

()

[]

> restart:

with(plots):

VALUE

SetkaRavnomer:=proc(leftValue, rightValue, nValue)

local i, shagValue, Value:

VALUE

shagValue:=evalf((rightValue-leftValue)/nValue):

Value[1]:=leftValue:

for i from 2 to nValue do

Value[i] :=Value[i-1]+shagValue:

end do:

Value[nValue+1]:=rightValue;

[seq(Value[k], k=1..nValue+1)]

end proc:

ExactMeshSolution:=proc(T, l, L, a2, b2, c2, c_x21, c_x22,
Nx, Nt)

local odeXdrob, solXdrob, solTdrob, generalsoldrob,
show, subsolution, SetkaX:

local SetkaT, initialData, q1, q2, leftBound,
rightBound, q3, q4, j, i, NaSetkeFractDerivSol:

#

odeXdrob := diff(A2*diff(m2(x), x),x)/m2(x) = C2:

solXdrob := dsolve(odeXdrob, m2(x)):

solTdrob := n2(t)=Sum(t^k/GAMMA(b2*(k+1)), k=0..infinity):

generalsoldrob := subs(A2=a2, C2=c2, _C1=c_x21,

_C2=c_x22, evalf(subs(solXdrob, solTdrob, n2(t)*m2(x)))):

printf("

()

");

show:=p2=solXdrob;

print(show):

subsolution := subs(Sum=add, infinity=12,

generalsoldrob):

printf("

"

);

subsolution := evalf(subsolution):

print(subsolution):

#

SetkaX := SetkaRavnomer(l, L, Nx):

SetkaT := SetkaRavnomer(0, T, Nt):

for j from 1 to Nt+1 do:

for i from 1 to Nx+1 do:

NaSetkeFractDerivSol[j, i] :=

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evalf(subs(t=SetkaT[j], x=SetkaX[i], subsolution)):
      od:
    od:
    [NaSetkeFractDerivSol, subsolution]:
end proc:

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> #
T := 1: # , < 1
l := 0.01: #
L := 1: #
#
Nx := 1000: # - 1
Nt := 10: # - 1
SetkaX:= SetkaRavnomer(1, L, Nx):
SetkaT:=SetkaRavnomer(0, T, Nt):

#
a2 := 0.5: #
b2 := 0.5: #
#
c2 := 5: #
c_x21 := -0.01: #
c_x22 := 10: #
# 2 2

ForHelp := ExactMeshSolution(T, l, L, a2, b2, c2, c_x21,
c_x22, Nx, Nt):
NaSetkeFractDerivSol := evalf(ForHelp[1]):
PartSolution := 'PartSolution':
PartSolution := ForHelp[2]:
PartSolution;

#
#
InitialData := subs(t=0, PartSolution):
#
LeftBound := subs(x=l, PartSolution):
RightBound := subs(x=L, PartSolution):

printf(" ");
plot([LeftBound, RightBound], t=0..T, labels=["t", "p(t, x)"],
labelfont = ["HELVETICA", 15],
legend = [ " ", " " ], legendstyle =
[font = ["HELVETICA", 15], location = right], thickness = 3,
axesfont=["HELVETICA",10]);
plot([InitialData, subs(t=T, PartSolution)], x=l..L, labels=
["x", "p(t, x)"], labelfont = ["HELVETICA", 15],
legend = [ " ", " " ],
legendstyle = [font = ["HELVETICA", 15], location = right],
thickness = 3, axesfont=["HELVETICA",10]);

