

## Vectors, trigonometry and math:

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k} ; A = \|\vec{A}\| = |\vec{A}| = \sqrt{A_x^2 + A_y^2 + A_z^2}$$

$$\vec{A} + \vec{B} = (A_x + B_x)\hat{i} + (A_y + B_y)\hat{j} + (A_z + B_z)\hat{k}$$

$$\hat{A} = \frac{\vec{A}}{\|\vec{A}\|} ; \vec{A} \cdot \vec{B} = AB \cos \theta ; \vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z ;$$

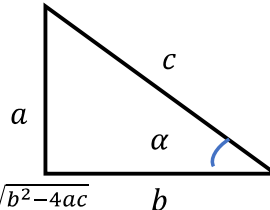
$$\vec{A} \times \vec{B} = AB \sin \theta \hat{n} ;$$

$$\vec{A} \times \vec{B} = \hat{i}(A_y B_z - A_z B_y) - \hat{j}(A_x B_z - A_z B_x) + \hat{k}(A_x B_y - A_y B_x)$$

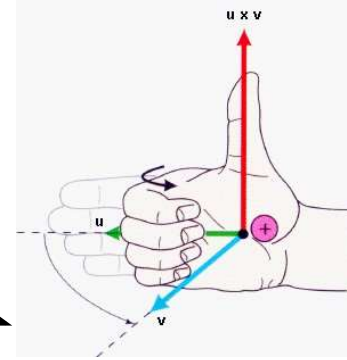
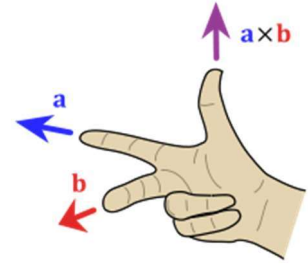
**Derivative:**  $\frac{d(ct^n)}{dt} = c n t^{n-1} ;$  where  $c$  is a constant

Trigonometry:  $\sin \alpha = \frac{a}{c} ; \cos \alpha = \frac{b}{c} ; \tan \alpha = \frac{a}{b}$

$$c^2 = a^2 + b^2$$



Quadratic equation  $ax^2 + bx + c = 0 ; x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$



## Prefixes and abbreviations for Powers of 10:

$10^{-12}$  pico (p);  $10^{-9}$  nano(n);  $10^{-6}$  micro( $\mu$ );  $10^{-3}$  mili(m);  $10^{-2}$  centi(c);  $10^3$  kilo(k)

**International System of Units:** Mass: kg; Length: m; Time: s

## Chapter 2

Average velocity  $v_{av-x} = \frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1} ;$  Instantaneous velocity  $v_x = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$

Average acceleration  $a_{av-} = \frac{\Delta v_x}{\Delta t} = \frac{v_{x2} - v_{x1}}{t_2 - t_1} ;$  Instantaneous acceleration  $a_x = \frac{dv_x}{dt}$

Equations of motion with constant acceleration:

$$v_x = v_{0x} + a_x t ; x = x_0 + v_{0x} t + \frac{1}{2} a_x t^2$$

$$v_x^2 = v_{0x}^2 + 2 a_x (x - x_0) ; x - x_0 = \frac{1}{2} (v_{0x} + v_x) t$$

Free falling bodies,  $a = g = 9.8 \text{ m/s}^2$

$$v_x = v_{0x} + \int_0^t a_x dt ; x = x_0 + \int_0^t v_x dt$$

## Chapter 3

Average velocity  $\vec{v}_{av} = \frac{\Delta \vec{r}}{\Delta t} = \frac{\vec{r}_2 - \vec{r}_1}{t_2 - t_1}$

Instantaneous velocity  $\vec{v} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{r}}{\Delta t} = \frac{d\vec{r}}{dt} ; v_x = \frac{dx}{dt} ; v_y = \frac{dy}{dt} ; v_z = \frac{dz}{dt}$

Average acceleration  $\vec{a}_{av} = \frac{\Delta \vec{v}}{\Delta t} = \frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1}$

Instantaneous acceleration  $\vec{a} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{v}}{\Delta t} = \frac{d\vec{v}}{dt}$ ;  $a_x = \frac{dv_x}{dt}$ ;  $a_y = \frac{dv_y}{dt}$ ;  $a_z = \frac{dv_z}{dt}$

Projectile motion:  $x = x_0 + (v_0 \cos \alpha_0)t$ ;  $y = y_0 + (v_0 \sin \alpha_0)t - \frac{1}{2}gt^2$

$$v_x = v_0 \cos \alpha_0$$
;  $v_y = v_0 \sin \alpha_0 - gt$

Circular motion:  $a_{rad} = \frac{v^2}{R}$ ;  $a_{rad} = \frac{4\pi^2 R}{T^2}$

Relative velocity:  $\vec{v}_{P/A} = \vec{v}_{P/B} + \vec{v}_{B/A}$

## **Chapter 4**

Force as a vector  $\vec{R} = \sum \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$

Newton's 2<sup>nd</sup> law  $\sum \vec{F} = m\vec{a}$ ;  $\sum F_x = ma_x$ ;  $\sum F_y = ma_y$ ;  $\sum F_z = ma_z$

Weight  $\vec{w} = m\vec{g}$

Newton's 3<sup>rd</sup> law  $\vec{F}_{A \text{ on } B} = -\vec{F}_{B \text{ on } A}$

## **Chapter 5**

Kinetic Friction Force  $f_k = \mu_k n$ ; Static Friction Force  $f_s \leq (f_s)_{max} = \mu_s n$

## **Chapter 6**

Work:  $W = \vec{F} \cdot \vec{s} = F s \cos \phi$

Kinetic Energy:  $K = \frac{1}{2}mv^2$

Work-energy theorem:  $W_{Total} = K_2 - K_1 = \Delta K$

Work done by a varying Force, straight line motion:  $W = \int_{x_1}^{x_2} F_x dx$

Power:  $P_{av} = \frac{\Delta W}{\Delta t}$ ;  $P = \lim_{\Delta t \rightarrow 0} \frac{\Delta W}{\Delta t} = \frac{dW}{dt}$