

Algorithms & Data Structures I

Lesson 4: ADT, stacks, queues

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Data structures

A data structure is a (often *non-obvious*) way to organize information to enable *efficient* computation over that information

A data structure supports certain *operations*, each with a:

- **Meaning**: what does the operation do/return
- **Performance**: how efficient is the operation

Examples:

- **List** with operations **insert** and **delete**
- **Stack** with operations **push** and **pop**

Trade-offs

A data structure strives to provide many useful, efficient operations

But there are unavoidable trade-offs:

- Time vs. space
- One operation more efficient if another less efficient
- Generality vs. simplicity vs. performance

We ask ourselves questions like:

- Does this support the operations I need efficiently?
- Will it be easy to use (and reuse), implement, and debug?
- What assumptions am I making about how my software will be used? (E.g., more lookups or more inserts?)

Terminology

- Abstract Data Type (ADT)
 - Mathematical description of a “thing” with set of operations
 - Not concerned with implementation details
- Algorithm
 - A high level, language-independent description of a step-by-step process
- Data structure
 - A specific organization of data and family of algorithms for implementing an ADT
- Implementation of a data structure
 - A specific implementation in a specific language

Example: Stacks

- The **Stack** ADT supports operations:
 - **isEmpty**: have there been same number of pops as pushes
 - **push**: adds an item to the top of the stack
 - **pop**: raises an error if empty, else removes and returns most-recently pushed item not yet returned by a pop
 - **peek**: the same as **pop** but without removing the item
 - What else?
- A Stack data structure could use a linked-list or an array and associated algorithms for the operations
- One implementation is in the library `java.util.Stack`

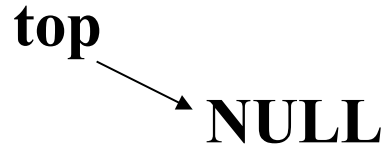
Why useful

The Stack ADT is a useful abstraction because:

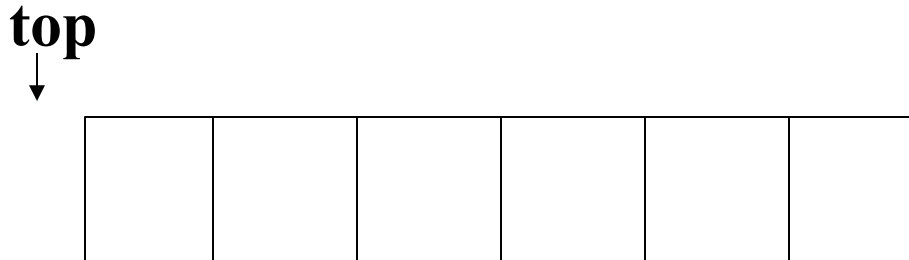
- It arises **all the time** in programming (e.g., see Weiss 3.6.3)
 - Recursive function calls
 - Syntax analysis of pairwise tags (XML)
 - Evaluating postfix notation: $3\ 4\ +\ 5\ *$
 - Clever: Infix $((3+4) * 5)$ to postfix conversion (see text)
- We can code up a **reusable library**
- We can **communicate** in high-level terms
 - “Use a stack and push numbers, popping for operators...”
 - Rather than, “create an array and keep indices to the...”

