

October 12

Recursion Problems

Problem 1: Generate Parentheses

Problem Statement:

Given n pairs of parentheses, write a function to generate all combinations of well-formed parentheses.

Link to problem:

<https://leetcode.com/problems/generate-parentheses/description/>

Example 1:

Input: n = 3

Output: ["((())", "(())", "()()", "()(())", "()()"]

Example 2:

Input: n = 1

Output: ["()"]

Solution:

```
class Solution {
    public List<String> generateParenthesis(int n) {
        List<String> result = new ArrayList<>();
        generateCombinations(result, "", 0, 0, n);
        return result;
    }

    // Recursive helper function to generate combinations
    private void generateCombinations(List<String> result, String current, int open, int close,
int max) {
        // Base case: if the current string has reached the maximum length
        if (current.length() == max * 2) {
            result.add(current);
            return;
        }

        // Recursion case: add an opening bracket if there are any left
        if (open < max) {
            generateCombinations(result, current + "(", open + 1, close, max);
        }
    }
}
```

```

// Recursion case: add a closing bracket if it doesn't exceed the number of open brackets
if (close < open) {
    generateCombinations(result, current + ")", open, close + 1, max);
}
}
}

```

Explanation:

- **Initial Call:**
 - We start with an empty string and call the recursive function `generateCombinations(result, "", 0, 0, n)` where `open = 0` and `close = 0` represent the number of opening and closing parentheses placed so far.
- **Base Case:**
 - When the current string has reached the length of $2 * n$ (i.e., when we have placed all n opening and n closing parentheses), we add the string to the result list.
- **Recursive Cases:**
 - If the number of opening parentheses used is less than n , we can add another opening parenthesis (.
 - If the number of closing parentheses used is less than the number of opening parentheses, we can add a closing parenthesis).

This ensures that only valid combinations are generated.

Time Complexity:

$O(4^n / \sqrt{n})$: This is a known complexity for generating all valid combinations of parentheses, as the Catalan number bounds the number of valid strings.

Space Complexity:

$O(n)$: The recursion depth can go up to n , and the space used to store the result list is proportional to the number of combinations.

Problem 2: Permutations

Problem Statement:

Given an array of distinct integers, return all the possible permutations. You can return the answer in any order.

Link to problem:

<https://leetcode.com/problems/permutations/description/>

Example 1:

Input: nums = [1,2,3]

Output: [[1,2,3],[1,3,2],[2,1,3],[2,3,1],[3,1,2],[3,2,1]]

Example 2:

Input: nums = [0,1]

Output: [[0,1],[1,0]]

Solution:

```
class Solution {
public List<List<Integer>> permute(int[] nums) {
    List<List<Integer>> result = new ArrayList<>();
    backtrack(result, new ArrayList<>(), nums);
    return result;
}

// Backtracking helper function
private void backtrack(List<List<Integer>> result, List<Integer> tempList, int[] nums) {
    // Base case: if the temporary list size equals the original list size
    if (tempList.size() == nums.length) {
        result.add(new ArrayList<>(tempList)); // Add the current permutation to the result
    } else {
        for (int i = 0; i < nums.length; i++) {
            // Skip used elements
            if (tempList.contains(nums[i])) continue;
            tempList.add(nums[i]); // Choose
            backtrack(result, tempList, nums); // Recurse
            tempList.remove(tempList.size() - 1); // Un-choose
        }
    }
}
}
```

Explanation:**• Initialization:**

- We create a List<List<Integer>> result to store all the permutations.

- We call the backtrack function with the initial parameters: result, an empty tempList, and the input array nums.
 - **Base Case:**
 - The base case checks if the size of tempList is equal to the size of nums. If true, it means we've formed a complete permutation.
 - We then add a copy of tempList to result using `new ArrayList<>(tempList)`.
 - **Recursive Cases:**
 - We iterate through each element in nums.
 - **Checking for Used Elements:** We skip elements that are already in tempList to avoid duplicates.
 - If the element is not used, we add it to tempList.
 - We recursively call backtrack to continue building the permutation.
 - **Backtracking:** After the recursive call, we remove the last added element from tempList using `tempList.remove(tempList.size() - 1)` to backtrack and try other possibilities.
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Example Walkthrough

Input: nums = [1, 2, 3]

- Starting with an empty tempList, the process proceeds as follows:
 1. Add 1 → tempList = [1]
 - Add 2 → tempList = [1, 2]
 - Add 3 → tempList = [1, 2, 3] (Base case reached; add [1, 2, 3] to result)
 - Backtrack, remove 3, tempList = [1, 2]
 - Add 3 → tempList = [1, 3]
 - Add 2 → tempList = [1, 3, 2] (Base case reached; add [1, 3, 2] to result)
 - Backtrack, remove 2, tempList = [1, 3]
 - Backtrack to tempList = [1]
 2. Backtrack to empty tempList, add 2 → tempList = [2]
 - Add 1 → tempList = [2, 1]
 - Add 3 → tempList = [2, 1, 3] (Base case reached; add [2, 1, 3] to result)
 - Add 3 → tempList = [2, 3]
 - Add 1 → tempList = [2, 3, 1] (Base case reached; add [2, 3, 1] to result)
 3. Backtrack to empty tempList, add 3 → tempList = [3]
 - Add 1 → tempList = [3, 1]
 - Add 2 → tempList = [3, 1, 2] (Base case reached; add [3, 1, 2] to result)

- Add 2 \rightarrow tempList = [3, 2]
 - Add 1 \rightarrow tempList = [3, 2, 1] (Base case reached; add [3, 2, 1] to result)

Final Result: [[1, 2, 3], [1, 3, 2], [2, 1, 3], [2, 3, 1], [3, 1, 2], [3, 2, 1]].

Time Complexity:

$O(n! * n)$: The $n!$ factor comes from the number of permutations, and n comes from the time taken to copy the current permutation into the result list.

Space Complexity:

$O(n)$: The space used by the temporary list and the recursion stack can go up to $O(n)$.
