Handbook

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1 Grafos

1.1 Dinic

Insertar utilidad del algoritmo:

```
struct edge{
int x, y, flow;
3 };
5 int ans;
6 vector < edge > edges;
7 vector < vector < int > > grafo;
8 vector <int > sn;
void addEdge(int x, int y, int flow){
   grafo[x].PB(edges.size());
11
    edges.PB({x, y, flow});
12
13
    grafo[y].PB(edges.size());
14
    edges.PB({y, x, 0});
15
16 }
17
int bfs(int &ori, int &target){
    int x = ori, y, flow;
19
20
    FOR(i, 0, target + 1) sn[i] = INF;
21
22
23
    sn[x] = 0;
    deque<int> q(1, x);
24
25
    while(!q.empty()){
26
27
      x = q.F(); q.P_F();
28
      for(auto &e: grafo[x]){
29
        auto &edge = edges[e];
30
         y = edge.y;
31
         flow = edge.flow;
32
33
        if(flow <= 0) continue;</pre>
34
        if(sn[y] != INF) continue;
35
         sn[y] = sn[x] + 1;
36
37
         q.PB(y);
38
39
    return sn[target];
41
42 }
43
int dfs(int ori, int &target, int min_flow){
   int flow = INF, y;
46
47
    for(auto &e_id: grafo[ori]){
auto &e = edges[e_id];

y = e.y;
```

```
50
       if(sn[y] != 1 + sn[ori]) continue;
if(e.flow <= 0) continue;</pre>
51
52
53
       if(y == target){
54
         flow = min(min_flow, e.flow);
ans += flow;
55
56
57
         edges[e_id].flow -= flow;
         edges[e_id^1].flow += flow;
58
         return flow;
59
60
61
62
       flow = dfs(y, target, min(min_flow, e.flow));
63
       if(flow != INF){
64
         edges[e_id].flow -= flow;
65
         edges[e_id^1].flow += flow;
66
67
         return flow;
68
      }
69
    return flow;
71
72 }
```

2 Strings

2.1 Función Z

Insertar utilidad del algoritmo:

C++:

```
vector<int> z_function(string s) {
   int n = (int) s.length();
   vector<int> z(n);

for (int i = 1, l = 0, r = 0; i < n; ++i) {
   if (i <= r)
        z[i] = min (r - i + 1, z[i - 1]);

   while (i + z[i] < n && s[z[i]] == s[i + z[i]])
   ++z[i];

   if (i + z[i] - 1 > r)
        l = i, r = i + z[i] - 1;

return z;

}
```

2.2 KMP

Insertar utilidad del algoritmo:

C++:

```
vector<int> z;

void kmp(string &s){
   int j, n = s.size();
   z.resize(n);

FOR(i, 1, n){
   j = z[i - 1];
   while(j > 0 and s[i] != s[j]) j = z[j - 1];
   if(s[i] == s[j]) j++;
   z[i] = j;
}
```

