



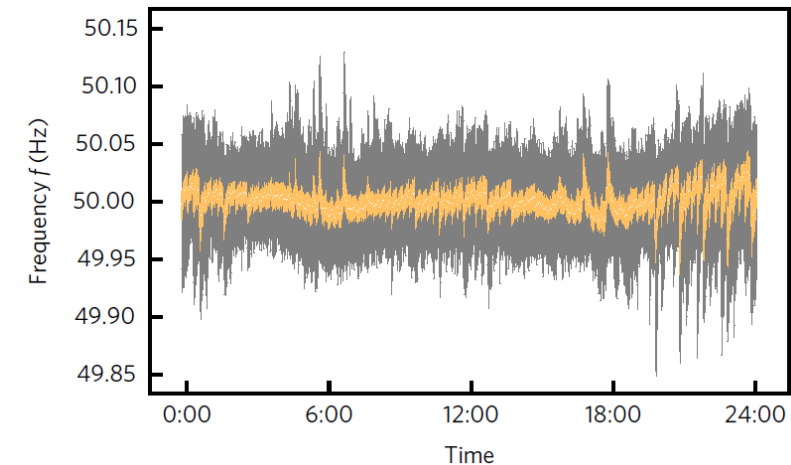
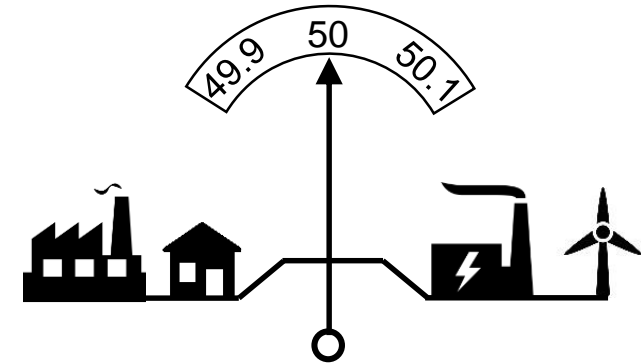
# STOCHASTIC DYNAMICS OF POWER SYSTEMS OVERVIEW FOR R. TEMPONE AND E. HALL

19.2.2019 | DIRK WITTHAUT

# FREQUENCY DYNAMICS IN POWER SYSTEMS

## Why study power system frequency data?

- The mains frequency is the central observable in power system control: It measures the *power balance* in the grid.
- The frequency is readily measured at any plug (in contrast to power), so data is easy to obtain.
- What can we learn about power system dynamics and stability?

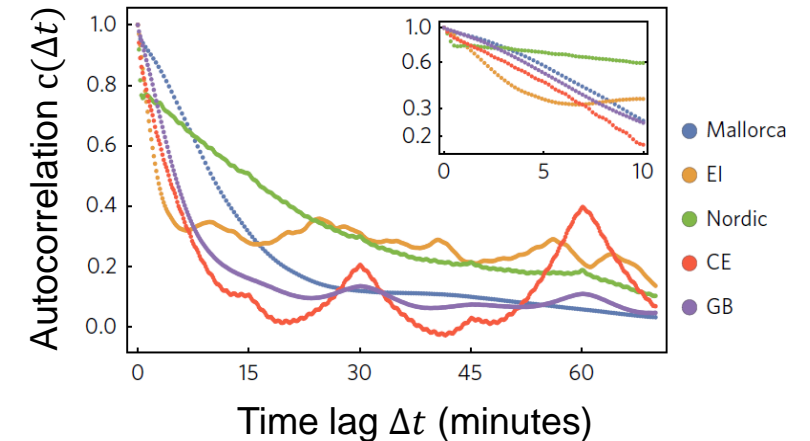
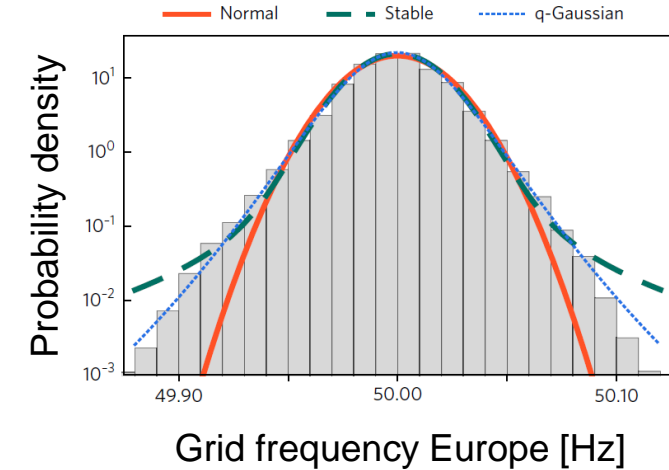


