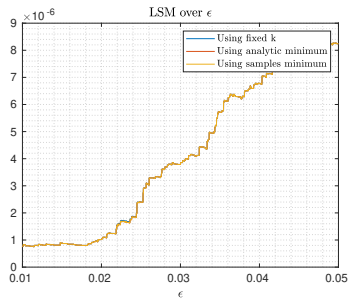
Files: **MATLAB\_Files/Results/epsilon: theta\_0.eps** and **num\_over\_eps\_t0.eps** (plot\_epsilon.m, third cell).



On the right, the number of samples as a function of  $\gamma$ . This samples satisfies that  $p_i \in [\gamma, 1 - \gamma]$ . On the left, the LSM over the samples that satisfies the  $\gamma$  condition.

## Estimation of $(\theta_0, \alpha, \varepsilon)$ : $\varepsilon$ using LSM over different sets

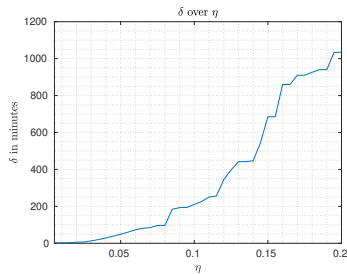
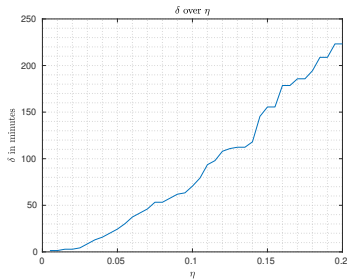
Files: **MATLAB\_Files/Results/epsilon: LSM.eps** and **num\_over\_eps.eps** (plot\_epsilon.m, second cell).



On the right, the number of samples as a function of  $\varepsilon$ . This samples satisfies that  $p_i^\varepsilon \in \{\varepsilon, 1 - \varepsilon\}$ . On the left, the LSM for  $\varepsilon$ , over the samples that satisfies the  $\varepsilon$  condition.

$\delta$  over  $\eta$ :

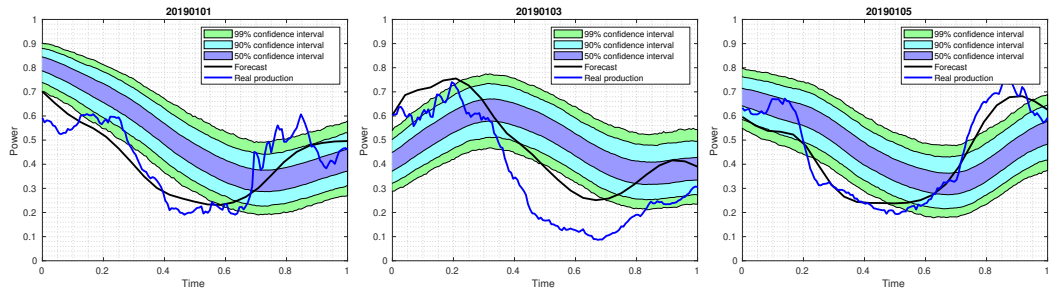
Files: **MATLAB\_Files/Results/delta: eta\_min\_ini.eps** and **eta\_min\_opt.eps** (initiasl\_time.m, second cell).



We use the initial transitions that satisfies  $|\Delta V| < \eta$ . On the left, we use the initial  $(\theta_0, \alpha)$  ( $\alpha\theta_0 = 0.098$ ) and we get  $\delta = 220$  min. On the right, we use the optimal ones. As the optimal product  $\alpha\theta_0$  ( $\alpha\theta_0 = 0.083$ ) is smaller than the initial one, we need either a larger  $\delta$  to match the variance of the initial error, or to remove some data.

# Probability bands for model with delay:

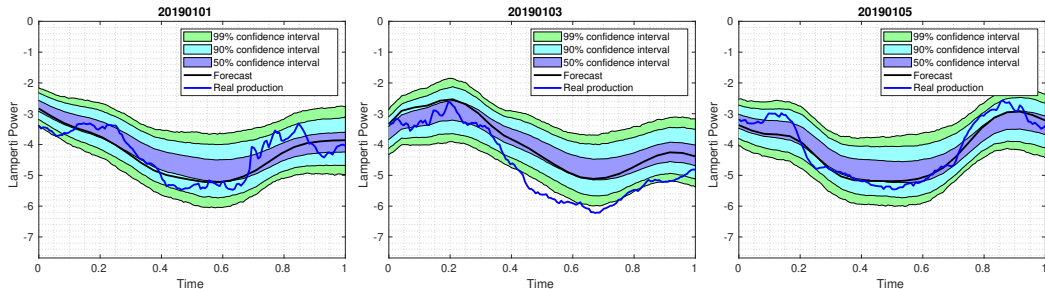
Files: **MATLAB\_Files/Results/bands\_testing\_days/model\_1**  
(path\_simulator\_OPT\_model\_1.m).



We used the optimal parameters of the error SDE. We have results for the 128 testing days.

# Probability bands for Lamperti:

Files: **MATLAB\_Files/Results/bands\_testing\_days/lamperti\_optimal**  
(path\_simulator\_Lamperti.m).

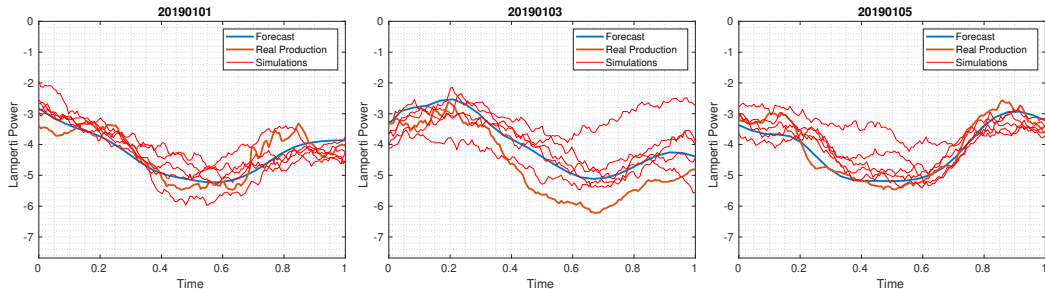


We used the Lamperti optimal parameters to simulate the Lamperti SDE. We have results for the 128 testing days.



# Paths for Lamperti:

Files: **MATLAB\_Files/Results/paths\_testing\_days/lamperti\_optimal**  
(path\_simulator\_Lamperti.m).



We used the Lamperti optimal parameters to simulate the Lamperti SDE. We have results for the 128 testing days.