2.3 Suffix array

Devuelve un arreglo con el orden lexicográfico de los sufijos de un string S

```
vector < int > p, c;
void count_sort(vector < int > &p, vector < int > &c){
   int n = p.size();
   vector < int > cnt(n), p_new(n), pos(n);
   pos[0] = 0;
   for(auto x : c) cnt[x]++;
```

```
for(int i = 1 ; i < n ; ++i) pos[i] = pos[i - 1] + cnt[i - 1];</pre>
7
       for(auto x : p){
8
           int i = c[x];
9
           p_new[pos[i]] = x;
10
           pos[i]++;
11
       }
12
13
       p = p_new;
14 }
vector<int> suffix_array(string &s){
16
       s+=" ";
       int n = s.size();
17
18
       p.resize(n);
       c.resize(n):
19
       vector<pair<char, int>> a(n);
20
       for(int i = 0; i < n; ++i) a[i] = {s[i], i};
21
       sort(a.begin(), a.end());
22
23
       for(int i = 0 ; i < n ; ++i) p[i] = a[i].second;</pre>
       c[p[0]] = 0;
24
25
       for(int i = 1 ; i < n ; ++i)</pre>
         c[p[i]] = a[i].first == a[i - 1].first ? c[p[i - 1]] : c[p[i - 1]] + 1;
26
       int k = 0, shift;
27
       while( (1<<k) < n ){</pre>
28
           shift = 1<<k;
29
           for(int i = 0 ; i < n ; ++i)
30
               p[i] = (p[i] - (1 << k) + n) % n;
31
           count_sort(p,c);
           vector < int > c_new(n);
33
           c_new[p[0]] = 0;
34
           for(int i = 1 ; i < n ; ++i){</pre>
35
               pair < int, int > prev = \{c[p[i - 1]], c[(p[i - 1] + shift) \% n]\};
36
               pair < int , int > now = {c[p[i]], c[(p[i] + shift) % n]};
37
               if(prev == now) c_new[p[i]] = c_new[p[i - 1]];
38
               else c_new[p[i]] = c_new[p[i - 1]] + 1;
39
           }
40
41
           c = c_new;
42
           k++;
       }
43
44
       return p;
45 }
  Java:
static int[]p, c;
public static class Suffix implements Comparable < Suffix > {
       int index, r, next;
3
4
       public Suffix(int index, int rank, int next){
           this.index = index; this.r = rank; this.next = next;
5
6
       public int compareTo(Suffix s){
           return r != s.r ? r - s.r : (next != s.next ? next - s.next : index - s.index);
8
9
10 }
public static int[] sort(int[] p, int[]c){
       int N = p.length;
12
       int[]cnt = new int[N], pos = new int[N], p_new = new int[N];;
13
14
       for(int e : c) cnt[e]++;
           for(int i = 1 ; i < N ; ++i) pos[i] = pos[i - 1] + cnt[i - 1];</pre>
15
           for(int x : p){
```

```
p_new[pos[c[x]]] = x; pos[c[x]]++;
17
          }
18
          p = p_new;
19
20
          return p;
21
public static int[] suffixArray(String s) {
23
      s+="$";
      int n = s.length();
24
      c = new int[n];
25
26
      p = new int[n];
      Suffix[] su = new Suffix[n];
27
      for (int i = 0; i < n; ++i) su[i] = new Suffix(i, s.charAt(i), 0);</pre>
28
      Arrays.sort(su);
29
30
      for(int i = 0 ; i < n ; ++i) p[i] = su[i].index;</pre>
      c[p[0]] = 0;
31
      for (int i = 1; i < n; ++i) c[p[i]] = su[i].r == su[i - 1].r ?c[p[i-1]] :c[p[i-1]] + 1;
32
      int k = 0, shift;
33
      while ((1 << k) < n) {
34
35
          shift = (1<<k);
         for(int i = 0 ; i < n ; ++i) p[i] = (p[i] - shift + n ) % n;</pre>
36
          p = sort(p, c);
37
          int[] c_new = new int[n];
38
          c_new[p[0]] = 0;
39
          for(int i = 1 ; i < n ; ++i)</pre>
40
             41
42
          c = c_new;
43
44
          ++k;
      }
45
46
      return p;
47 }
```

2.4 Longest Common Prefix on Suffixs

Devuelve un arreglo que contiene el largo del prefijo común máximo entre 2 sufijos i e i+1

```
C++:
```

static int[]p, c, LCP;

```
vector < int > lcp(vector < int > &p, vector < int > &c, string &s){
      int n = p.size();
      vector < int > lcp(n);
3
       int k = 0;
      for(int i = 0; i < n - 1; ++i){
5
           int pi = c[i];
6
           int j = p[pi - 1];
           while(s[i + k] == s[j + k]) k++;
8
9
           lcp[pi] = k;
           k = max(k - 1, 0);
10
11
      return lcp;
12
13 }
```

```
2
static int[] lcp(int[] p, int[]c, String s){
      int n = p.length;
4
      LCP = new int[n];
5
      int k = 0;
6
7
      for(int i = 0 ; i < n - 1 ; ++i){</pre>
          int pi = c[i];
          int j = p[pi - 1];
9
          while(s.charAt(i + k) == s.charAt(j + k)) k++;
10
          LCP[pi] = k;
11
          k = Math.max(k - 1, 0);
12
13
      return LCP;
14
15 }
```