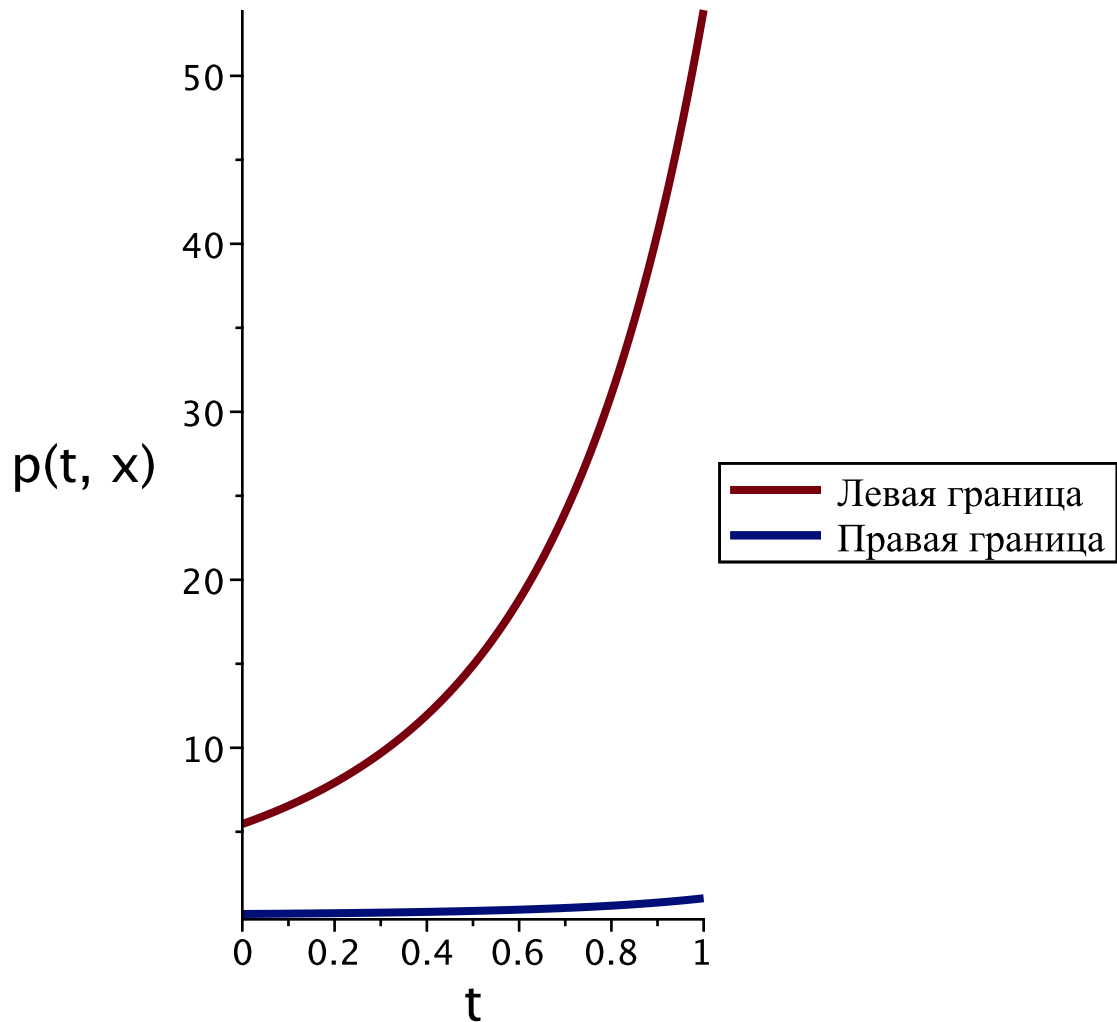
```

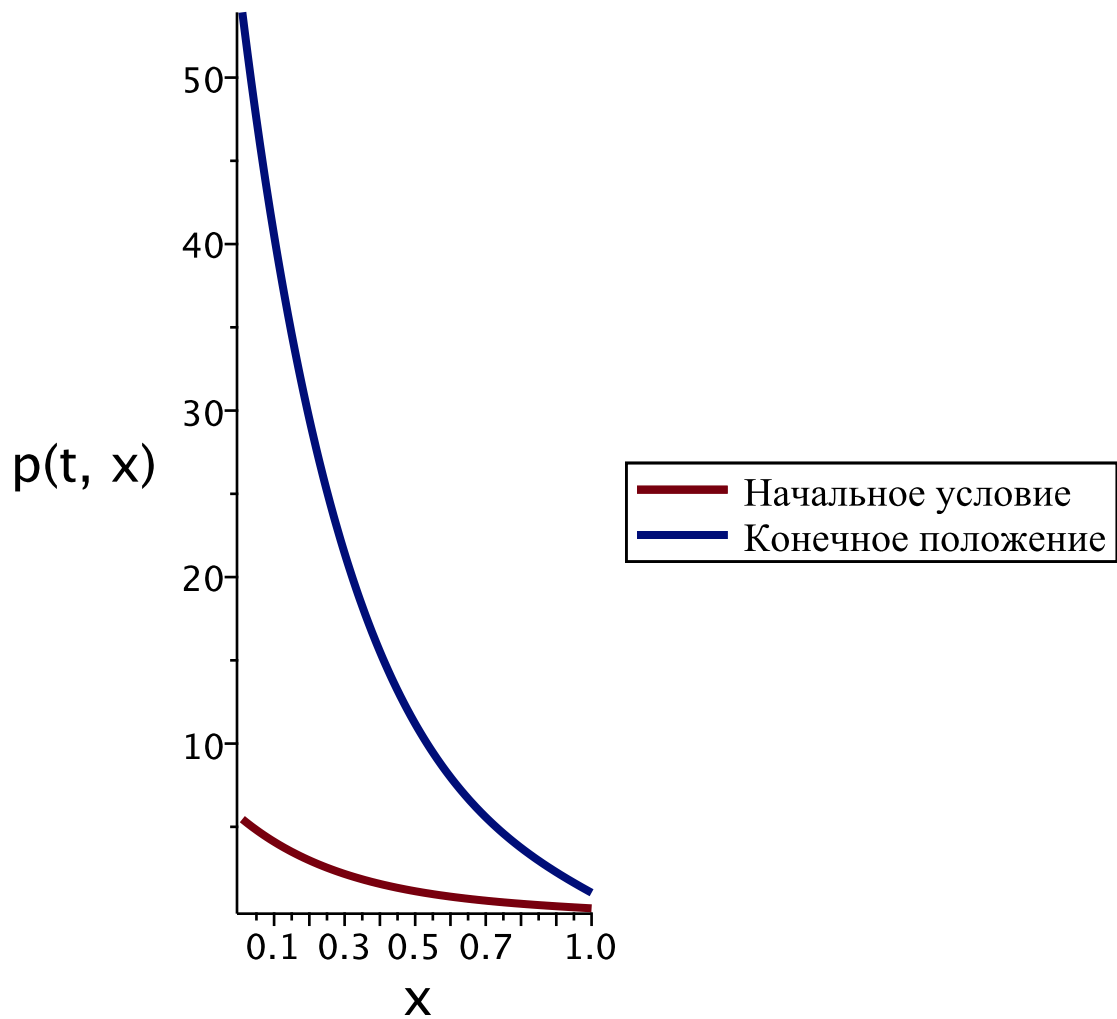
()

$$p2 = \left(m2(x) = _C1 e^{\frac{\sqrt{C2} x}{\sqrt{A2}}} + _C2 e^{-\frac{\sqrt{C2} x}{\sqrt{A2}}} \right)$$

$$add\left(\frac{t^k}{\Gamma(0.5 k + 0.5)}, k=0..12\right) (-0.01 e^{3.162277659 x} + 10. e^{-3.162277659 x})$$

$$(0.5641895835 + t + 1.128379167 t^2 + t^3 + 0.7522527782 t^4 + 0.5000000000 t^5 + 0.3009011113 t^6 + 0.1666666667 t^7 + 0.08597174604 t^8 + 0.04166666667 t^9 + 0.01910483246 t^{10} + 0.008333333333 t^{11} + 0.003473605902 t^{12}) (-0.01 e^{3.162277659 x} + 10. e^{-3.162277659 x})$$





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> #-----  
#-----  
#-----  
#-----  
#-----  
  
solverOsred:=proc(stepPerm, coefPerm, stepPoros, coefPoros,  
l, L, pl0, pL0, Kosh, SetkaX, SetkaT)  
    local Kapprox, Mapprox, PDE, IBC, pds, g;  
    local solut, NSetkaX, NSetkaT, shagX, shagT, i, j,  
    U, Ux, kUx, Ut;  
    #option remember:
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# , ,

Kapprox:=(x)^stepPerm*coefPerm:
Mapprox:=(x)^stepPoros*coefPoros:
PDE := Mapprox*diff(u(x, t), t) = diff(Kapprox*diff
(u(x, t),x), x);
IBC := {u(1, t) = pl0, u(x, 0) = Kosh, u(L, t) =
pL0}:
pds := pdsolve(PDE, IBC, numeric, time=t, range=1..
L, compile=true):
pds:-value(output = listprocedure);
solut:=subs(%[3], u(x, t)):
#
NSetkaX:=numelems(SetkaX):
NSetkaT:=numelems(SetkaT):
shagX:=SetkaX[2]-SetkaX[1]:
shagT:=SetkaT[2]-SetkaT[1]:
for i from 1 to NSetkaX do
    for j from 1 to NSetkaT do
        U[i, j]:=solut(SetkaX[i],
SetkaT[j]):
    od:
od:
#subs(x=SetkaX[i], Kapprox)*
for i from 1 to NSetkaX-1 do
    for j from 1 to NSetkaT do
        Ux[i, j]:=(solut(SetkaX[i+1],
SetkaT[j])-solut(SetkaX[i], SetkaT[j]))/shagX:
    od:
od:
if 0=1 then
    #subs(x=SetkaX[i+1], Kapprox)*
    for i from 1 to NSetkaX do
        for j from 1 to NSetkaT-1 do
            Ut[i, j]:=(solut(SetkaX[i],
SetkaT[j+1])-solut(SetkaX[i], SetkaT[j]))/shagT:
        od:
    od:
fi:

[U, Ux, Ut]
end proc:

#
minimizeFun:=proc(Fun)
    local i, j ,NCoef, NStep, dddd, NomerMin:

    NStep:=numelems(Fun):
    NCoef:=numelems(Fun[1]):
    dddd:=Matrix([seq([seq(Fun[i,j,3], i = 1 .. NStep)
], j = 1 .. NCoef)]);
    NomerMin:=min[index](dddd);

    [Fun[NomerMin[2],NomerMin[1],1],Fun[NomerMin[2],
NomerMin[1],2],Fun[NomerMin[2],NomerMin[1],3]]:

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evalf(%);
end proc:

#
maximizeFun:=proc(Fun)
    local i, j ,NCoef, NStep, dddd, NomerMax:

    NStep:=numelems(Fun):
    NCoef:=numelems(Fun[1]):
    dddd:=Matrix([seq([seq(Fun[i,j,3], i = 1 .. NStep)
], j = 1 .. NCoef)]);
    NomerMax:=max[index](dddd);

    [Fun[NomerMax[2],NomerMax[1],1],Fun[NomerMax[2],
NomerMax[1],2],Fun[NomerMax[2],NomerMax[1],3]]:
    evalf(%);
end proc:

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# 1 2
FunPieceMinusStep:=proc(Piece, LeftStep, RightStep, NStep,
LeftCoef, RightCoef, NCoef, SetkaX)
    local i,j:
    local Coef, Step, NSetkaX, RaznicaStupStepen,
RaznicaStupStepenDiskret, Gunkzional:

    Coef:=SetkaRavnomer(LeftCoef, RightCoef, NCoef);
    Step:=SetkaRavnomer(LeftStep, RightStep, NStep);
    NSetkaX:=numelems(SetkaX):
    RaznicaStupStepen:=(Piece-BB*x^AA)^2:
    RaznicaStupStepenDiskret:=add(eval
(RaznicaStupStepen, x = SetkaX[hh])*(SetkaX[hh]-SetkaX[hh-1]
), hh=2..NSetkaX):
    for i from 1 to NStep+1 do
        for j from 1 to NCoef+1 do
            Gunkzional[i,j]:=subs(BB=Coef
[j], AA=Step[i], RaznicaStupStepenDiskret):
        od:
    od:

    seq([seq([Step[i], Coef[j], Gunkzional[i,j]], i = 1
.. NStep+1)], j = 1 .. NCoef+1)
end proc:

```

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> weight1 := 1:
weight2 := 1:
weight3 := 1:

```

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#-----
#
NTwant := 10:
NTstart := 1:

```

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NTend := 10:
#-----

#
Na := 20:
Nb := 20:
aEnd := 1:
bEnd := 1:
aStart := 0.01: #
bStart := 0: #

SetkaA := SetkaRavnomer(aStart, aEnd, Na):
SetkaB := SetkaRavnomer(bStart, bEnd, Nb):

#
shagX:=SetkaX[2]-SetkaX[1]:
shagT:=SetkaT[2]-SetkaT[1]:
for j from 1 to Na do
    for k from 1 to Nb do
        NaSetkePowerNumericSol := solverOsred
        (SetkaB[k], SetkaA[j], 0, 1, 1, L, LeftBound, RightBound,
        InitialData, SetkaX, SetkaT):
        for vv from 1 to Nt+1 do
            for hh from 1 to Nx do
                f[vv, hh] := weight1*
                (NaSetkePowerNumericSol[1][hh, vv]-NaSetkeFractDerivSol[vv,
                hh])^2/max(NaSetkePowerNumericSol[1][hh, vv],
                NaSetkeFractDerivSol[vv, hh])^2+
                weight2*(SetkaA[j]
                *SetkaX[hh]^SetkaB[j]*NaSetkePowerNumericSol[2][hh, vv]-a2*
                (NaSetkeFractDerivSol[vv, hh+1]-NaSetkeFractDerivSol[vv, hh])
                /shagX)^2/max(abs(SetkaA[j]*SetkaX[hh]^SetkaB[j]
                *NaSetkePowerNumericSol[2][hh, vv]), a2*abs
                (NaSetkeFractDerivSol[vv, hh+1]-NaSetkeFractDerivSol[vv, hh])
                /shagX)^2:
            od:
            f[vv, Nx+1] := weight1*
            (NaSetkePowerNumericSol[1][Nx+1, vv]-NaSetkeFractDerivSol[vv,
            Nx+1])^2+weight3*(a2-SetkaA[j]*SetkaX[Nx+1]^SetkaB[j])^2:
        od:
        FunRaznica[j, k] := shagT*shagX*add(add(f
        [vv, hh], hh=2..Nx+1), vv=2..Nt+1):
        NaSetkePowerNumericSol := 0:
        f := 0:
        printf("a=%f, b=%f, Funkcional=%f \n",
        SetkaA[j], SetkaB[k], FunRaznica[j, k]);
    od:
    printf("===== \n");
od:

#
For3dPlot := [seq([seq([SetkaA[jj], SetkaB[kk], FunRaznica
[jj, kk]], jj=1..Na)], kk=1..Nb)]:

```

```

MinimumAandB := minimizeFun(For3dPlot):
p r i n t f ( "          " ) :
print(MinimumAandB):
surfdata(For3dPlot, labels = [a, b, 'F'], labelfont =
["Verdana", bold, 14], shading=none, axes=boxed);

```