# FREQUENCY DYNAMICS IN POWER SYSTEMS

## Aggregate statistics for frequency time series

A first look at the frequency time series as a whole:

- A histogram of the mains frequency  $f$  reveals *heavy tails* not compatible with Gaussian statistics
- Data is best described by described Levy-stable or  $q$ -Gaussians distributions
- Auto-correlation of time series  $f(t)$  reveals:
  - effective damping  $\gamma$
  - high impact of electricity trading in intervals of 15,30,45,60,... minutes



Schäfer, Beck, Aihara, DW, Timme, Nature Energy 3, 119 (2018)

# FREQUENCY DYNAMICS IN POWER SYSTEMS

## Aggregate statistics for frequency time series

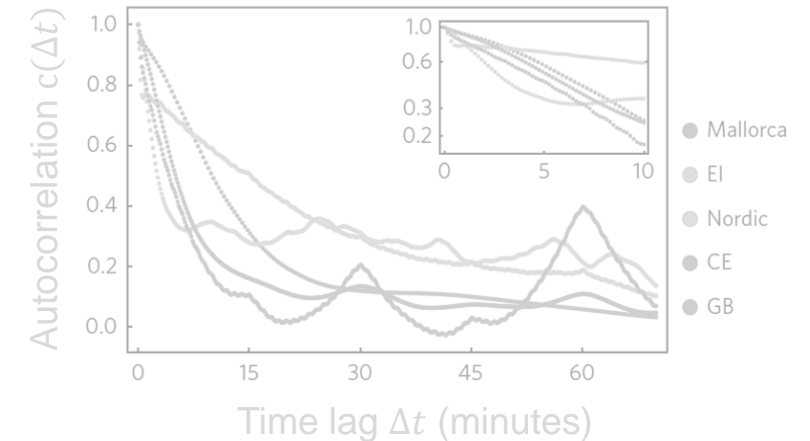
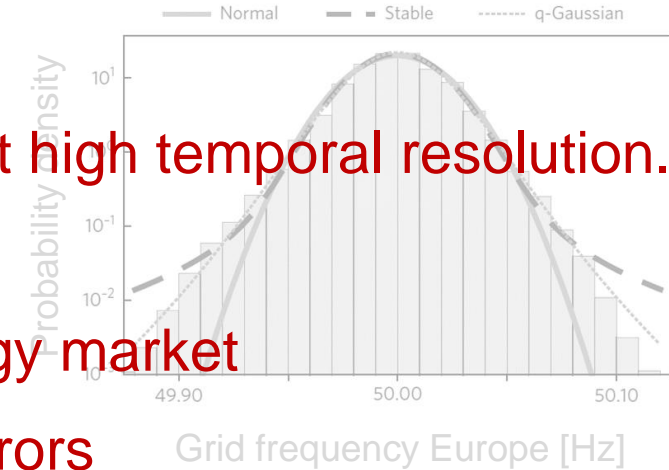
A first look at the frequency time series as a whole:

**We should have a more detailed view on the data at high temporal resolution.**

- A histogram of the mains frequency  $f$  reveals heavy tails not compatible with Gaussian statistics

