

Chapter 8.2-8.3

Question for Today

Recall the Mario Kart analysis

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
                       1.71 24.15 < 2e-16 ***
(Intercept)
             41.34
                       1.05 -4.88 2.91e-06 ***
condused
              -5.13
stockPhotoyes
              1.08
                       1.06 1.02 0.308
duration
              -0.03
                       0.19 -0.14
                                     0.888
wheels
              7 29
                       0.55 13.13 < 2e-16 ***
```

Residual standard error: 4.901 on 136 degrees of freedom Multiple R-squared: 0.719, Adjusted R-squared: 0.7108

Question for Today

This is the full model: every explanatory variable provided is included.

Recall Occam's Razor: all other things being equal, simpler is better.

In our case: simpler = less predictor variables included in the model.

The act of choosing which predictor variables to include in your model is model selection.

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Two Common Strategies

There are two stepwise regression methods that add/subtract one variable at a time:

- Backward Flimination
- Forward Selection

The criteria used will be p-values (R_{adi}^2 can be used as well).

Backward Elimination

- 1. Start with the full model
- 2. While there still exists statistically non-significant variables
 - 2.1 Identify the variable with the largest p-value and drop it
 - 2.2 Refit the model
- 3. Report model once there are no more non-significant variables

Backward Elimination

Starting here:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	41.3415	1.7117	24.15	0.0000
cond_used	-5.1306	1.0511	-4.88	0.0000
stockPhotoyes	1.0803	1.0568	1.02	0.3085
duration	-0.0268	0.1904	-0.14	0.8882
wheels	7.2852	0.5547	13.13	0.0000

Backward Elimination

Drop duration.

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	41.3415	1.7117	24.15	0.0000
cond_used	-5.1306	1.0511	-4.88	0.0000
stockPhotoyes	1.0803	1.0568	1.02	0.3085
duration	-0.0268	0.1904	-0.14	0.8882
wheels	7.2852	0.5547	13.13	0.0000

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Backward Elimination

Drop stockPhotoyes.

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	41.2245	1.4911	27.65	0.0000
cond_used	-5.1763	0.9961	-5.20	0.0000
stockPhotoyes	1.1177	1.0192	1.10	0.2747
wheels	7.2984	0.5448	13.40	0.0000

Backward Elimination

Done.

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	42.3698	1.0651	39.78	0.0000
cond_used	-5.5848	0.9245	-6.04	0.0000
wheels	7.2328	0.5419	13.35	0.0000

Forward Selection

- 1. Start with the model with no variables
- 2. Fit all models with one possible additional variable
- 3. Add the additional variable with the smallest p-value if its significant
- 4. Repeat steps 2 and 3 until there are no significant additional variables.

Criticisms of the Techniques

Critics regard stepwise regression as data dredging, where intense computation is used as a substitute for subject area expertise when deciding on a model.

Data mining involves automatically testing huge numbers of hypotheses about a single data set by exhaustively searching for combinations of variables that might show a correlation.

Criticisms of the Techniques



Assumptions of Multiple Regression

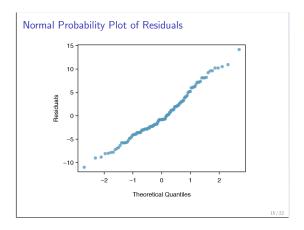
- ▶ The residuals e; of the model
 - are nearly normal
 - ▶ have nearly constant variance
 - are independent
- ► Each variable is linearly related to the outcome

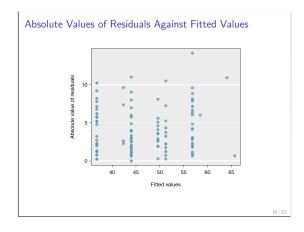
Example Model

We investigate plots for the following model:

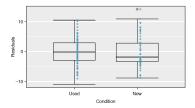
$$\widehat{\text{price}} = b_0 + b_1 \times \text{cond.new} + b_2 \times \text{wheels}$$

- ▶ Normal probability plot of residuals
- Absolute values of residuals against fitted values: look for non-constant variance
- Residuals against each predictor variable

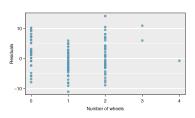








Residuals Against Each Predictor Variable: Wheels



George E.P. Box

There was a famous statistician named Box



famous for the Box/Cox Transformation.

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George E.P. Box's Famous Quote

"All models are wrong, but some are useful."

Caution

We can tolerate a little leeway with model assumptions, but when they are grossly violated we have to be skeptical of any confidence intervals/p-values. If model assumptions are clearly violated

- consider a new model
- ▶ get the assistance of someone who can help

Next Time

What if the outcome variable is not numerical, but rather a yes/no response variable?

- ► Was an email spam or not?
- ▶ Will someone develop cancer or not?
- ▶ Is a person female?

We use logistic regression.