Monty Hall Constraints

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Parse results after processing KLEE dump for Monty Hall Example.

```
Path: 1
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         !((!(car_door_sym == 2) && !(choice_pse_var_sym == 2)))
         !(!(door_switch_pse_var_sym == 0))
Path: 2
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car door sym <= 3
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         (!(car_door_sym == 2) && !(choice_pse_var_sym == 2))
         !(door_switch_pse_var_sym == 0)
         !(choice_pse_var_sym == 1)
Path: 3
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         !((!(car_door_sym == 2) && !(choice_pse_var_sym == 2)))
         !(door_switch_pse_var_sym == 0)
```

```
choice_pse_var_sym == 1
Path: 4
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car door sym <= 3
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         !((!(car_door_sym == 2) && !(choice_pse_var_sym == 2)))
         !(door_switch_pse_var_sym == 0)
         !(choice_pse_var_sym == 1)
Path: 5
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         (!(car_door_sym == 1) && !(choice_pse_var_sym == 1))
         !(!(door_switch_pse_var_sym == 0))
         choice_pse_var_sym == car_door_sym
Path: 6
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         (!(car_door_sym == 1) && !(choice_pse_var_sym == 1))
         !(!(door_switch_pse_var_sym == 0))
         !(choice_pse_var_sym == car_door_sym)
Path: 7
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car door sym <= 3
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         (!(car_door_sym == 2) && !(choice_pse_var_sym == 2))
         !(!(door_switch_pse_var_sym == 0))
```

```
choice_pse_var_sym == car_door_sym
Path: 8
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car door sym <= 3
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         (!(car_door_sym == 2) && !(choice_pse_var_sym == 2))
         !(!(door_switch_pse_var_sym == 0))
         !(choice_pse_var_sym == car_door_sym)
Path: 9
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         (!(car_door_sym == 1) && !(choice_pse_var_sym == 1))
         !(door_switch_pse_var_sym == 0)
         !(choice_pse_var_sym == 2)
         car_door_sym == 2
Path: 10
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car door sym <= 3
         (!(car_door_sym == 1) && !(choice_pse_var_sym == 1))
         !(door_switch_pse_var_sym == 0)
         !(choice_pse_var_sym == 2)
         !(car_door_sym == 2)
Path: 11
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         (!(car_door_sym == 1) && !(choice_pse_var_sym == 1))
```

```
!(door_switch_pse_var_sym == 0)
         choice_pse_var_sym == 2
         car_door_sym == 3
Path: 12
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         (!(car_door_sym == 1) && !(choice_pse_var_sym == 1))
         !(door_switch_pse_var_sym == 0)
         choice pse var sym == 2
         !(car_door_sym == 3)
Path: 13
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice_pse_var_sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         (!(car_door_sym == 2) && !(choice_pse_var_sym == 2))
         !(door_switch_pse_var_sym == 0)
         choice_pse_var_sym == 1
         car_door_sym == 3
Path: 14
         0 <= door_switch_pse_var_sym</pre>
         door_switch_pse_var_sym <= 1</pre>
         0 <= choice pse var sym</pre>
         choice_pse_var_sym <= 3</pre>
         0 <= car_door_sym</pre>
         car_door_sym <= 3</pre>
         !((!(car_door_sym == 1) && !(choice_pse_var_sym == 1)))
         (!(car_door_sym == 2) && !(choice_pse_var_sym == 2))
         !(door_switch_pse_var_sym == 0)
         choice_pse_var_sym == 1
         !(car_door_sym == 3)
```

We present the observations for the Monty Hall.

```
- For door_switch == 0
        (P(win) >= 0.5) passes,
- For door_switch == 1
        (P(win) >= 0.5) fails,
- When count(door_switch == 0) == count(door_switch == 1)
        (P(win) \le 0.5) fails
        (P(win) >= 0.5) passes.
- When ever count(door_switch == 0) < count(door_switch == 1) with bias
               Higher probability of winning when the person switches.
                       (P(win) <= 0.5) fails :
       Fail : P(choice == car_door) : 0.860216
       Fail : P(choice == car_door) : 0.520136
       Fail : P(choice == car_door) : 0.780963
- When ever count(door_switch == 0) > count(door_switch == 1) with bias
               (P(win) >= 0.5) fails :
       Fail : P(choice == car_door) : 0.499620
       Fail : P(choice == car_door) : 0.379960
       Fail : P(choice == car_door) : 0.139769
```