**Then we might learn a lot about:**

- The scheduling of power generation on the energy market
- Data is best described by described Levy-stable or  $q$ -Gaussians distributions
- The impact of renewables including prognosis errors
- The problem of decreasing grid inertia
- Auto-correlation of time series  $f(t)$  reveals:
  - effective damping  $\gamma$
  - high impact of electricity trading in intervals of 15,30,45,60,... minutes



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# KRAMERS-MOYAL COEFFICIENTS

## Constructing an stochastic model

- Let us assume that the frequency dynamics can be modeled by an SDE:

$$df = a(f, t) dt + b(f, t) dW$$

- Kramers-Moyal coefficients:

$$a(f, t) = \lim_{\Delta t \rightarrow 0} E([f(t + \Delta t) - f(t)] \mid f)$$

$$b(f, t) = \frac{1}{2} \lim_{\Delta t \rightarrow 0} E([f(t + \Delta t) - f(t)]^2 \mid f)$$

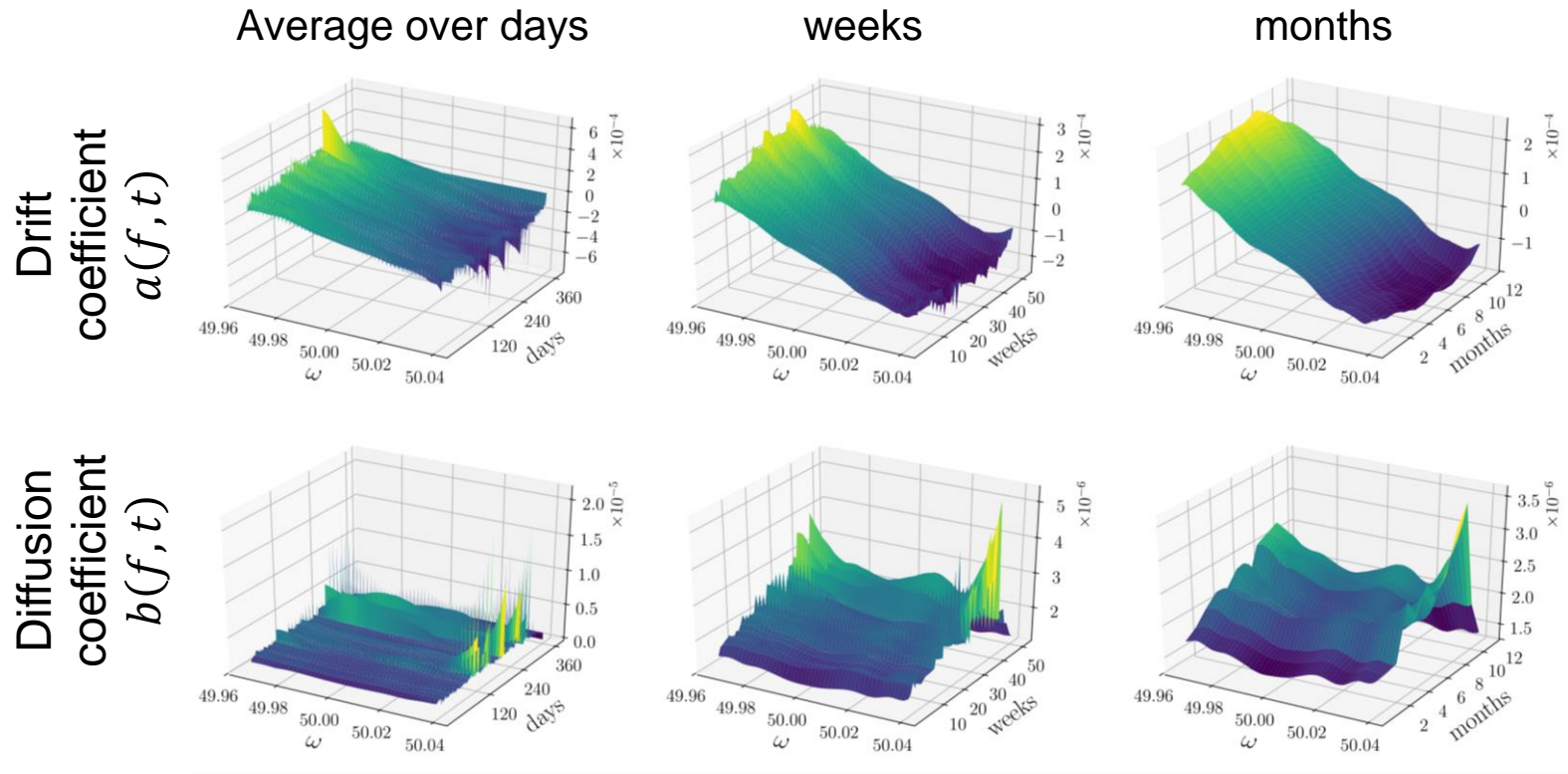
- In practice we cannot take the limit and we do not know the expected value.  
➤ Use a finite  $\Delta t$ , replace expected value  $E$  by time average...