```

#end proc:

```

```

a=0.010000, b=0.000000, Funkcional=1.312960
a=0.010000, b=0.050000, Funkcional=1.317668
a=0.010000, b=0.100000, Funkcional=1.322036
a=0.010000, b=0.150000, Funkcional=1.326072
a=0.010000, b=0.200000, Funkcional=1.329785
a=0.010000, b=0.250000, Funkcional=1.333187
a=0.010000, b=0.300000, Funkcional=1.336293
a=0.010000, b=0.350000, Funkcional=1.339117
a=0.010000, b=0.400000, Funkcional=1.341676
a=0.010000, b=0.450000, Funkcional=1.343986
a=0.010000, b=0.500000, Funkcional=1.346066
a=0.010000, b=0.550000, Funkcional=1.347933
a=0.010000, b=0.600000, Funkcional=1.349604
a=0.010000, b=0.650000, Funkcional=1.351097
a=0.010000, b=0.700000, Funkcional=1.352428
a=0.010000, b=0.750000, Funkcional=1.353613
a=0.010000, b=0.800000, Funkcional=1.354668
a=0.010000, b=0.850000, Funkcional=1.355606
a=0.010000, b=0.900000, Funkcional=1.356441
a=0.010000, b=0.950000, Funkcional=1.357184
=====
a=0.059500, b=0.000000, Funkcional=1.031710
a=0.059500, b=0.050000, Funkcional=1.050152
a=0.059500, b=0.100000, Funkcional=1.067893
a=0.059500, b=0.150000, Funkcional=1.084847
a=0.059500, b=0.200000, Funkcional=1.100950
a=0.059500, b=0.250000, Funkcional=1.116157
a=0.059500, b=0.300000, Funkcional=1.130442
a=0.059500, b=0.350000, Funkcional=1.143794
a=0.059500, b=0.400000, Funkcional=1.156217
a=0.059500, b=0.450000, Funkcional=1.167727
a=0.059500, b=0.500000, Funkcional=1.178349
a=0.059500, b=0.550000, Funkcional=1.188115
a=0.059500, b=0.600000, Funkcional=1.197065
a=0.059500, b=0.650000, Funkcional=1.205241
a=0.059500, b=0.700000, Funkcional=1.212690
a=0.059500, b=0.750000, Funkcional=1.219456
a=0.059500, b=0.800000, Funkcional=1.225590
a=0.059500, b=0.850000, Funkcional=1.231136
a=0.059500, b=0.900000, Funkcional=1.236142
a=0.059500, b=0.950000, Funkcional=1.240651
=====
a=0.109000, b=0.000000, Funkcional=0.789182
a=0.109000, b=0.050000, Funkcional=0.816594
a=0.109000, b=0.100000, Funkcional=0.844047
a=0.109000, b=0.150000, Funkcional=0.871203
a=0.109000, b=0.200000, Funkcional=0.897769
a=0.109000, b=0.250000, Funkcional=0.923500
a=0.109000, b=0.300000, Funkcional=0.948201

```



```
a=0.109000, b=0.350000, Funkcional=0.971719
a=0.109000, b=0.400000, Funkcional=0.993945
a=0.109000, b=0.450000, Funkcional=1.014809
a=0.109000, b=0.500000, Funkcional=1.034274
a=0.109000, b=0.550000, Funkcional=1.052336
a=0.109000, b=0.600000, Funkcional=1.069011
a=0.109000, b=0.650000, Funkcional=1.084340
a=0.109000, b=0.700000, Funkcional=1.098374
a=0.109000, b=0.750000, Funkcional=1.111179
a=0.109000, b=0.800000, Funkcional=1.122826
a=0.109000, b=0.850000, Funkcional=1.133391
a=0.109000, b=0.900000, Funkcional=1.142952
a=0.109000, b=0.950000, Funkcional=1.151584
```

```
=====
a=0.158500, b=0.000000, Funkcional=0.587196
a=0.158500, b=0.050000, Funkcional=0.616742
a=0.158500, b=0.100000, Funkcional=0.648144
a=0.158500, b=0.150000, Funkcional=0.680756
a=0.158500, b=0.200000, Funkcional=0.713980
a=0.158500, b=0.250000, Funkcional=0.747282
a=0.158500, b=0.300000, Funkcional=0.780192
a=0.158500, b=0.350000, Funkcional=0.812312
a=0.158500, b=0.400000, Funkcional=0.843312
a=0.158500, b=0.450000, Funkcional=0.872935
a=0.158500, b=0.500000, Funkcional=0.900987
a=0.158500, b=0.550000, Funkcional=0.927338
a=0.158500, b=0.600000, Funkcional=0.951912
a=0.158500, b=0.650000, Funkcional=0.974679
a=0.158500, b=0.700000, Funkcional=0.995650
a=0.158500, b=0.750000, Funkcional=1.014869
a=0.158500, b=0.800000, Funkcional=1.032403
a=0.158500, b=0.850000, Funkcional=1.048339
a=0.158500, b=0.900000, Funkcional=1.062772
a=0.158500, b=0.950000, Funkcional=1.075807
```

```
=====
a=0.208000, b=0.000000, Funkcional=0.431898
a=0.208000, b=0.050000, Funkcional=0.456887
a=0.208000, b=0.100000, Funkcional=0.486188
a=0.208000, b=0.150000, Funkcional=0.518901
a=0.208000, b=0.200000, Funkcional=0.554141
a=0.208000, b=0.250000, Funkcional=0.591072
a=0.208000, b=0.300000, Funkcional=0.628929
a=0.208000, b=0.350000, Funkcional=0.667020
a=0.208000, b=0.400000, Funkcional=0.704742
a=0.208000, b=0.450000, Funkcional=0.741581
a=0.208000, b=0.500000, Funkcional=0.777117
a=0.208000, b=0.550000, Funkcional=0.811021
a=0.208000, b=0.600000, Funkcional=0.843050
a=0.208000, b=0.650000, Funkcional=0.873042
a=0.208000, b=0.700000, Funkcional=0.900905
a=0.208000, b=0.750000, Funkcional=0.926608
a=0.208000, b=0.800000, Funkcional=0.950173
a=0.208000, b=0.850000, Funkcional=0.971658
a=0.208000, b=0.900000, Funkcional=0.991156
a=0.208000, b=0.950000, Funkcional=1.008777
```

```
=====
a=0.257500, b=0.000000, Funkcional=0.323539
```

a=0.257500,	b=0.050000,	Funkcional=0.339423
a=0.257500,	b=0.100000,	Funkcional=0.361381
a=0.257500,	b=0.150000,	Funkcional=0.389089
a=0.257500,	b=0.200000,	Funkcional=0.421670
a=0.257500,	b=0.250000,	Funkcional=0.458068
a=0.257500,	b=0.300000,	Funkcional=0.497237
a=0.257500,	b=0.350000,	Funkcional=0.538196
a=0.257500,	b=0.400000,	Funkcional=0.580047
a=0.257500,	b=0.450000,	Funkcional=0.621993
a=0.257500,	b=0.500000,	Funkcional=0.663346
a=0.257500,	b=0.550000,	Funkcional=0.703528
a=0.257500,	b=0.600000,	Funkcional=0.742079
a=0.257500,	b=0.650000,	Funkcional=0.778647
a=0.257500,	b=0.700000,	Funkcional=0.812983
a=0.257500,	b=0.750000,	Funkcional=0.844932
a=0.257500,	b=0.800000,	Funkcional=0.874420
a=0.257500,	b=0.850000,	Funkcional=0.901443
a=0.257500,	b=0.900000,	Funkcional=0.926051
a=0.257500,	b=0.950000,	Funkcional=0.948336

=====

a=0.307000,	b=0.000000,	Funkcional=0.257352
a=0.307000,	b=0.050000,	Funkcional=0.262679
a=0.307000,	b=0.100000,	Funkcional=0.274426
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a=0.307000,	b=0.250000,	Funkcional=0.350545
a=0.307000,	b=0.300000,	Funkcional=0.387306
a=0.307000,	b=0.350000,	Funkcional=0.427838
a=0.307000,	b=0.400000,	Funkcional=0.470964
a=0.307000,	b=0.450000,	Funkcional=0.515595
a=0.307000,	b=0.500000,	Funkcional=0.560753
a=0.307000,	b=0.550000,	Funkcional=0.605588
a=0.307000,	b=0.600000,	Funkcional=0.649382
a=0.307000,	b=0.650000,	Funkcional=0.691553
a=0.307000,	b=0.700000,	Funkcional=0.731649
a=0.307000,	b=0.750000,	Funkcional=0.769348
a=0.307000,	b=0.800000,	Funkcional=0.804437
a=0.307000,	b=0.850000,	Funkcional=0.836806
a=0.307000,	b=0.900000,	Funkcional=0.866430
a=0.307000,	b=0.950000,	Funkcional=0.893352

=====

a=0.356500,	b=0.000000,	Funkcional=0.231122
a=0.356500,	b=0.050000,	Funkcional=0.224195
a=0.356500,	b=0.100000,	Funkcional=0.223955
a=0.356500,	b=0.150000,	Funkcional=0.231241
a=0.356500,	b=0.200000,	Funkcional=0.246612
a=0.356500,	b=0.250000,	Funkcional=0.270036
a=0.356500,	b=0.300000,	Funkcional=0.300749
a=0.356500,	b=0.350000,	Funkcional=0.337509
a=0.356500,	b=0.400000,	Funkcional=0.378928
a=0.356500,	b=0.450000,	Funkcional=0.423642
a=0.356500,	b=0.500000,	Funkcional=0.470386
a=0.356500,	b=0.550000,	Funkcional=0.518015
a=0.356500,	b=0.600000,	Funkcional=0.565534
a=0.356500,	b=0.650000,	Funkcional=0.612097
a=0.356500,	b=0.700000,	Funkcional=0.657019
a=0.356500,	b=0.750000,	Funkcional=0.699767

a=0.356500, b=0.800000, Funkcional=0.739953
a=0.356500, b=0.850000, Funkcional=0.777325
a=0.356500, b=0.900000, Funkcional=0.811745
a=0.356500, b=0.950000, Funkcional=0.843176

=====
a=0.406000, b=0.000000, Funkcional=0.237539
a=0.406000, b=0.050000, Funkcional=0.219920
a=0.406000, b=0.100000, Funkcional=0.207738
a=0.406000, b=0.150000, Funkcional=0.202403
a=0.406000, b=0.200000, Funkcional=0.205296
a=0.406000, b=0.250000, Funkcional=0.217365
a=0.406000, b=0.300000, Funkcional=0.238679
a=0.406000, b=0.350000, Funkcional=0.268379
a=0.406000, b=0.400000, Funkcional=0.305064
a=0.406000, b=0.450000, Funkcional=0.347165
a=0.406000, b=0.500000, Funkcional=0.393139
a=0.406000, b=0.550000, Funkcional=0.441550
a=0.406000, b=0.600000, Funkcional=0.491106
a=0.406000, b=0.650000, Funkcional=0.540680
a=0.406000, b=0.700000, Funkcional=0.589321
a=0.406000, b=0.750000, Funkcional=0.636256
a=0.406000, b=0.800000, Funkcional=0.680890
a=0.406000, b=0.850000, Funkcional=0.722791
a=0.406000, b=0.900000, Funkcional=0.761678
a=0.406000, b=0.950000, Funkcional=0.797402

=====
a=0.455500, b=0.000000, Funkcional=0.261901
a=0.455500, b=0.050000, Funkcional=0.237283
a=0.455500, b=0.100000, Funkcional=0.216545
a=0.455500, b=0.150000, Funkcional=0.201026
a=0.455500, b=0.200000, Funkcional=0.192293
a=0.455500, b=0.250000, Funkcional=0.192022
a=0.455500, b=0.300000, Funkcional=0.201557
a=0.455500, b=0.350000, Funkcional=0.221231
a=0.455500, b=0.400000, Funkcional=0.250211
a=0.455500, b=0.450000, Funkcional=0.286963
a=0.455500, b=0.500000, Funkcional=0.329736
a=0.455500, b=0.550000, Funkcional=0.376813
a=0.455500, b=0.600000, Funkcional=0.426601
a=0.455500, b=0.650000, Funkcional=0.477676
a=0.455500, b=0.700000, Funkcional=0.528800
a=0.455500, b=0.750000, Funkcional=0.578935
a=0.455500, b=0.800000, Funkcional=0.627246
a=0.455500, b=0.850000, Funkcional=0.673095
a=0.455500, b=0.900000, Funkcional=0.716023
a=0.455500, b=0.950000, Funkcional=0.755741

=====
a=0.505000, b=0.000000, Funkcional=0.294047
a=0.505000, b=0.050000, Funkcional=0.265190
a=0.505000, b=0.100000, Funkcional=0.238974
a=0.505000, b=0.150000, Funkcional=0.216545
a=0.505000, b=0.200000, Funkcional=0.199308
a=0.505000, b=0.250000, Funkcional=0.188924
a=0.505000, b=0.300000, Funkcional=0.187174
a=0.505000, b=0.350000, Funkcional=0.195552
a=0.505000, b=0.400000, Funkcional=0.214572
a=0.505000, b=0.450000, Funkcional=0.243474