2.5 Aho Corasick

```
int trie[MAX][26], nds = 1;
int fin[MAX], fail[MAX], sure_fail[MAX];
4 int add(string &s){
   int cr = 0, x;
6
    for(const auto &c: s){
      x = c - a';
9
      if(trie[cr][x] == 0) trie[cr][x] = nds++;
10
      cr = trie[cr][x];
11
12
13
    fin[cr] = 1;
14
15
    return cr;
16 }
17
void build(){
   int x, cr = 0;
19
20
21
    deque<int> q;
22
    q.PB(cr);
23
24
    while(!q.empty()){
      cr = q.F(); q.P_F();
25
26
      FOR(i, 0, 26){
27
        x = trie[cr][i];
28
29
        if(x) q.PB(x);
30
        if(cr == 0) continue;
31
        if(x == 0){
32
          trie[cr][i] = trie[fail[cr]][i];
33
34
          continue;
35
36
        fail[x] = trie[fail[cr]][i];
37
```

3 Búsqueda

3.1 Ternary Search

Insertar utilidad del algoritmo:

```
#define ld long double
3 ld ternary_search(ld l, ld r) {
        ld eps = 1e-9;
        ld m1, m2, f1, f2;
        while (r - 1 > eps) {
            m1 = 1 + (r - 1) / 3;

m2 = r - (r - 1) / 3;

f1 = f(m1);  //evaluates the function at m1

f2 = f(m2);  //evaluates the function at m2
9
10
             if (f1 < f2) 1 = m1;</pre>
11
12
              else r = m2;
13
14
        //return the maximum of f(x) in [1, r]
15
        return f(1);
17 }
```

4 Geometría

4.1 Convex Hull

Insertar utilidad del algoritmo:

```
C++:
```

```
struct pt {
double x, y;
3 };
5 int orientation(pt a, pt b, pt c) {
double v = a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y);
    if (v < 0) return -1; // clockwise</pre>
    if (v > 0) return +1; // counter-clockwise
9
    return 0;
10 }
11
bool cw(pt a, pt b, pt c, bool include_collinear) {
   int o = orientation(a, b, c);
13
    return o < 0 || (include_collinear && o == 0);</pre>
14
15 }
bool ccw(pt a, pt b, pt c, bool include_collinear) {
int o = orientation(a, b, c);
    return o > 0 || (include_collinear && o == 0);
18
19 }
20
void convex_hull(vector<pt>& a, bool include_collinear = false) {
   if (a.size() == 1)
22
      return;
23
24
    sort(a.begin(), a.end(), [](pt a, pt b) {
25
      return make_pair(a.x, a.y) < make_pair(b.x, b.y);</pre>
26
    });
27
    pt p1 = a[0], p2 = a.back();
    vector < pt > up , down;
29
    up.push_back(p1);
30
31
    down.push_back(p1);
    for (int i = 1; i < (int)a.size(); i++) {</pre>
32
33
      if (i == a.size() - 1 || cw(p1, a[i], p2, include_collinear)) {
        while (up.size() >= 2){
34
          if(cw(up[up.size()-2], up[up.size()-1], a[i], include_collinear)) break;
35
36
          up.pop_back();
37
38
        up.push_back(a[i]);
39
      if (i == a.size() - 1 || ccw(p1, a[i], p2, include_collinear)) {
40
        while (down.size() >= 2){
41
          if(ccw(down[down.size()-2], down[down.size()-1], a[i], include_collinear)) break;
42
43
          down.pop_back();
44
45
         down.push_back(a[i]);
46
47
    if (include_collinear && up.size() == a.size()) {
```

```
reverse(a.begin(), a.end());
return;
}
a.clear();
for (int i = 0; i < (int)up.size(); i++)
a.push_back(up[i]);
for (int i = down.size() - 2; i > 0; i--)
a.push_back(down[i]);
}
```

