

```
    cout << "Roots = " << A[i];
```

```
    return 0;
```

```
}
```

## Secant Method:

$$f(x) = x^3 - 10x + 1$$

$$\text{formula} = x_{i+1} = x_i - \frac{x_i - x_{i-1}}{f(x_i) - f(x_{i-1})} * f(x_i)$$

### Guess Values:

$x$	$f(x)$	$x$	$f(x)$	$x$	$f(x)$
• -10	-899	• -9	4	• 4	25
• -9	-638	• -8	13	• 5	76
• -8	-431	• -1	10	• 6	157
• -7	-272	• 0	1	• 7	274
• -6	-155	• 1	-8	• 8	433
• -5	-74	• 2	-11	• 9	640
• -4	-23	• 3	-2	• 10	901

We use Guess value (0, 1)

$x_0 = 0$

$x_1 = 1$

We want to find  $x_2 = ?$

" $i=2$ " put  $i=2$  in formula

$$x_2 = x_1 - \frac{x_1 - x_0}{f(x_1) - f(x_0)} * f(x_1) \quad \text{--- (1)}$$

$$f(x_0) = (0)^3 - 10(0) + 1$$

$$= 1$$



$$f(x_1) = (1)^3 - 10(1) + 1 \\ = -8$$

Putting value in of  $x_1, x_0, f(x_1), f(x_0)$  in equation (1)

$$x_2 = 1 - \left( \frac{1-0}{(-8-1)} \right) * (-8)$$

$$1 - \left( \frac{-1}{-9} \right) * (-8)$$

$$1 - \left( \frac{8}{9} \right) \Rightarrow \frac{9-8}{9} \Rightarrow \frac{1}{9} \Rightarrow 0.1111$$

$$|x_2 - x_1| \Rightarrow |0.1111 - 1| \Rightarrow 0.8889$$

"i=3" putting i=3 in formula

$$x_3 = x_2 - \frac{x_2 - x_1}{f(x_2) - f(x_1)} * f(x_2) \quad \text{--- (11)}$$

$$x_1 = 1$$

$$f(x_1) = -8$$

$$x_2 = 0.1111$$

$$f(x_2) = (0.1111)^3 - 10(0.1111) + 1$$

$$= 0.00137 - 1.1111 + 1$$

$$= -0.1098$$

Putting value of  $x_1, x_2, f(x_1), f(x_2)$  in eqn (11)



$$x_3 = 0.1111 - \frac{0.1111 - 1}{-0.1098 - (-8)} * -0.1098$$

$$0.1111 - \left( \frac{-0.8889}{7.8902} \right) * (-0.1098)$$

$$0.1111 - \frac{0.0976}{7.8902}$$

$$\frac{0.8766 - 0.0976}{7.8902} \Rightarrow \frac{0.779}{7.8902} = 0.0987$$

$$x_3 = 0.0987$$

$$|x_3 - x_2| \Rightarrow |0.0987 - (0.1111)| \Rightarrow 0.0124$$

"i.e. 4" put in formula

$$x_4 = x_3 - \frac{x_3 - x_2 * f(x_3)}{f(x_3) - f(x_2)} \quad \text{--- (11)}$$

$$x_2 = 0.1111$$

$$f(x_2) = -0.1098$$

$$x_3 = 0.0987$$

$$\begin{aligned} f(x_3) &= (0.0987)^3 - 10(0.0987) + 1 \\ &= 0.0089 - 0.987 + 1 \\ &= 0.0139 \end{aligned}$$

Putting, value of  $x_2$ ,  $f(x_2)$ ,  $x_3$ ,  $f(x_3)$  in equ (11)



$$0.0987 - \left( \frac{0.0987 - 0.1111}{0.0139 - 0.1098} \right) * 0.0139$$

$$0.0987 - \left( \frac{-0.0124}{0.1237} \right) * 0.0139$$

$$0.0987 - \frac{0.0001}{0.1237}$$

$$\frac{0.0122 - 0.00017}{0.1237} \approx \frac{0.0123}{0.1237} \approx 0.0978$$

$$x_4 \approx 0.0994$$

$$|x_4 - x_3| \approx |0.0978 - 0.0994| \approx 0.0016$$

As the value is less than 0.001 we stop computing

Program

```
#include <iostream.h>
#include <conio.h>
#include <math.h>
int main()
{
    float x[20], fx[20];
    int i = 0;
    cout << "Enter Value of Lower Bound";
    cin >> x[i];
```



cout << "Enter the Value of upper bound";

cin >> x[i+1];

do

{

fx[i] = x[i] \* x[i] \* x[i] - 10 \* x[i] + 1;

fx[i+1] = x[i+1] \* x[i+1] \* x[i+1] - 10 \* x[i+1] + 1;

x[i+2] = x[i+1] -  $\left( \frac{x[i+1] - x[i]}{fx[i+1] - fx[i]} \right) * fx[i+1];$

i++

while (fabs(x[i+1] - x[i]) > 0.0001)

}

return 0;

}

## Algorithm:

Secant Method for finding roots where "x" and "fx" is an array of 20 elements and i is a loop Counter which is equal to 0

Step 1: Read x[0], x[0+1]

Step 2: Do Step 3 to 6 while (x[i+1] - x[i]) > 0.0001

Step 3: fx[i] = x[i] \* x[i] \* x[i] - 10 \* x[i] + 1;

Step 4: fx[i+1] = x[i+1] \* x[i+1] \* x[i+1] - 10 \* x[i+1] + 1

Step 5: x[i+2] = x[i+1] -  $\left( \frac{x[i+1] - x[i]}{fx[i+1] - fx[i]} \right) * fx[i+1]$

Step 6: increment in i

Step 7: Write "The Root is" x[i]