```
a=0.505000, b=0.500000, Funkcional=0.280665
a=0.505000, b=0.550000, Funkcional=0.324266
a=0.505000, b=0.600000, Funkcional=0.372419
a=0.505000, b=0.650000, Funkcional=0.423400
a=0.505000, b=0.700000, Funkcional=0.475676
a=0.505000, b=0.750000, Funkcional=0.527924
a=0.505000, b=0.800000, Funkcional=0.579047
a=0.505000, b=0.850000, Funkcional=0.628169
a=0.505000, b=0.900000, Funkcional=0.674633
a=0.505000, b=0.950000, Funkcional=0.717975
```

```
=====
a=0.554500, b=0.000000, Funkcional=0.328611
a=0.554500, b=0.050000, Funkcional=0.297301
a=0.554500, b=0.100000, Funkcional=0.267711
a=0.554500, b=0.150000, Funkcional=0.240800
a=0.554500, b=0.200000, Funkcional=0.217774
a=0.554500, b=0.250000, Funkcional=0.200120
a=0.554500, b=0.300000, Funkcional=0.189570
a=0.554500, b=0.350000, Funkcional=0.187918
a=0.554500, b=0.400000, Funkcional=0.196602
a=0.554500, b=0.450000, Funkcional=0.216133
a=0.554500, b=0.500000, Funkcional=0.245787
a=0.554500, b=0.550000, Funkcional=0.283952
a=0.554500, b=0.600000, Funkcional=0.328670
a=0.554500, b=0.650000, Funkcional=0.377975
a=0.554500, b=0.700000, Funkcional=0.430049
a=0.554500, b=0.750000, Funkcional=0.483280
a=0.554500, b=0.800000, Funkcional=0.536290
a=0.554500, b=0.850000, Funkcional=0.587953
a=0.554500, b=0.900000, Funkcional=0.637381
a=0.554500, b=0.950000, Funkcional=0.683920
```

```
=====
a=0.604000, b=0.000000, Funkcional=0.362968
a=0.604000, b=0.050000, Funkcional=0.330331
a=0.604000, b=0.100000, Funkcional=0.298736
a=0.604000, b=0.150000, Funkcional=0.268985
a=0.604000, b=0.200000, Funkcional=0.242107
a=0.604000, b=0.250000, Funkcional=0.219396
a=0.604000, b=0.300000, Funkcional=0.202429
a=0.604000, b=0.350000, Funkcional=0.192979
a=0.604000, b=0.400000, Funkcional=0.192774
a=0.604000, b=0.450000, Funkcional=0.203061
a=0.604000, b=0.500000, Funkcional=0.224184
a=0.604000, b=0.550000, Funkcional=0.255399
a=0.604000, b=0.600000, Funkcional=0.295081
a=0.604000, b=0.650000, Funkcional=0.341220
a=0.604000, b=0.700000, Funkcional=0.391776
a=0.604000, b=0.750000, Funkcional=0.444867
a=0.604000, b=0.800000, Funkcional=0.498835
a=0.604000, b=0.850000, Funkcional=0.552283
a=0.604000, b=0.900000, Funkcional=0.604079
a=0.604000, b=0.950000, Funkcional=0.653357
```

```
=====
a=0.653500, b=0.000000, Funkcional=0.395906
a=0.653500, b=0.050000, Funkcional=0.362653
a=0.653500, b=0.100000, Funkcional=0.329938
a=0.653500, b=0.150000, Funkcional=0.298439
```

```
a=0.653500, b=0.200000, Funkcional=0.269036
a=0.653500, b=0.250000, Funkcional=0.242852
a=0.653500, b=0.300000, Funkcional=0.221290
a=0.653500, b=0.350000, Funkcional=0.206008
a=0.653500, b=0.400000, Funkcional=0.198771
a=0.653500, b=0.450000, Funkcional=0.201147
a=0.653500, b=0.500000, Funkcional=0.214080
a=0.653500, b=0.550000, Funkcional=0.237677
a=0.653500, b=0.600000, Funkcional=0.271130
a=0.653500, b=0.650000, Funkcional=0.312785
a=0.653500, b=0.700000, Funkcional=0.360584
a=0.653500, b=0.750000, Funkcional=0.412441
a=0.653500, b=0.800000, Funkcional=0.466438
a=0.653500, b=0.850000, Funkcional=0.520907
a=0.653500, b=0.900000, Funkcional=0.574464
a=0.653500, b=0.950000, Funkcional=0.626007
```

=====

```
a=0.703000, b=0.000000, Funkcional=0.426929
a=0.703000, b=0.050000, Funkcional=0.393506
a=0.703000, b=0.100000, Funkcional=0.360247
a=0.703000, b=0.150000, Funkcional=0.327729
a=0.703000, b=0.200000, Funkcional=0.296707
a=0.703000, b=0.250000, Funkcional=0.268161
a=0.703000, b=0.300000, Funkcional=0.243333
a=0.703000, b=0.350000, Funkcional=0.223739
a=0.703000, b=0.400000, Funkcional=0.211082
a=0.703000, b=0.450000, Funkcional=0.207045
a=0.703000, b=0.500000, Funkcional=0.212920
a=0.703000, b=0.550000, Funkcional=0.229283
a=0.703000, b=0.600000, Funkcional=0.256011
a=0.703000, b=0.650000, Funkcional=0.292204
a=0.703000, b=0.700000, Funkcional=0.336148
a=0.703000, b=0.750000, Funkcional=0.385734
a=0.703000, b=0.800000, Funkcional=0.438852
a=0.703000, b=0.850000, Funkcional=0.493579
a=0.703000, b=0.900000, Funkcional=0.548271
a=0.703000, b=0.950000, Funkcional=0.601586
```

=====

