

Rationalizing the Denominator of a Radical Expression

• Example 1

Simplify and rationalize the denominator.

$$\frac{\sqrt{15}}{\sqrt{35}}$$

We begin by rewriting, using properties of radicals and simplifying.

$$\frac{\sqrt{15}}{\sqrt{35}} = \sqrt{\frac{15}{35}}$$
$$= \sqrt{\frac{3}{7}} = \frac{\sqrt{3}}{\sqrt{7}}$$

To rationalize the denominator, we multiply both numerator and denominator by $\sqrt{7}$ and simplify the result.

$$\frac{\sqrt{3}}{\sqrt{7}} \frac{\sqrt{7}}{\sqrt{7}} = \frac{\sqrt{3}\sqrt{7}}{7}$$
$$= \frac{\sqrt{21}}{7}$$

• • CHECK YOURSELF 1

Simplify and rationalize the denominator.

$$\frac{\sqrt{12}}{\sqrt{33}}$$

CHECK YOURSELF ANSWER

1.
$$\frac{2\sqrt{11}}{11}$$

Section

ANSWERS

1.

2.

3.

4.

5.

6.

7.

8.

9.

10.

11.

12.

Simplify and rationalize the denominator of each of the following.

1.
$$\frac{\sqrt{20}}{\sqrt{30}}$$

2.
$$\frac{\sqrt{6}}{\sqrt{18}}$$

3.
$$\frac{\sqrt{14}}{\sqrt{28}}$$

4.
$$\frac{\sqrt{13}}{\sqrt{39}}$$

5.
$$\frac{\sqrt{8}}{\sqrt{160}}$$

6.
$$\frac{\sqrt{40}}{\sqrt{52}}$$

7.
$$\frac{\sqrt{10}}{\sqrt{55}}$$

8.
$$\frac{\sqrt{2}}{\sqrt{6}}$$

9.
$$\frac{\sqrt{56}}{\sqrt{88}}$$

10.
$$\frac{\sqrt{144}}{\sqrt{171}}$$

11.
$$\frac{\sqrt{72}}{\sqrt{117}}$$

12.
$$\frac{\sqrt{35}}{\sqrt{77}}$$