4.2 Interseccion de lineas

C++:

```
struct line {
     double a, b, c;
2
3 };
5 const double EPS = 1e-9;
7 double det(double a, double b, double c, double d) {
     return a*d - b*c;
8
9 }
bool intersect(line m, line n, pt & res) {
      double zn = det(m.a, m.b, n.a, n.b);
12
     if (abs(zn) < EPS)
13
         return false;
14
     res.x = -det(m.c, m.b, n.c, n.b) / zn;
     res.y = -det(m.a, m.c, n.a, n.c) / zn;
16
17
      return true;
18 }
19
20 bool parallel(line m, line n) {
     return abs(det(m.a, m.b, n.a, n.b)) < EPS;</pre>
21
22 }
23
24 bool equivalent(line m, line n) {
    return abs(det(m.a, m.b, n.a, n.b)) < EPS</pre>
         26
27
28 }
```

4.3 Punto en polígono

```
const ld EPSILON = 0.000001;

struct pt{
   ld x, y;
  };

int orientation(pt &a, pt &b, pt &c){
   ld A, B, C;
```

```
9 A = -(b.y - a.y);
    B = b.x - a.x;
    C = b.y*a.x - a.y*b.x;
11
12
    ld result = A*c.x + B*c.y + C;
13
    if(result > 0.0) return 1; // Clockwise;
14
    if(result < 0.0) return -1; // Counter-clockwise;</pre>
15
    return 0; // Collinear.
16
17 }
18
19 bool coord_in_bounds(ld x, ld y, ld a){
20
   ld mini, maxi;
    mini = min(x, y);
21
22
    maxi = max(x, y);
23
    return (a + EPSILON >= mini and a - EPSILON <= maxi);</pre>
24
25 }
26
27 bool point_in_segment(pt &a, pt &b, pt &c){
    ld A, B, C;
28
    A = -(b.y - a.y);
29
    B = b.x - a.x;
30
    C = b.y*a.x - a.y*b.x;
31
32
    ld result = A*c.x + B*c.y + C;
33
34
    if(fabs(result) < EPSILON){</pre>
      if(coord_in_bounds(a.x, b.x, c.x) and coord_in_bounds(a.y, b.y, c.y)) return true;
35
36
37
    return false;
38
39 }
40
bool lines_intersect(pt &a, pt &b, pt &c, pt &d){
42
    int o1, o2, o3, o4;
    o1 = orientation(a, b, c);
43
44
    o2 = orientation(a, b, d);
    o3 = orientation(c, d, a);
45
    o4 = orientation(c, d, b);
47
48
    if(o1 != o2 and o3 != o4) return true;
49
    if(o1 == 0 and point_in_segment(a, b, c)) return true;
50
51
    if(o2 == 0 and point_in_segment(a, b, d)) return true;
    if(o3 == 0 and point_in_segment(c, d, a)) return true;
52
    if(o4 == 0 and point_in_segment(c, d, b)) return true;
53
54
    return false;
55
56 }
57
58 bool point_in_polygon(pt &P, vector<pt> &pts){
    pt aux = pt{INF, P.y};
59
    int intersections = 0, duplicatedIntersections = 0;
60
61
    FOR(i, 0, pts.size()){
62
63
      pt &p1 = pts[i];
       pt &p2 = pts[(i + 1)%pts.size()];
64
```

```
// Projected line pass across one point.
if(fabs(P.y - p1.y) < EPSILON and P.x - EPSILON < p1.x) duplicatedIntersections++;

intersections += lines_intersect(P, aux, p1, p2);

return (intersections - duplicatedIntersections) & 1;

return (intersections - duplicatedIntersections) & 1;</pre>
```