```
a=0.752500, b=0.000000, Funkcional=0.455897
a=0.752500, b=0.050000, Funkcional=0.422587
a=0.752500, b=0.100000, Funkcional=0.389159
a=0.752500, b=0.150000, Funkcional=0.356107
a=0.752500, b=0.200000, Funkcional=0.324088
a=0.752500, b=0.250000, Funkcional=0.293959
a=0.752500, b=0.300000, Funkcional=0.266823
a=0.752500, b=0.350000, Funkcional=0.244055
a=0.752500, b=0.400000, Funkcional=0.227259
a=0.752500, b=0.450000, Funkcional=0.218122
a=0.752500, b=0.500000, Funkcional=0.218131
a=0.752500, b=0.550000, Funkcional=0.228193
a=0.752500, b=0.600000, Funkcional=0.248530
a=0.752500, b=0.650000, Funkcional=0.278833
a=0.752500, b=0.700000, Funkcional=0.318084
a=0.752500, b=0.750000, Funkcional=0.364473
a=0.752500, b=0.800000, Funkcional=0.415842
a=0.752500, b=0.850000, Funkcional=0.470071
a=0.752500, b=0.900000, Funkcional=0.525273
```

a=0.752500, b=0.950000, Funkcional=0.579856

=====

a=0.802000, b=0.000000, Funkcional=0.482843
a=0.802000, b=0.050000, Funkcional=0.449825
a=0.802000, b=0.100000, Funkcional=0.416472
a=0.802000, b=0.150000, Funkcional=0.383215
a=0.802000, b=0.200000, Funkcional=0.350626
a=0.802000, b=0.250000, Funkcional=0.319464
a=0.802000, b=0.300000, Funkcional=0.290712
a=0.802000, b=0.350000, Funkcional=0.265614
a=0.802000, b=0.400000, Funkcional=0.245664
a=0.802000, b=0.450000, Funkcional=0.232503
a=0.802000, b=0.500000, Funkcional=0.227705
a=0.802000, b=0.550000, Funkcional=0.232420
a=0.802000, b=0.600000, Funkcional=0.247126
a=0.802000, b=0.650000, Funkcional=0.271772
a=0.802000, b=0.700000, Funkcional=0.305910
a=0.802000, b=0.750000, Funkcional=0.348362
a=0.802000, b=0.800000, Funkcional=0.397190
a=0.802000, b=0.850000, Funkcional=0.450193
a=0.802000, b=0.900000, Funkcional=0.505277
a=0.802000, b=0.950000, Funkcional=0.560618

=====

a=0.851500, b=0.000000, Funkcional=0.507881
a=0.851500, b=0.050000, Funkcional=0.475265
a=0.851500, b=0.100000, Funkcional=0.442148
a=0.851500, b=0.150000, Funkcional=0.408906
a=0.851500, b=0.200000, Funkcional=0.376046
a=0.851500, b=0.250000, Funkcional=0.344241
a=0.851500, b=0.300000, Funkcional=0.314372
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a=0.851500, b=0.400000, Funkcional=0.265220
a=0.851500, b=0.450000, Funkcional=0.248890
a=0.851500, b=0.500000, Funkcional=0.240177
a=0.851500, b=0.550000, Funkcional=0.240396
a=0.851500, b=0.600000, Funkcional=0.250249
a=0.851500, b=0.650000, Funkcional=0.269848
a=0.851500, b=0.700000, Funkcional=0.298975
a=0.851500, b=0.750000, Funkcional=0.337050
a=0.851500, b=0.800000, Funkcional=0.382672
a=0.851500, b=0.850000, Funkcional=0.433771
a=0.851500, b=0.900000, Funkcional=0.488129
a=0.851500, b=0.950000, Funkcional=0.543710

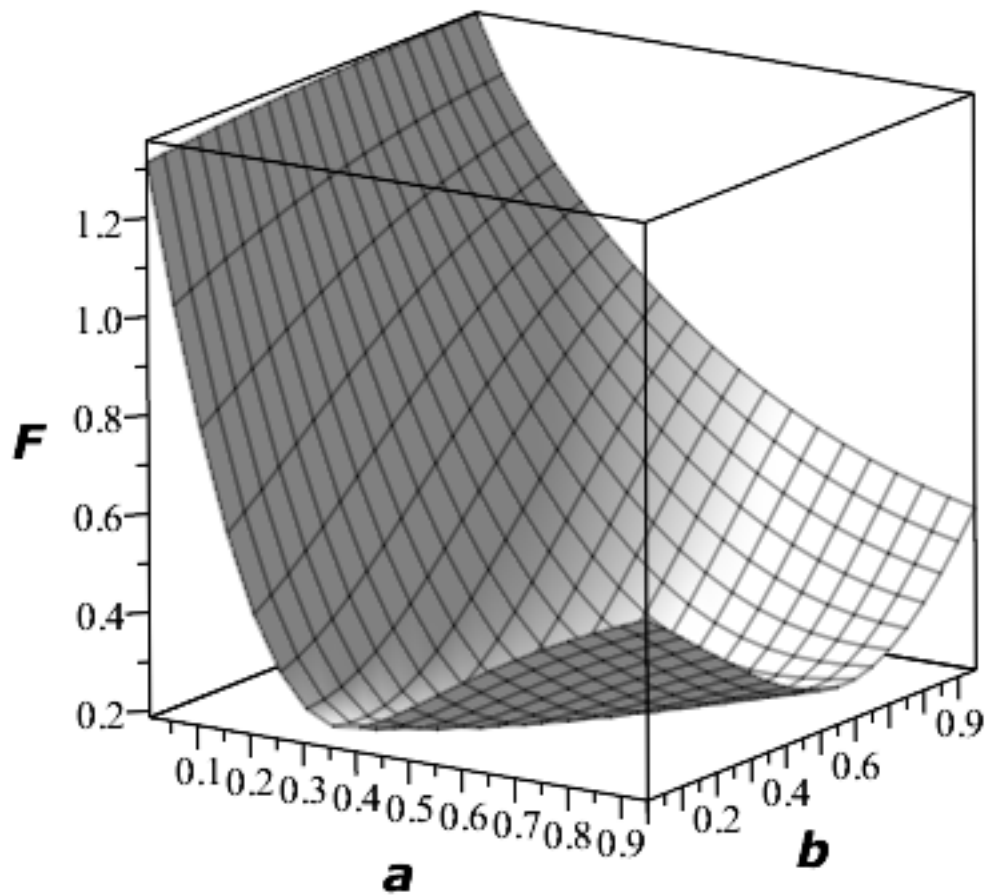
=====

a=0.901000, b=0.000000, Funkcional=0.531161
a=0.901000, b=0.050000, Funkcional=0.499011
a=0.901000, b=0.100000, Funkcional=0.466233
a=0.901000, b=0.150000, Funkcional=0.433156
a=0.901000, b=0.200000, Funkcional=0.400231
a=0.901000, b=0.250000, Funkcional=0.368061
a=0.901000, b=0.300000, Funkcional=0.337442
a=0.901000, b=0.350000, Funkcional=0.309404
a=0.901000, b=0.400000, Funkcional=0.285226
a=0.901000, b=0.450000, Funkcional=0.266402
a=0.901000, b=0.500000, Funkcional=0.254507
a=0.901000, b=0.550000, Funkcional=0.250957
a=0.901000, b=0.600000, Funkcional=0.256653

```
a=0.901000, b=0.650000, Funkcional=0.271852
a=0.901000, b=0.700000, Funkcional=0.296432
a=0.901000, b=0.750000, Funkcional=0.330086
a=0.901000, b=0.800000, Funkcional=0.372043
a=0.901000, b=0.850000, Funkcional=0.420641
a=0.901000, b=0.900000, Funkcional=0.473694
a=0.901000, b=0.950000, Funkcional=0.529007
```

```
=====
a=0.950500, b=0.000000, Funkcional=0.552836
a=0.950500, b=0.050000, Funkcional=0.521188
a=0.950500, b=0.100000, Funkcional=0.488813
a=0.950500, b=0.150000, Funkcional=0.456002
a=0.950500, b=0.200000, Funkcional=0.423157
a=0.950500, b=0.250000, Funkcional=0.390822
a=0.950500, b=0.300000, Funkcional=0.359721
a=0.950500, b=0.350000, Funkcional=0.330795
a=0.950500, b=0.400000, Funkcional=0.305231
a=0.950500, b=0.450000, Funkcional=0.284440
a=0.950500, b=0.500000, Funkcional=0.269960
a=0.950500, b=0.550000, Funkcional=0.263256
a=0.950500, b=0.600000, Funkcional=0.265391
a=0.950500, b=0.650000, Funkcional=0.276774
a=0.950500, b=0.700000, Funkcional=0.297348
a=0.950500, b=0.750000, Funkcional=0.326889
a=0.950500, b=0.800000, Funkcional=0.365001
a=0.950500, b=0.850000, Funkcional=0.410632
a=0.950500, b=0.900000, Funkcional=0.461850
a=0.950500, b=0.950000, Funkcional=0.516407
```

```
=====
[0.5050000000, 0.3000000000, 0.187174360127205]
```



```

> if 0=1:
#1
                                f[hh] := weight1*
(NaSetkePowerNumericSol[1][hh, NTwant]-NaSetkeFractDerivSol
[NTwant, hh])^2/max(NaSetkePowerNumericSol[1][hh, NTwant],
NaSetkeFractDerivSol[NTwant, hh])^2+
                                weight2*
(NaSetkePowerNumericSol[2][hh, NTwant]-(NaSetkeFractDerivSol
[NTwant, hh+1]-NaSetkeFractDerivSol[NTwant, hh])/shagX)^2/max
(abs(NaSetkePowerNumericSol[2][hh, NTwant]), abs
(NaSetkeFractDerivSol[NTwant, hh+1]-NaSetkeFractDerivSol
[NTwant, hh])/shagX)^2+
                                weight3*(a2-SetkaA
[j]*SetkaX[hh]^SetkaB[j])^2/max(a2, SetkaA[j]*SetkaX[hh]
^SetkaB[j])^2:
#2
f[Nx+1] := weight1*(NaSetkePowerNumericSol[1][Nx+1, NTwant]-
NaSetkeFractDerivSol[NTwant, Nx+1])^2+weight3*(a2-SetkaA[j]
*SetkaX[Nx+1]^SetkaB[j])^2:
fi:
#FunPieceMinusStep:=proc(a2, b2, weight1, weight2, weight3)

```