# KRAMERS-MOYAL COEFFICIENTS

## Results for the Central European Power Grid

Results for the Central European Grid 2016:  $df = a(f, t) dt + b(f, t) dW$



This is dominated by primary control:  
 $a(f, t) \approx -\frac{\gamma_2}{M} f$

Higher in summer and for large  $f$ . Why?

# MAXIMUM LIKELIHOOD APPROACH

## Constructing an stochastic model

- The mains frequency just follows the power imbalance in the grid:

$$M df = \Delta P dt, \quad M: \text{inertia}, f: \text{frequency relative to 50 Hz}$$

- We can decompose the power balance  $\Delta P$  into four contributions:

1. Mismatch of the power generation  $\Delta P_{gen}$
2. Rapid, irregular changes of the generation and load  $\rightarrow$  treated as noise  $D dW$
3. Action of primary control:  $\Delta P_1 = -\gamma_1 f \times H(f - 10 \text{ mHz})$
4. Action of secondary control:  $\Delta P_2$

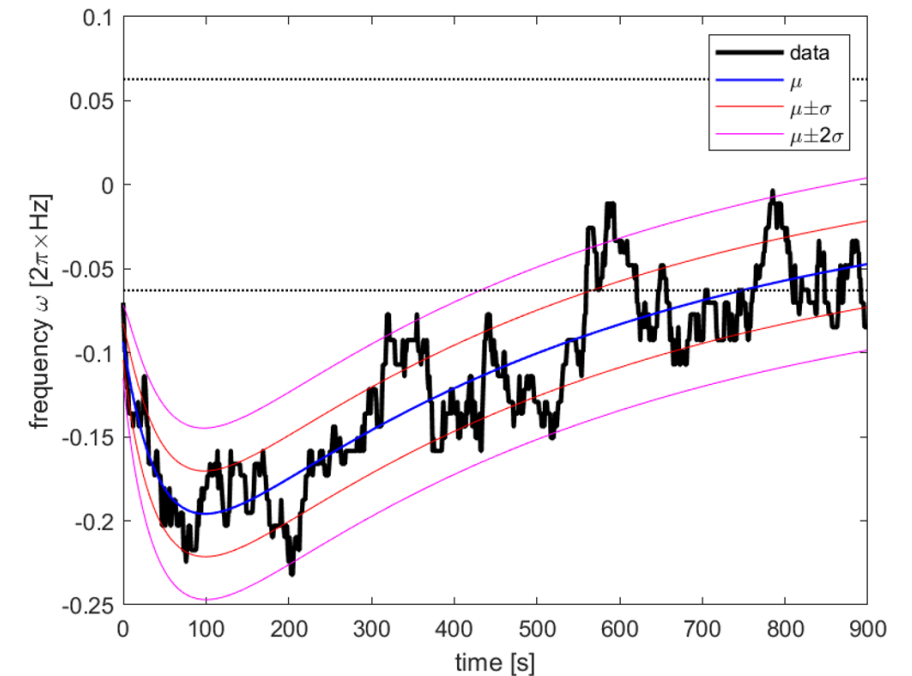
$$\triangleright M df = (\Delta P_{gen} + \Delta P_2) dt - \gamma_1 f \times H(f - 10 \text{ mHz}) dt + D dW$$

