

Q1. A diffraction grating used at normal incidence gives a yellow line ($\lambda = 6000 \text{ \AA}$) in a certain spectral order superimposed on a blue line ($\lambda = 4800 \text{ \AA}$) of next higher order. If the angle of diffraction is $\sin^{-1}(3/4)$ calculate the grating element.

Given:- $\lambda_1 = 6000 \text{ \AA} = 6 \times 10^{-5} \text{ cm}$; $\lambda_2 = 4800 \text{ \AA} = 4.8 \times 10^{-5} \text{ cm}$; $\theta = \sin^{-1}\left(\frac{3}{4}\right)$

Formula:- $(a + b)\sin \theta = n \lambda$; $n = 1, 2, 3, 4, \dots$

Solution:- for given $(a + b)$ and θ ; $n \propto 1/\lambda$

$$(a + b)\sin \theta = n \lambda_1$$

$$(a + b)\sin \theta = (n + 1) \lambda_2$$

$$n \lambda_1 = (n + 1) \lambda_2$$

$$\frac{\lambda_1}{\lambda_2} = 1 + \frac{1}{n}$$

Therefore, $n = 4$

$$(a + b) = \frac{n \lambda_1}{\sin \theta} = \frac{4 \times 6 \times 10^{-5}}{\frac{3}{4}} = 32 \times 10^{-5} \text{ cm}$$

Ans:- The grating element is $3.2 \times 10^{-4} \text{ cm}$.