4.4 Ordenamiento por ángulo polar

C++:

```
struct pt {
2 11 x, y;
3 };
5 pt Ori = pt{0, 0};
7 // Vector Oa -> Ob
8 ll cross(pt a, pt b, pt 0){
    return a.x*(b.y-0.y)+b.x*(0.y-a.y)+0.x*(a.y-b.y);
10 }
11
int orientation(pt a, pt b, pt 0) {
if (v < 0) return -1; // clockwise
  if (v > 0) return +1; // counter-clockwise
15
   return 0;
16
17 }
18
bool firstHalf(pt a){
int o = orientation(pt{1, 0}, a, pt{0, 0});
   if(o == 0) o = a.x > 0 ? 1 : -1;
   return o > 0;
22
23 }
bool comp(pt &a, pt &b){
if(firstHalf(a) == firstHalf(b)) return cross(a, b, Ori) > 0;
   return firstHalf(a);
27
```

4.5 Área de polígono

```
1 ld area(const vector<pt>& fig) {
2    ld res = 0;
3    for (unsigned i = 0; i < fig.size(); i++) {
4       pt p = i ? fig[i - 1] : fig.back();
5       pt q = fig[i];
6       res += (p.x - q.x) * (p.y + q.y);
7    }
8    return fabs(res) / 2;
9 }</pre>
```

5 Matemáticas

5.1 Factorial modulo m

Permite calcular $n! \mod m$

C++:

```
vector<ll> factorial(ll N, ll p) {
vector<ll> fac(N + 1);
fac[0] = 1;
for (int i = 1; i <= N; i++)
fac[i] = fac[i - 1] * i % p;
return fac;
}</pre>
```

5.2 Exponenciacion binaria

Permite calcular $c \equiv a^b \pmod{m}$

C++:

```
long long binpow(long long a, long long b, long long m) {
    a %= m;
    long long res = 1;
    while (b > 0) {
        if (b & 1)
            res = res * a % m;
        a = a * a % m;
        b >>= 1;
    }
    return res;
}
```

5.3 Inverso Modular

Permite calcular $a^{-1} \mod m$, este número satisface $a \cdot a^{-1} \equiv 1 \pmod m$

Con el pequeño teorema de Fermat, siempre que m
 sea primo, se calcula $x \equiv a^{m-2} \pmod{m}$, siendo x su inverso modular.

Con el algoritmo de Euclides extendido, siempre y cuando gcd(a, m) = 1, se calculan x, y tal que ax + my = 1, por lo que $ax \equiv 1 \pmod{m}$, siendo x el inverso modular

```
1 //Usando binpow
2 ll inv(ll a, ll mod){
3     ll n = mod - 2;
4     ll ans = binpow(a, n, mod);
5     return ans;
```

```
6 }
7 //Usando euclides extendido
8 ll inv(ll a, ll b) {
9  pair<ll,ll> x = extend_euclid(a, b);
10  ll ans = x.first + (x.first < 0) * b;
11  return ans;
12 }</pre>
```

5.4 Inverso modular del factorial modulo m

Permite calcular $i!^{-1} \mod m$ para todo $1 \le i \le N$

C++:

```
vector<ll> factorial(ll N, ll p) {
   vector<ll> fac(N + 1);
   fac[0] = 1;
   for (int i = 1; i <= N; i++)
   fac[i] = fac[i - 1] * i % p;
   return fac;
}</pre>
```