Stack Implementations

- stack as a linked list

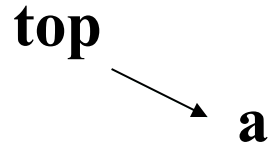


- stack as an array

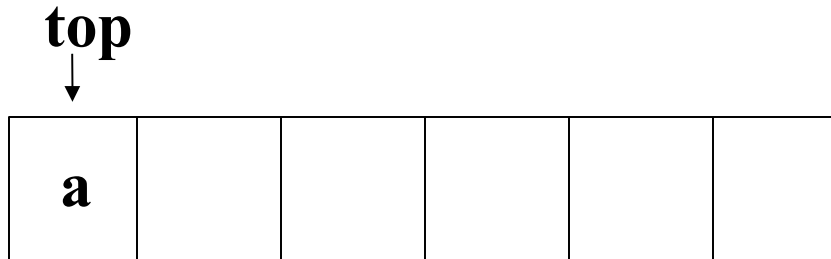


Stack Implementations

- stack as a linked list

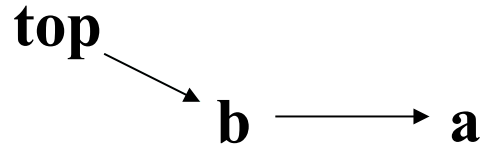


- stack as an array

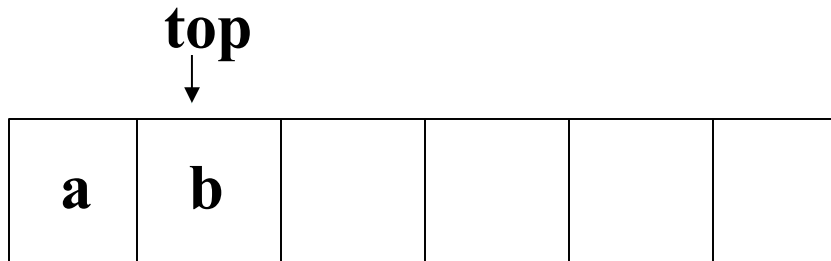


Stack Implementations

- stack as a linked list



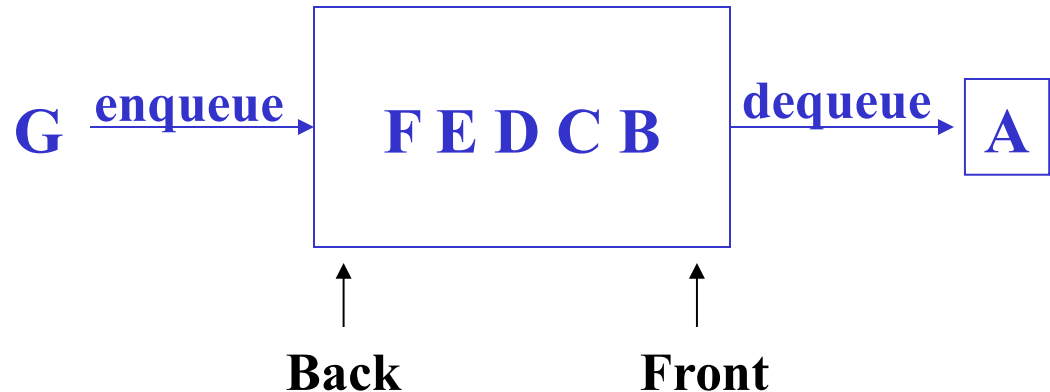
- stack as an array



The Queue ADT

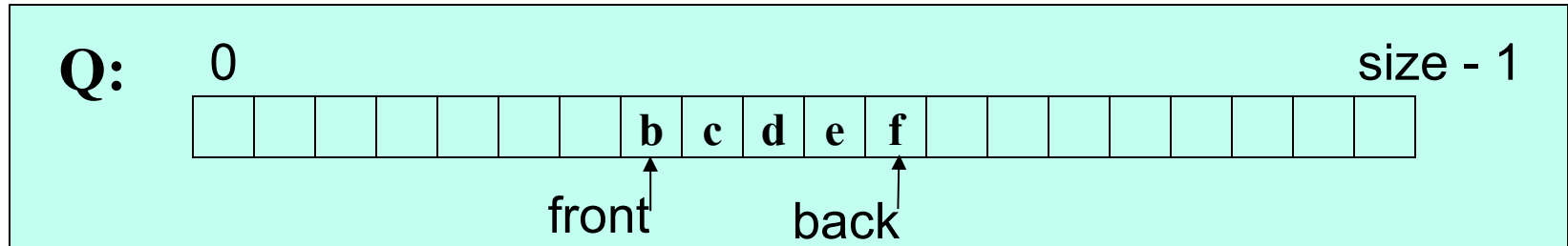
- Operations
 - `create`
 - `destroy`
 - `enqueue`
 - `dequeue`
 - `is_empty`

What else?