```

> #
#plots[animate]( plot, [[seq([SetkaX[i], subs(t=SetkaT[trunc(j)],
x=SetkaX[i], ForHelp[2]]), i=1..Nx+1)]], j=1..Nt):
MinimumAandB:= [.5050000000, .3000000000]:

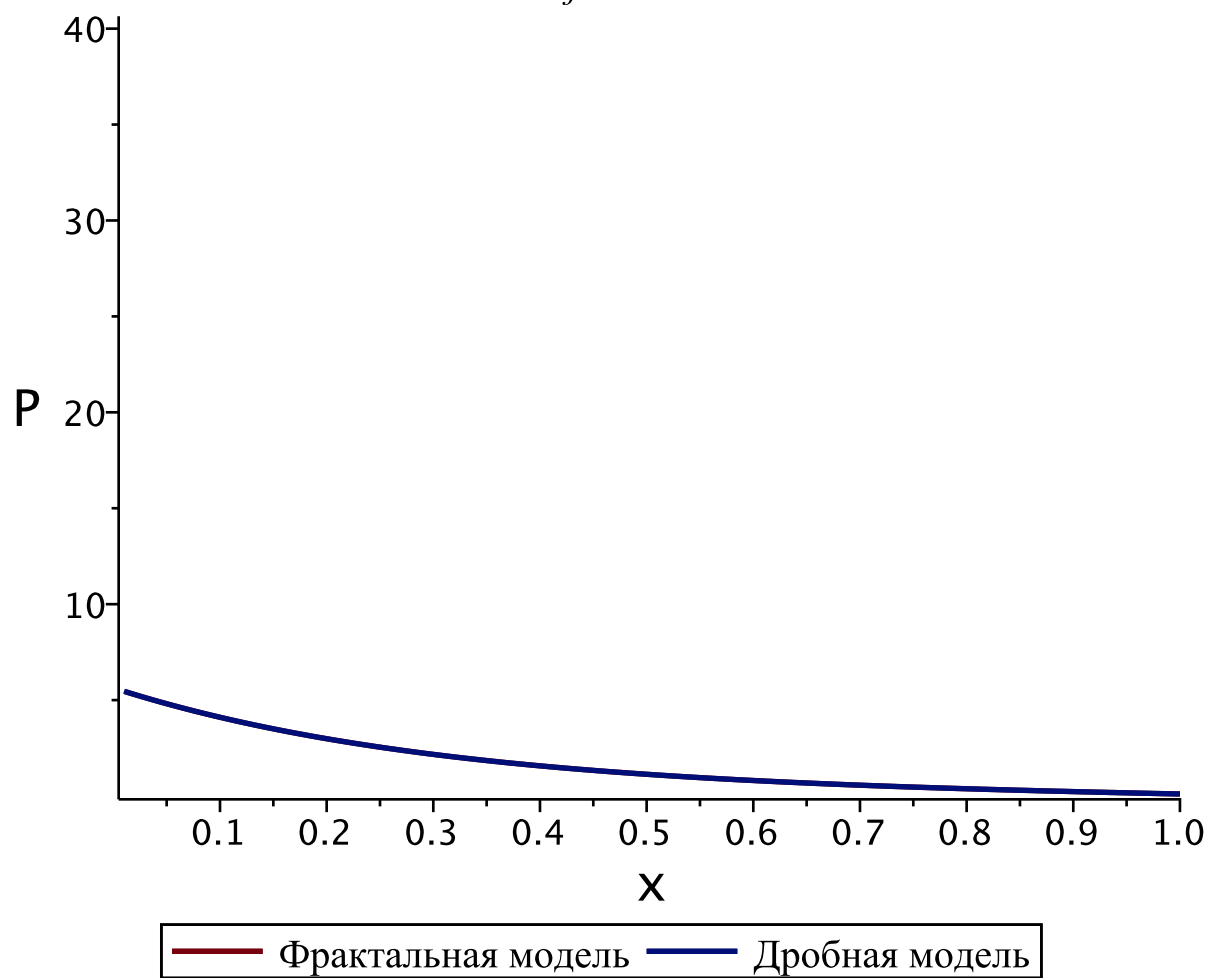
NumericSol3 := solverOsred(MinimumAandB[2], MinimumAandB[1], 0,
1, 1, L, LeftBound, RightBound, InitialData, SetkaX, SetkaT):
j:='j':
plots[animate]( plot, [[[seq([SetkaX[i], NumericSol3[1][i, trunc
(j)]]), i=1..Nx+1]]],
[seq([SetkaX[i], subs(t=SetkaT
[trunc(j)], x=SetkaX[i], ForHelp[2]]), i=1..Nx+1)]], legend=
[ " " , " " ], j=1..Nt, thickness =
2, labels=["x","P"], labelfont = ["HELVETICA", 15], axesfont=
["HELVETICA",10], legendstyle = [font = ["HELVETICA", 15],
location = bottom], trace = 5);
plots[animate]( plot, [[[seq([SetkaX[i], MinimumAandB[1]*SetkaX
[i]^MinimumAandB[2]*NumericSol3[2][i, trunc(j)]]), i=1..Nx+1]]],
[seq([SetkaX[i], a2*
(NaSetkeFractDerivSol[trunc(j), i+1]-NaSetkeFractDerivSol[trunc
(j), i])/shagX], i=1..Nx+1)]], legend = [ " " ,
" " ], j=1..Nt, thickness = 2, labels=["x","kPx"],
labelfont = ["HELVETICA", 15], axesfont=["HELVETICA",10],
legendstyle = [font = ["HELVETICA", 15], location = bottom],
trace = 5);

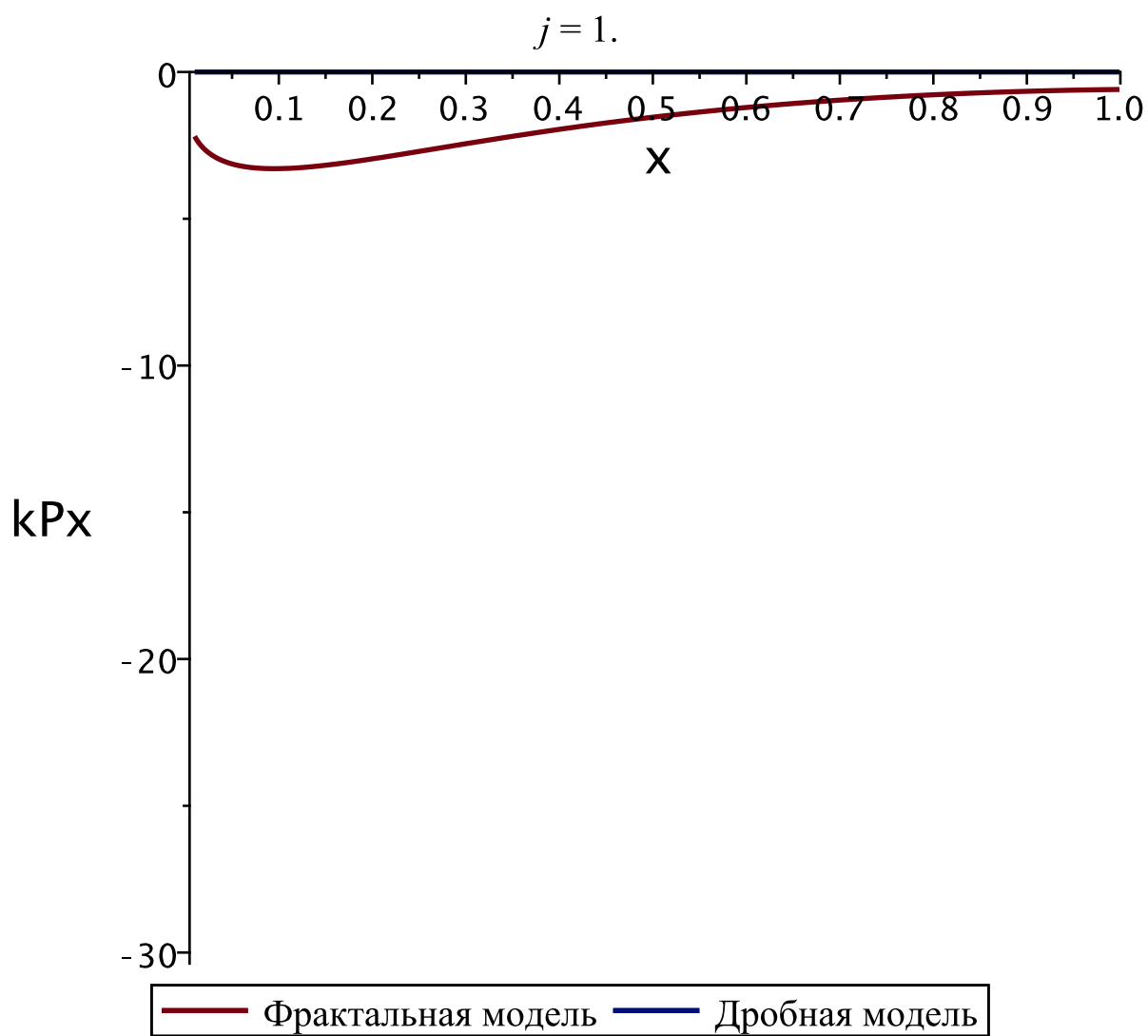
plot([MinimumAandB[1]*x^MinimumAandB[2], a2], x=1..L, labels=
["x","k"], labelfont = ["HELVETICA", 15], axesfont=["HELVETICA",
10], legendstyle = [font = ["HELVETICA", 15], location = bottom],
thickness = 2, legend = [ " " , " " ] );

