

# The Name of the Title Is Hope

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## Abstract

abstract

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## 1 Introduction

## 2 Related Work

## 3 Auditing Framework

### 3.1 Preliminaries

A row  $r_i$  is a lookup table or dictionary. A database  $\mathcal{D} = \{r_1, r_2, \dots\}$  is a collection of rows. The attributes of  $\mathcal{D}$  is  $\mathcal{A} = \{A_1, A_2, \dots\}$ . The domain of  $A_i$  is  $\Omega_i$ .

Let  $C \subseteq \mathcal{A}$ . Let  $\Omega_C = \prod_{i \in C} \Omega_i$ . The marginal  $[1, 5]$  on  $C$  is a vector  $\mu \in \mathbb{R}^{|\Omega_C|}$ , indexed by domain element  $t \in \Omega_C$ , such that each entry is a count  $\mu_t = \sum_{x \in \mathcal{D}} \mathbb{1}[x_C = t]$  where  $\mathbb{1}$  is the indicator function. Let  $M_C(\mathcal{D})$  be the function that computes the marginal on  $C$ , i.e.,  $\mu = M_C(\mathcal{D})$ .

A randomized mechanism is a randomized algorithm  $M$  that takes a database  $\mathcal{D}$  and, after, introducing noise, outputs some results in set  $R$ .

The  $p$ -norm is denoted by  $L_p$  and the  $p$ -norm of a vector  $x$  is denoted by  $\|x\|_p$ .

The normal distribution or Gaussian distribution with mean  $\mu$  and standard deviation  $\sigma$  is denoted by  $\mathcal{N}(\mu, \sigma^2)$ .

The Kullback–Leibler divergence between probability distributions  $P$  and  $Q$  is denoted by  $D_{KL}(P\|Q)$ . The generalization of it, Rényi divergence[7], of order  $\alpha$  is denoted by  $D_\alpha(P\|Q)$ .

### 3.2 Fairness Measures

### 3.3 Differential Privacy

*Definition 3.1 (Sensitivity[3]).* Let  $f$  be a function that takes a database  $\mathcal{D}$  and outputs a vector  $\mathbb{R}^p$ . The  $L_2$  sensitivity of  $f$  is for all databases  $\mathcal{D}_1, \mathcal{D}_2$  that differ in exactly one row:

$$\Delta_f^2 = \max_{\mathcal{D}_1, \mathcal{D}_2} \|f(\mathcal{D}_1) - f(\mathcal{D}_2)\|_p$$

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*Definition 3.2 (Gaussian Mechanism[3]).* Let  $f$  be a function that takes a database  $\mathcal{D}$  and outputs a vector  $\mathbb{R}^p$ . The Gaussian Mechanism  $M$  adds Gaussian noise with scale  $\sigma$  to each of the  $p$  outputs:

$$M(\mathcal{D}) = f(\mathcal{D}) + \mathcal{N}(0, \sigma^2 \mathbb{I})$$

*Definition 3.3 (Differential Privacy (DP) [2, 3, 5]).* A randomized mechanism  $M$  satisfies  $(\epsilon, \delta)$ -DP if, for all databases  $\mathcal{D}_1, \mathcal{D}_2$  that differ in exactly one row and for all subsets  $S$  of  $R$ , we have

$$\Pr[M(\mathcal{D}_1) \in S] \leq e^\epsilon \Pr[M(\mathcal{D}_2) \in S] + \delta$$

*Definition 3.4 (Rényi Differential Privacy (RDP)).* A randomized mechanism  $M$  satisfies  $(\alpha, \gamma)$ -RDP for  $\alpha \geq 1$  and  $\gamma \geq 1$  if, for all databases  $\mathcal{D}_1, \mathcal{D}_2$  that differ in exactly one row, we have

$$D_\alpha(M(\mathcal{D}_1)\|M(\mathcal{D}_2)) \leq \gamma$$

THEOREM 3.5 (RDP OF THE GAUSSIAN MECHANISM[4, 6]). *The Gaussian Mechanism satisfies  $(\alpha, \alpha \frac{\Delta_f^2}{2\sigma^2})$ -RDP.*

## 3.4 Synthetic Data

## 4 Methodology

### 4.1 Differential Private Synthetic Data

### 4.2 Fairness Checker

### 4.3 Implementation

## 5 Results

### 5.1 Adult Income Dataset

### 5.2 COMPAS Dataset

### 5.3 One More Dataset

## 6 Discussion

### 6.1 Accuracy

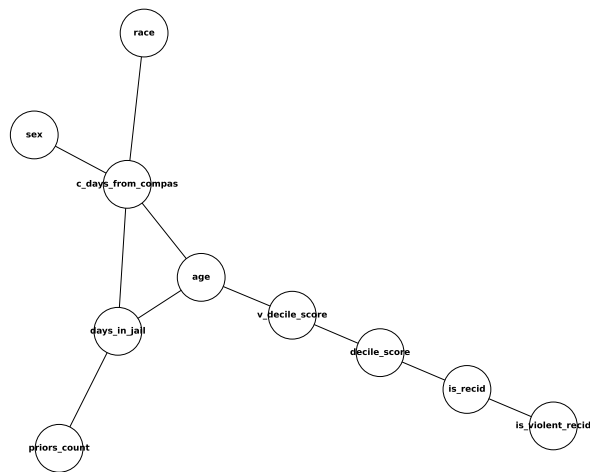
### 6.2 Impossibility

## 7 Conclusion

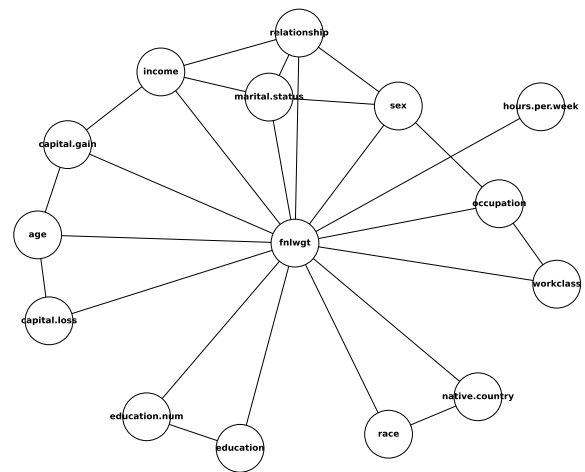
Some examples. A paginated journal article [? ]

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**Figure 1: 1907 Franklin Model D roadster. Photograph by Harris & Ewing, Inc. [Public domain], via Wikimedia Commons. (<https://goo.gl/VLCRBB>).**



**Figure 2: 1907 Franklin Model D roadster. Photograph by Harris & Ewing, Inc. [Public domain], via Wikimedia Commons. (<https://goo.gl/VLCRBB>).**

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