- Just like a stack except:
 - Stack: LIFO (last-in-first-out)
 - Queue: FIFO (first-in-first-out)

Circular Array Queue Data Structure



// Basic idea only!

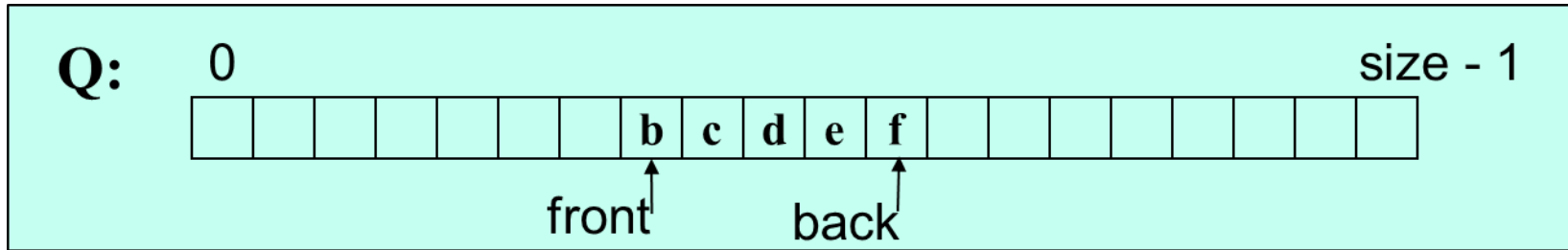
```
enqueue(x) {  
    next = (back + 1) % size  
    Q[next] = x;  
    back = next  
}
```

// Basic idea only!

```
dequeue() {  
    x = Q[front];  
    front = (front + 1) % size;  
    return x;  
}
```

- What if **queue** is empty?
 - Enqueue?
 - Dequeue?
- What if **array** is full?
- How to *test* for empty?
- What is the *complexity* of the operations?
- Can you find the k^{th} element in the queue?

Circular Array Example



enqueue('g')

o1 = dequeue()

o4 = dequeue()

o2 = dequeue()

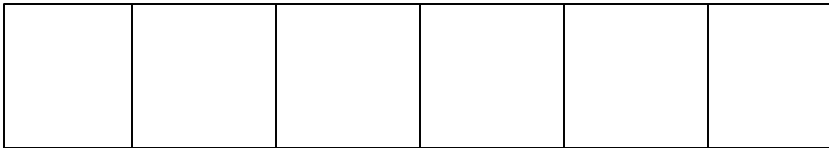
o5 = dequeue()

o3 = dequeue()

