

October 4

Problem: Missing Number

Problem Statement: Given an array `nums` containing `n` distinct numbers in the range `[0, n]`, return the only number in the range that is missing from the array.

Link to problem:

<https://leetcode.com/problems/missing-number/>

Example 1:

Input: `nums = [3,0,1]`

Output: 2

Explanation: `n = 3` since there are 3 numbers, so all numbers are in the range `[0,3]`. 2 is the missing number in the range since it does not appear in `nums`.

Example 2:

Input: `nums = [0,1]`

Output: 2

Explanation: `n = 2` since there are 2 numbers, so all numbers are in the range `[0,2]`. 2 is the missing number in the range since it does not appear in `nums`.

Example 3:

Input: `nums = [9,6,4,2,3,5,7,0,1]`

Output: 8

Explanation: `n = 9` since there are 9 numbers, so all numbers are in the range `[0,9]`. 8 is the missing number in the range since it does not appear in `nums`.

Solution:

```
class Solution {
    public int missingNumber(int[] nums) {
        int ans = 0;

        // XOR all numbers from 0 to n
        for (int i = 0; i <= nums.length; i++) {
            ans = ans ^ i;
        }

        // XOR all numbers in the array
        for (int i : nums) {
            ans = ans ^ i;
        }

        // The result is the missing number
        return ans;
    }
}
```

}

Explanation:

- **Concept:** The XOR operation has a useful property that $a \oplus a = 0$ and $a \oplus 0 = a$. This can be used to cancel out all the numbers that appear in both the array and the range $[0, n]$, leaving only the missing number.
- **Step 1:** First, we XOR all numbers from 0 to n (since the numbers are in the range $[0, n]$, there are $n+1$ numbers).
- **Step 2:** Then, we XOR all the numbers in the given array `nums`.
- **Step 3:** By XORing the result of the first and second steps, all numbers that appear in both the range $[0, n]$ and the array will cancel each other out, leaving only the missing number.

Time Complexity:

- $O(n)$, where n is the number of elements in the array. We iterate through the array twice (once for XOR from 0 to n and once for XOR over the array).

Space Complexity:

- $O(1)$, since we use only a single extra variable `ans` for computation.
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