Analyse I Huiswerk

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1. a)

b)

$$\lim_{x \to -\infty} \sqrt{x^2 + x + 4} + x = \lim_{t \to \infty} \sqrt{t^2 - t + 4} - t$$

$$= \lim_{t \to \infty} \frac{(\sqrt{t^2 - t + 4} - t)(\sqrt{t^2 - t + 4} + t)}{\sqrt{t^2 - t + 4} + t}$$

$$= \lim_{t \to \infty} \frac{\cancel{t^2} - t + 4 - \cancel{t^2}}{\sqrt{t^2 - t + 4} + t}$$

$$= \lim_{t \to \infty} \frac{\frac{-t}{t} + \frac{4}{t}}{\sqrt{\frac{t^2}{t^2} - \frac{t}{t^2} + \frac{4}{t^2}} + \frac{t}{t}}}$$

$$= \frac{-1 + 0}{\sqrt{1 + 0 + 0} + 1} = \boxed{-\frac{1}{2}}$$