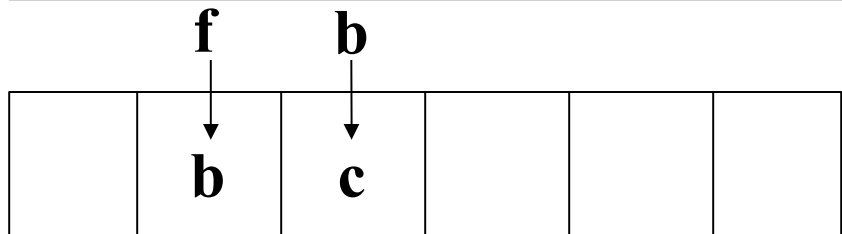
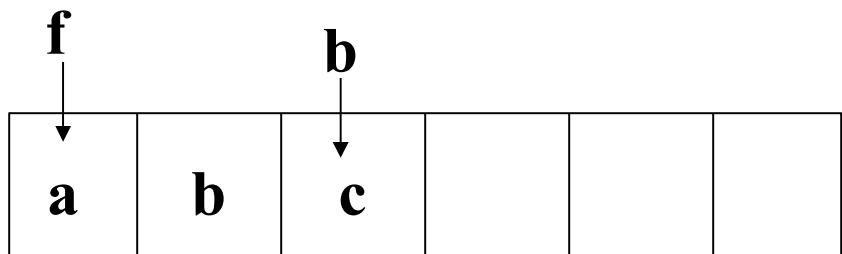
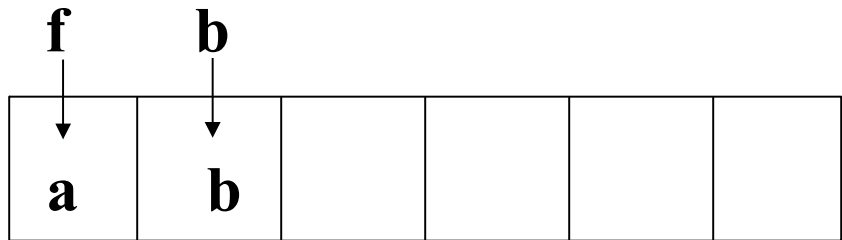
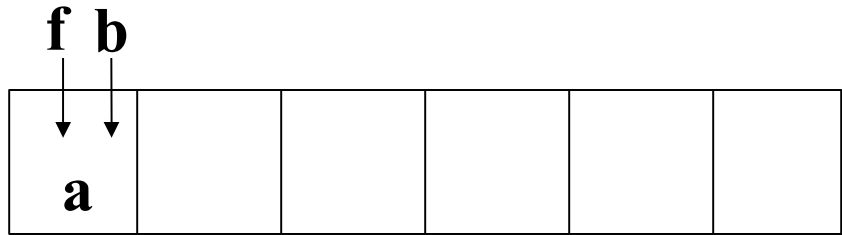
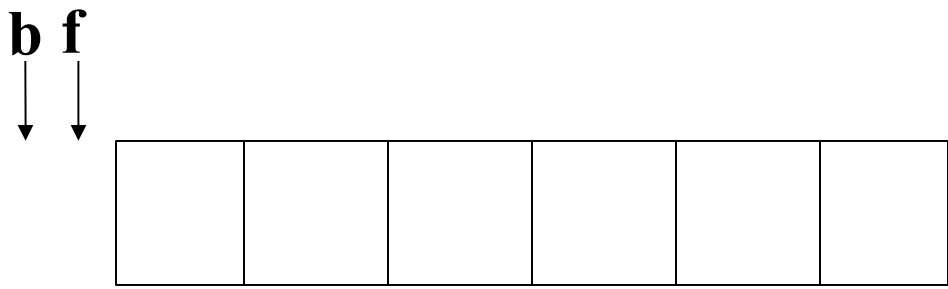
o6 = dequeue()

In Class Practice

b f
↓ ↓



```
enqueue('a')  
enqueue('b')  
enqueue('c')  
o = dequeue()  
o = dequeue()  
enqueue('d')  
enqueue('e')  
enqueue('f')  
enqueue('g')  
enqueue('h')  
enqueue('i')
```

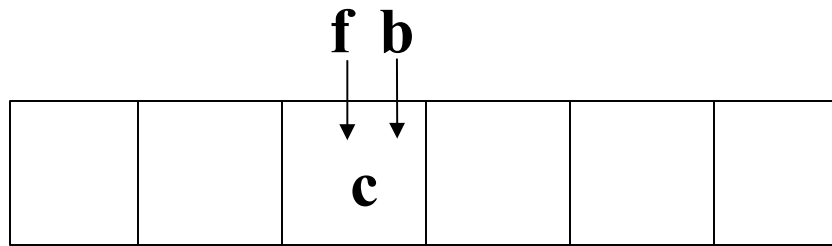


enqueue('a')

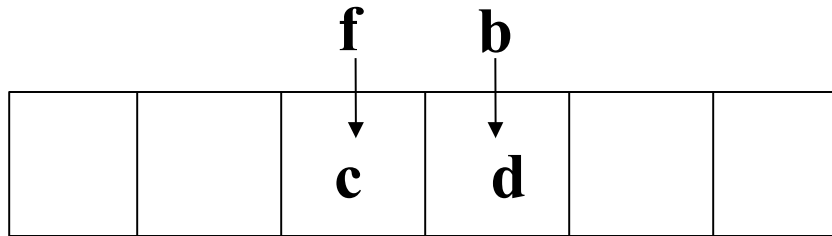
enqueue('b')

enqueue('c')