- $\triangleright$  Can we recover parameters such as  $\Delta P_{gen}, D, M$  from data?

# MAXIMUM LIKELIHOOD APPROACH

## Results for a simplified model

- A first attempt with some simplifications:
  - Primary control always on:  $\Delta P_1 = -\gamma_1 f$
  - Assume that secondary control brings mismatch to zero at fixed rate:  $\Delta P_{gen} + \Delta P_2 = \Delta P_0 e^{-\gamma_2 t}$
  - Assume a Gaussian distribution at all times
- Fit parameters of model and initial state such that log-likelihood function assumes a maximum
- Results look quite good for the example shown on the right

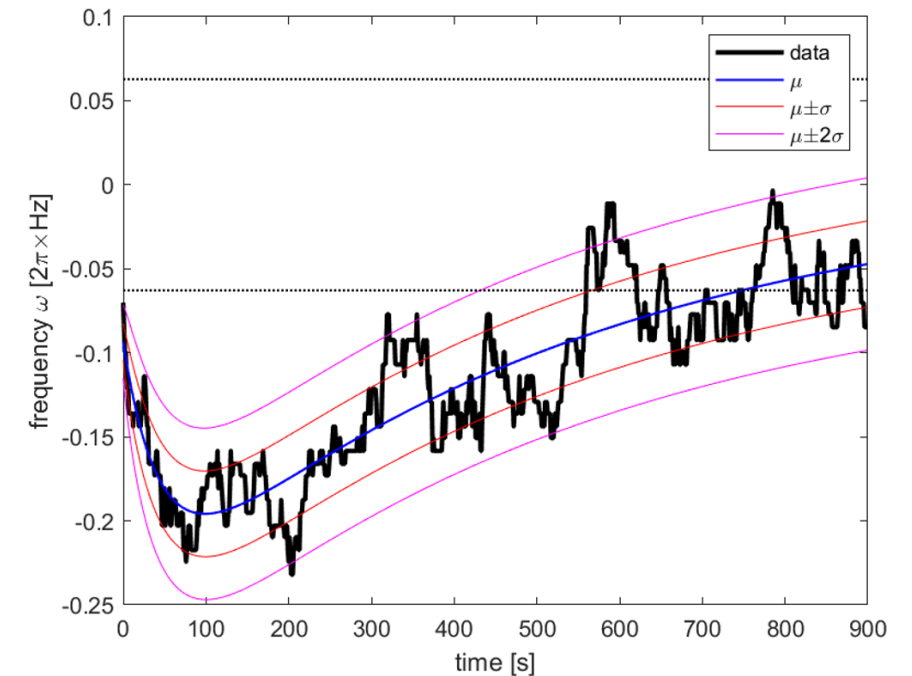




# MAXIMUM LIKELIHOOD APPROACH

## Challenges of the maximum likelihood approach

- Challenge 1: overfitting
- There quite a number of parameters in the model and there will be even more if I include a more adequate model for secondary control.
- For instance, it is hard to disentangle the contributions of the two damping factors  $\gamma_1, \gamma_2$



# MAXIMUM LIKELIHOOD APPROACH

## Challenges of the maximum likelihood approach

- Challenge 2: dead bands
- Let's proceed with the same model to the next 15 minute interval
- Result: The results look far worse and the reconstructed parameters are very strange.
- That shows that we cannot assume that primary control is always on. We have to include it explicitly. But then we have to deal with a nasty discontinuous function...