5.5 Coeficientes binomiales modulo m

Calculo de $\binom{n}{k}$ mod m de múltiples formas

5.5.1 $nCk \mod m$ si m es primo

Para $m \ge 10^9$, se puede emplear la fórmula recursiva

$$\binom{n}{k} = \binom{n-1}{k-1} + \binom{n-1}{k} \mod m$$

O la formula explicita mediante factoriales

$$\binom{n}{k} = \frac{n!}{k!(n-k)!} \mod m = n! \, k!^{-1} (n-k)!^{-1} \mod m$$

```
/** Computa nCk mod p usando DP */
ll binomial(int n, int k, ll p) {
  vector<vector<ll>> dp(n + 1, vector<ll>> (k + 1, 0));

  for (int i = 0; i <= n; i++) {
    dp[i][0] = 1;
    if (i <= k)
        dp[i][i] = 1;
}

for (int i = 0; i <= n; i++)
  for (int j = 1; j <= min(i, k); j++)
    if (i != j)</pre>
```

```
dp[i][j] = (dp[i - 1][j - 1] + dp[i - 1][j]) % p;
12
13
      /** Puede retornarse el arreglo completo
      con la respuesta de todos los combinatorios desde
14
      nCO hasta nCk*/
15
    return dp[n][k];
16
17 }
18 /** Computa nCk mod p usando factoriales,
19 que pueden ser precomputados */
20 ll binomial(int n, int k, ll p) {
     vector<ll> fac = factorial(n, p); //Precomputarse
    vector<ll> inv = inv_factorial(n, p); //Precomputarse
    return fac[n] * inv[k] % p * inv[n - k] % p;
23
```

Para $m \leq 10^5$, se puede usar el teorema de Lucas que plantea

$$\binom{n}{k} \mod m = \prod_{i=1}^{\log m} \binom{n_i}{k_i}$$

Donde

$$n_i = \frac{n_{i-1}}{m}, \qquad n_0 = n$$

$$k_i = \frac{k_{i-1}}{m}, \qquad k_0 = k$$

5.5.2 nCk mod m si m es compuesto

Se realiza la descomposición en factores primos de m, resultando

$$k_i = \frac{k_{i-1}}{m}, \qquad k_0 = k$$

Por cada factor primo se computa

5.6 Miller-Rabin

Test de primalidad.

```
vector<int> a{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};

ll mult(ll a, ll b, ll mod) {
    return ((__int128)a * b) % mod;
}

/*
a a es la base.
d es la potencia.
n es el modulo.

*/
ll pw(ll a, ll d, ll n){ // pow in log(n)
vector<ll> dp(63);
dp[0] = a;
```

```
ll res;
15
16
     FOR(i, 1, 63) dp[i] = mult(dp[i - 1], dp[i - 1], n);
17
18
     deque<int> bits;
19
20
     FOR(i, 0, 63) if(d & (11)1 << i) bits.PB(i);
21
22
     res = dp[bits.F()]%n;
23
     bits.P_F();
24
25
     while(!bits.empty()){
26
      res = (mult(res, dp[bits.F()], n))%n;
27
       bits.P_F();
28
29
30
31
    return res;
32 }
33
_{34} bool prime(ll n){ // test de primalidad
35
    ll r, x, m, d;
    bool out;
36
37
    r = 0;
    m = n - 1;
38
39
     while(m%2 == 0){
40
      m /= 2;
41
      r++;
42
    }
43
44
     d = m;
45
     FOR(i, 0, a.size()){
46
47
       x = pw(a[i], d, n);
       out = false;
48
       if (x == 1 \text{ or } x == n - 1) \text{ continue};
49
50
       else{
         FOR(j, 0, r - 1){
51
           x = mult(x, x, n);
if(x == n - 1){
52
53
54
             out = true;
55
             break;
56
           }
        }
57
58
59
       if(out) continue;
60
       return false;
61
    }
62
    return true;
63
```

5.7 Pollard Rho

Encontrar un divisor de P.

```
1 ll mult(ll a, ll b, ll mod) {
      return ((__int128)a * b) % mod;
3 }
5 ll f(ll x, ll c, ll mod) {
     return (mult(x, x, mod) + c) % mod;
6
7 }
9 ll rho(ll n) {
10 ll c = 1, x, y, g;
   y = x = 2;
11
12
    g = c;
    while(g == 1){
13
     x = f(x, c, n);
14
     y = f(y, c, n);
15
    y = f(y, c, n);
16
g = __gcd(abs(x - y), n);
18 }
return g;
20 }
```

5.8 Inclusión-Exclusión

```
C++:
```

```
1 ll inclusionExclusion(int pos, int size, ll res, ll x, vector<ll> &p){
2    if(res > x) return 0;
3    if(size == 0) return x/res;
4
5    ll ans = 0;
6    FOR(i, pos, p.size()){
7       ans += inclusionExclusion(i + 1, size - 1, res*p[i]/__gcd(res, p[i]), x, p);
8    }
9
10    return ans;
11 }
```