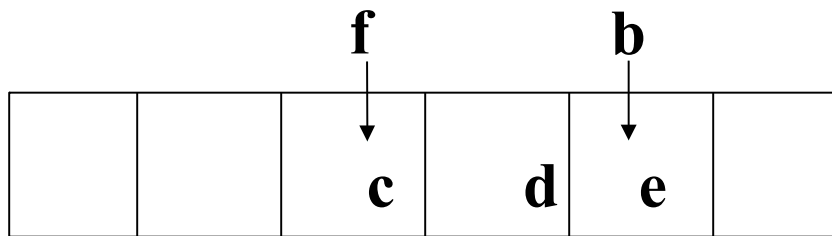
o = dequeue()



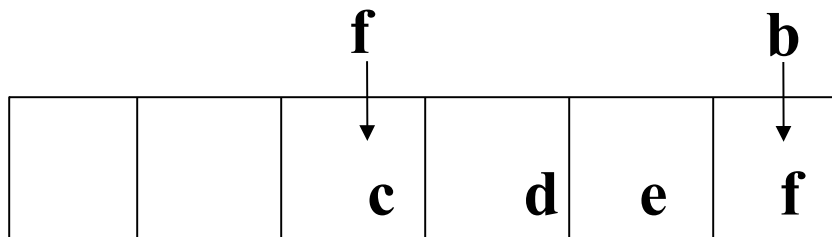
o = dequeue



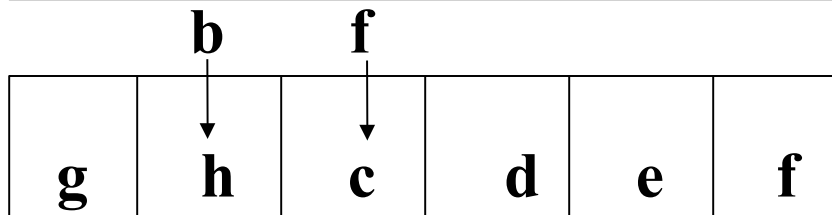
enqueue('d')



enqueue('e')

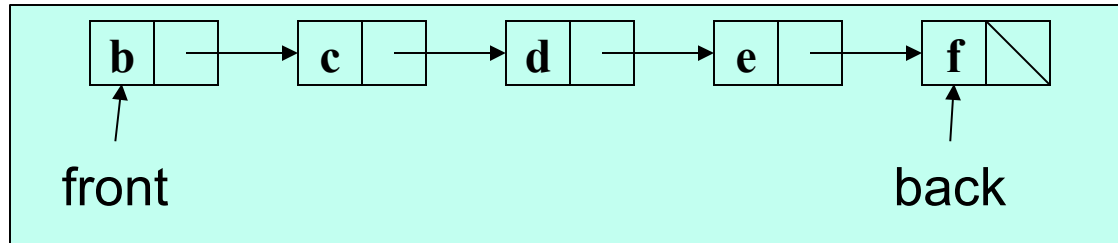


enqueue('f')



enqueue('g'), enqueue('h')

Linked List Queue Data Structure



```
// Basic idea only!
```

```
enqueue(x) {  
    back.next = new Node(x);  
    back = back.next;  
}
```

```
// Basic idea only!
```

```
dequeue() {  
    x = front.item;  
    front = front.next;  
    return x;  
}
```

- What if **queue** is empty?
 - Enqueue?
 - Dequeue?
- Can **list** be full?
- How to *test* for empty?
- What is the *complexity* of the operations?
- Can you find the k^{th} element in the queue?

Circular Array vs. Linked List

Array

- May waste unneeded space or run out of space
- Space per element excellent
- Operations very simple / fast
- Constant-time access to k^{th} element (not in ADT!!)

List

- Always just enough space
- But more space per element
- Operations very simple / fast
- No constant-time access to k^{th} element (not in ADT!!)

Conclusion

- Abstract data structures allow us to define a new data type and its operations.
- Each abstraction will have one or more implementations.
- Which implementation to use depends on the application, the expected operations, the memory and time requirements.
- Both stacks and queues have array and linked implementations.
- We'll look at other ordered-queue implementations later.