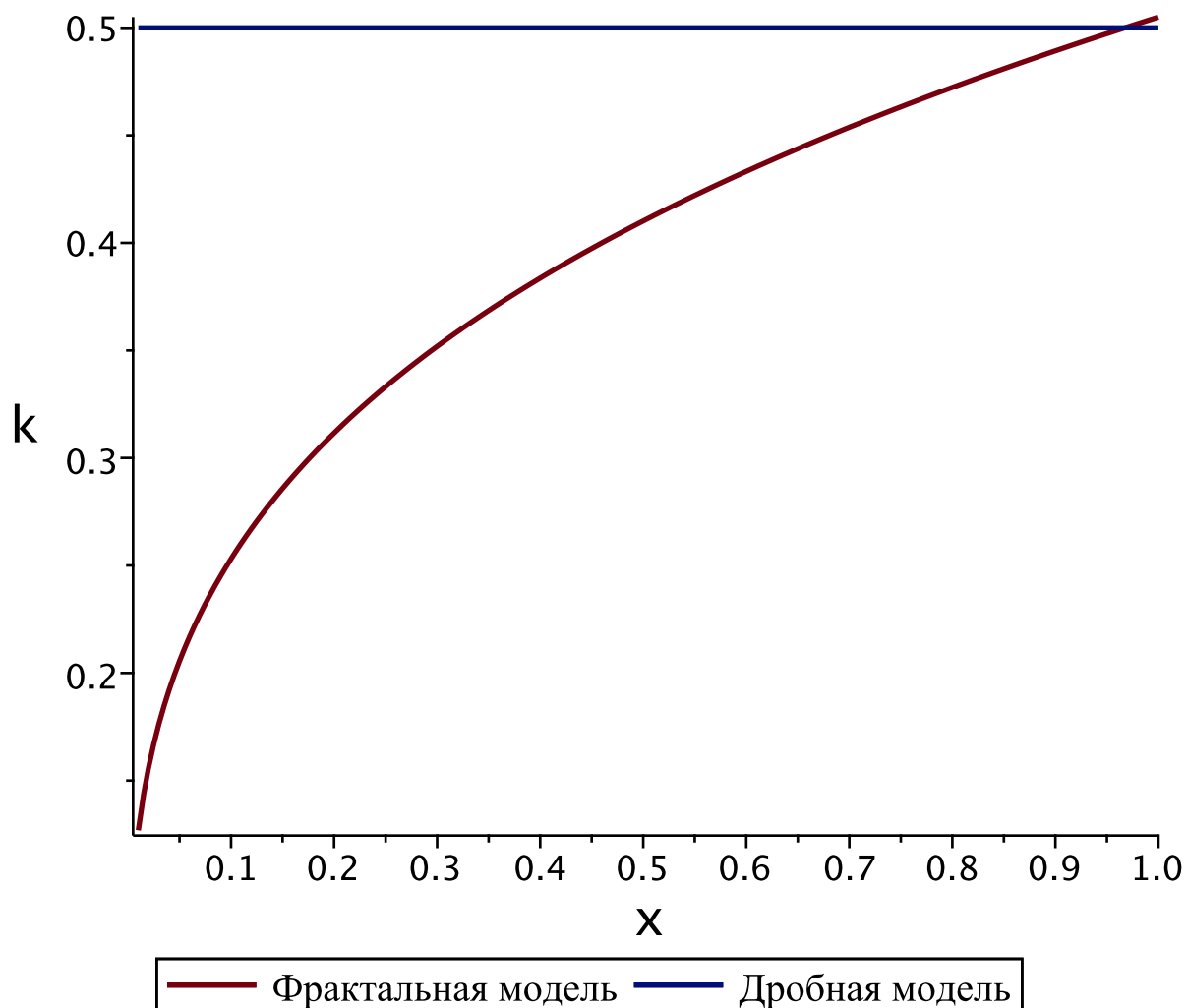
#plot([LeftBound, RightBound], t=0..T, labels=["t","p(t, x)"],
labelfont = ["HELVETICA", 15],
#legend = [ " " , " " ], legendstyle = [font
= ["HELVETICA", 15], location = right], thickness = 3, axesfont=
["HELVETICA",10]);

```

$$j = 1.$$







> NumericSol3;

solverOsred(0.3000000000, 0.5050000000, 0, 1, 0.01, 1, 5.460451711 + 9.678398663 t
+ 10.92090342 t^2 + 9.678398663 t^3 + 7.280602283 t^4 + 4.839199332 t^5 + 2.912240913 t^6
+ 1.613066444 t^7 + 0.8320688319 t^8 + 0.4032666110 t^9 + 0.1849041849 t^{10}
+ 0.08065332219 t^{11} + 0.03361894272 t^{12} , 0.1055309664 + 0.1870487678 t
+ 0.2110619328 t^2 + 0.1870487678 t^3 + 0.1407079552 t^4 + 0.09352438390 t^5
+ 0.05628318210 t^6 + 0.03117479464 t^7 + 0.01608090916 t^8 + 0.007793698659 t^9
+ 0.003573535371 t^{10} + 0.001558739732 t^{11} + 0.0006497337038 t^{12} ,
-0.005641895835 $e^{3.162277659x}$ + 5.641895835 $e^{-3.162277659x}$, [0.01, 0.01990000000,
0.02980000000, 0.03970000000, 0.04960000000, 0.05950000000, 0.06940000000,
0.07930000000, 0.08920000000, 0.09910000000, 0.1090000000, 0.1189000000,
0.1288000000, 0.1387000000, 0.1486000000, 0.1585000000, 0.1684000000,
0.1783000000, 0.1882000000, 0.1981000000, 0.2080000000, 0.2179000000,
0.2278000000, 0.2377000000, 0.2476000000, 0.2575000000, 0.2674000000,
0.2773000000, 0.2872000000, 0.2971000000, 0.3070000000, 0.3169000000,
0.3268000000, 0.3367000000, 0.3466000000, 0.3565000000, 0.3664000000,

(1)

```

0.3763000000, 0.3862000000, 0.3961000000, 0.4060000000, 0.4159000000,
0.4258000000, 0.4357000000, 0.4456000000, 0.4555000000, 0.4654000000,
0.4753000000, 0.4852000000, 0.4951000000, 0.5050000000, 0.5149000000,
0.5248000000, 0.5347000000, 0.5446000000, 0.5545000000, 0.5644000000,
0.5743000000, 0.5842000000, 0.5941000000, 0.6040000000, 0.6139000000,
0.6238000000, 0.6337000000, 0.6436000000, 0.6535000000, 0.6634000000,
0.6733000000, 0.6832000000, 0.6931000000, 0.7030000000, 0.7129000000,
0.7228000000, 0.7327000000, 0.7426000000, 0.7525000000, 0.7624000000,
0.7723000000, 0.7822000000, 0.7921000000, 0.8020000000, 0.8119000000,
0.8218000000, 0.8317000000, 0.8416000000, 0.8515000000, 0.8614000000,
0.8713000000, 0.8812000000, 0.8911000000, 0.9010000000, 0.9109000000,
0.9208000000, 0.9307000000, 0.9406000000, 0.9505000000, 0.9604000000,
0.9703000000, 0.9802000000, 0.9901000000, 1], [0, 0.1000000000, 0.2000000000,
0.3000000000, 0.4000000000, 0.5000000000, 0.6000000000, 0.7000000000,
0.8000000000, 0.9000000000, 1])

```

```

> #
a2_show := 10^(-10): #
b2_show := 0.2: #
#
c2_show := 0.000000001: #
c_x21_show := 0.0000001: #
c_x22_show := 0.000001: #

sol02 := ExactMeshSolution(T, 1, L, a2_show, 0.2, c2_show,
c_x21_show, c_x22_show, Nx, Nt):
NaSetkeFractDerivSol := sol02[1]:
PartSolution02 := sol02[2]:

sol05 := ExactMeshSolution(T, 1, L, a2_show, 0.5, c2_show,
c_x21_show, c_x22_show, Nx, Nt):
NaSetkeFractDerivSol := sol05[1]:
PartSolution05 := sol05[2]:

sol08 := ExactMeshSolution(T, 1, L, a2_show, 0.8, c2_show,
c_x21_show, c_x22_show, Nx, Nt):
NaSetkeFractDerivSol := sol08[1]:
PartSolution08 := sol08[2]:

j:='j':
plots[animate]( plot, [[
[seq([SetkaX[i], subs(t=SetkaT[trunc(j)], x=SetkaX[i],
PartSolution02)], i=1..Nx+1)],
[seq([SetkaX[i], subs(t=SetkaT[trunc(j)], x=SetkaX[i],
PartSolution05)], i=1..Nx+1)],
[seq([SetkaX[i], subs(t=SetkaT[trunc(j)], x=SetkaX[i],
PartSolution08)], i=1..Nx+1)]]], legend = [' =0.2', 0.5,

```

0.8]] , j=1..Nt) ;

()

$$p2 = \left(m2(x) = _C1 \, e^{\frac{\sqrt{C2} \, x}{\sqrt{A2}}} + _C2 \, e^{-\frac{\sqrt{C2} \, x}{\sqrt{A2}}} \right)$$

$$add\left(\frac{t^k}{\Gamma(0.2 \, k + 0.2)}, k=0..12\right) (1. \, 10^{-7} \, e^{3.162277660 \, x} + 1. \, 10^{-6} \, e^{-3.162277660 \, x})$$

()

$$p2 = \left(m2(x) = _C1 \, e^{\frac{\sqrt{C2} \, x}{\sqrt{A2}}} + _C2 \, e^{-\frac{\sqrt{C2} \, x}{\sqrt{A2}}} \right)$$

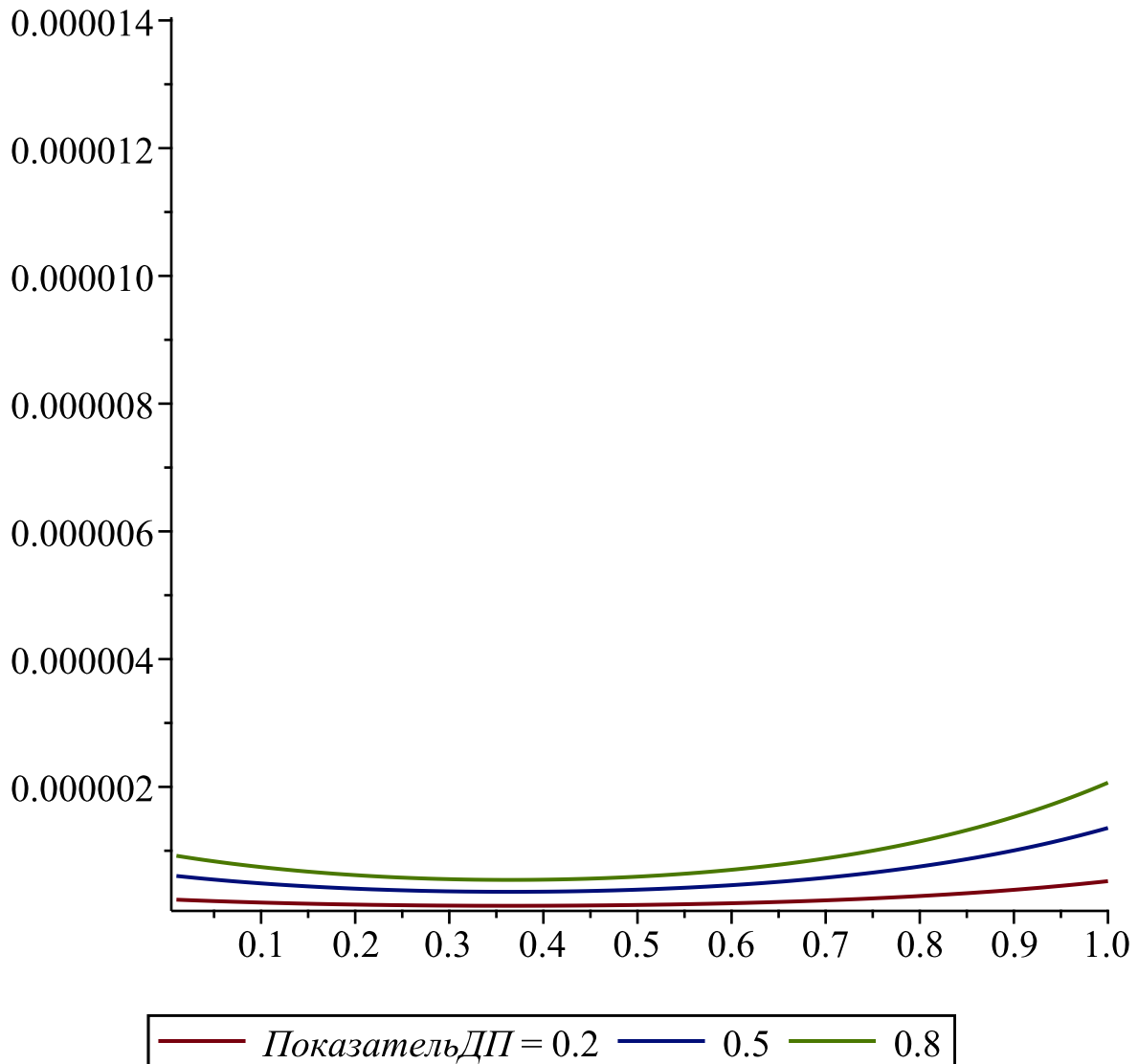
$$add\left(\frac{t^k}{\Gamma(0.5 \, k + 0.5)}, k=0..12\right) (1. \, 10^{-7} \, e^{3.162277660 \, x} + 1. \, 10^{-6} \, e^{-3.162277660 \, x})$$

()

$$p2 = \left(m2(x) = _C1 \, e^{\frac{\sqrt{C2} \, x}{\sqrt{A2}}} + _C2 \, e^{-\frac{\sqrt{C2} \, x}{\sqrt{A2}}} \right)$$

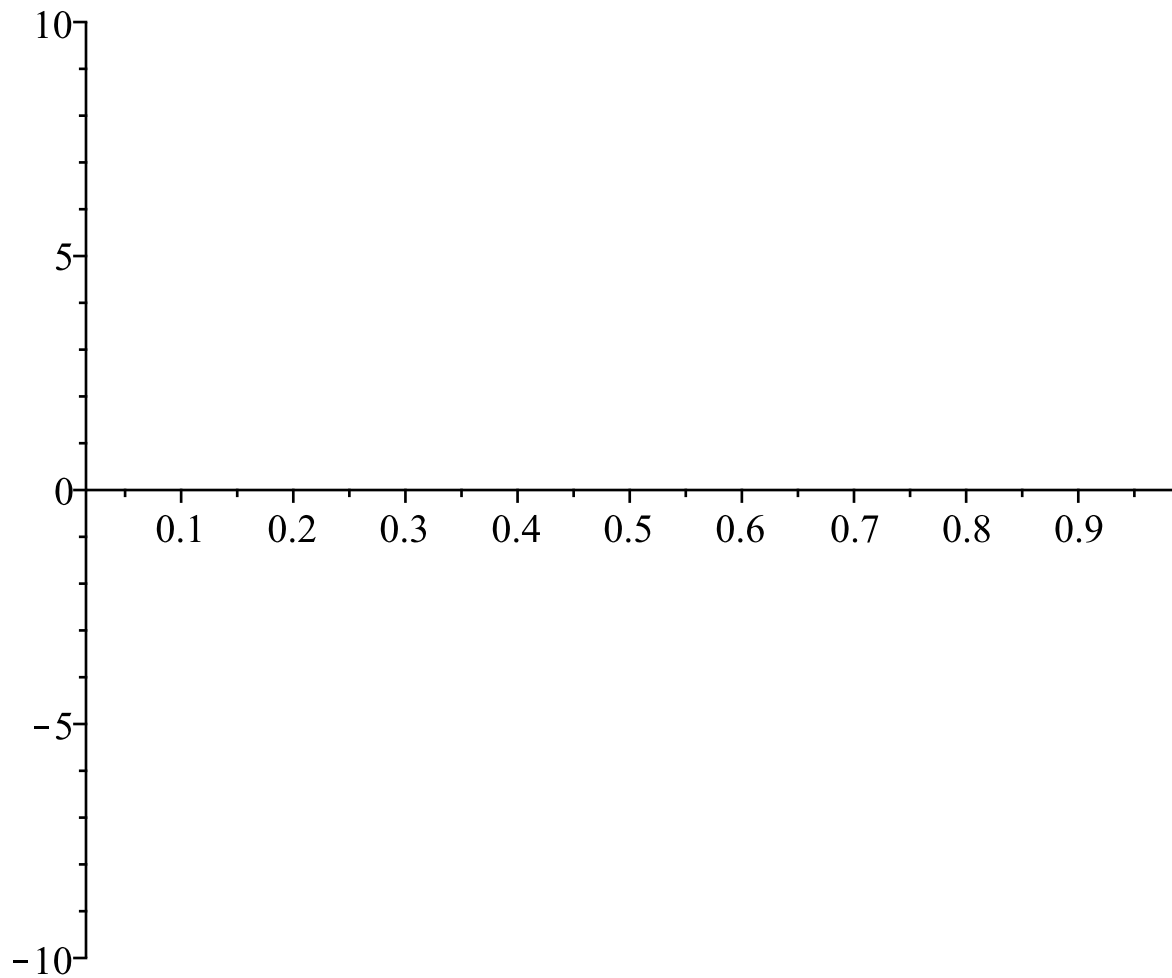
$$add\left(\frac{t^k}{\Gamma(0.8 \, k + 0.8)}, k=0..12\right) (1. \, 10^{-7} \, e^{3.162277660 \, x} + 1. \, 10^{-6} \, e^{-3.162277660 \, x})$$

$j = 1.$



```
> j:='j':
h:=SetkaX[2]-SetkaX[1]:
plots[animate]( plot, [[
[seq([SetkaX[i], (subs(t=SetkaT[trunc(j)], x=SetkaX[i+1],
PartSolution02)
+2*subs(t=SetkaT[trunc(j)], x=SetkaX[i], PartSolution02)
-subs(t=SetkaT[trunc(j)], x=SetkaX[i-1], PartSolution02))/h^2],
i=2..Nx)],
[seq([SetkaX[i], (subs(t=SetkaT[trunc(j)], x=SetkaX[i+1],
PartSolution05)
+2*subs(t=SetkaT[trunc(j)], x=SetkaX[i], PartSolution05)
-subs(t=SetkaT[trunc(j)], x=SetkaX[i-1], PartSolution05))/h^2],
i=2..Nx)],
[seq([SetkaX[i], (subs(t=SetkaT[trunc(j)], x=SetkaX[i+1],
PartSolution08)
+2*subs(t=SetkaT[trunc(j)], x=SetkaX[i], PartSolution08)
-subs(t=SetkaT[trunc(j)], x=SetkaX[i-1], PartSolution08))/h^2],
i=2..Nx)]]], j=1..Nt);
```

$$j = 1.$$



```
>
fff:=aa*x^bb-(kk/GAMMA(alpha)+kk*(1-alpha)/GAMMA(alpha)*x)

for j from 1 to Na do
    for k from 1 to Nb do
        FunRaznica[j, k] := subs(aa, fff):
        printf("a=%f, b=%f, Funkcional=%f \n", SetkaA
[j], SetkaB[k], FunRaznica[j, k]);
    od:
    printf("===== \n");
od:
Error, `)` unexpected
```