

Class : Nine
Section : Zinnia
Subject - Mathematics

Exercise-1

21. If $n = 2x - 1$, where $x \in N$. Prove that n^2 when divided by 8 gives 1 as remainder .

Given ,

$$n = 2x - 1 ; \text{ where } x \in N$$

$$\begin{aligned}\therefore n^2 &= (2x - 1)^2 \\ &= 4x^2 - 4x + 1 \\ &= 4x(x - 1) + 1\end{aligned}$$

Since , $(x - 1)$ and x are two consecutive natural numbers , one of them must be even number.

Hence $x(x - 1)$ is divisible by 2

So , $4x(x - 1)$ is divisible by $4 \times 2 = 8$.

Therefore , if we divided $4x(x - 1) + 1$ by 8 then as a result the remainder will be 1 .

Again ,

If $n = 1$

Then $n^2 = 1$, the remainder is 1 when divided by 8 .

$\therefore n^2$ is divided by 8 every time the remainder is 1 .

[Proved]

Extra. If $n = 2x - 1$, where $x \in \mathbb{Z}$. Prove that n^2 when divided by 8 gives 1 as remainder .

Given ,

$$n = 2x - 1 ; \text{ where } x \in \mathbb{Z}$$

$$\begin{aligned}\therefore n^2 &= (2x - 1)^2 \\ &= 4x^2 - 4x + 1 \\ &= 4x(x - 1) + 1\end{aligned}$$

Since , $(x - 1)$ and x are two consecutive integer numbers , one of them must be even number.

Hence $x(x - 1)$ is divisible by 2

So , $4x(x - 1)$ is divisible by $4 \times 2 = 8$.

Therefore , if we divided $4x(x - 1) + 1$ by 8 then as a result the remainder will be 1 .

$\therefore n^2$ is divided by 8 every time the remainder is 1 .

[Proved]

Extra : Show that , if the square of an odd natural number is divided by 8 then in each case the remainder will be 1 .

If n is an odd natural number ,

$$n = 2x - 1 ; \text{ where } x \in N$$

In this case ,

$$\begin{aligned} n^2 &= (2x - 1)^2 \\ &= 4x^2 - 4x + 1 \\ &= 4x(x - 1) + 1 \end{aligned}$$

Since , $(x - 1)$ and x are two consecutive natural numbers , one of them must be even number.

Hence $x(x - 1)$ is divisible by 2

So , $4x(x - 1)$ is divisible by $4 \times 2 = 8$.

Therefore , if we divided $4x(x - 1) + 1$ by 8 then as a result the remainder will be 1 .

Again ,

If $n = 1$

Then $n^2 = 1$, the remainder is 1 when divided by 8.

Therefore , when the square of an odd natural number is divided by 8 then in each case the remainder will be 1.

[Showed]

