#### Lecture 28: Logistic Regression

Chapter 8.4

## Binary Outcome Variables

#### Outcome Variable

# Logit Transformation

## Odds

#### Outcome Variable

Figure 8.13 from page 388

#### Simple Logistic Regression Example p.388

So say we fit a logistic regression with:

➤ Y<sub>i</sub> is spam: binary variable of whether message was classified as spam (1 if spam)

## Simple Logistic Regression Example p.388

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- x<sub>i</sub> is to\_multiple: binary variable indicating if more than one recipient listed

## Simple Logistic Regression Example p.388

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- x<sub>i</sub> is to\_multiple: binary variable indicating if more than one recipient listed

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-2.1161	0.0562	-37.67	0.0000
to_multiple	-1.8092	0.2969	-6.09	0.0000

## Inverse Logit Transformation

#### Fitted Probabilities

### Fitted Model Using Backwards Regression

The following model was selected in the text using backwards selection using  $\alpha=0.05$ .

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-0.8057	0.0880	-9.15	0.0000
to_multiple?	-2.7514	0.3074	-8.95	0.0000
word winner used?	1.7251	0.3245	5.32	0.0000
special formatting?	-1.5857	0.1201	-13.20	0.0000
'RE:' in subject?	-3.0977	0.3651	-8.48	0.0000
attachment?	0.2127	0.0572	3.72	0.0002
word password used?	-0.7478	0.2956	-2.53	0.0114

#### Fitted Model Using Backwards Regression

The following variables increase the probability that the email is spam, since b>0

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, ,				
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		0.00		
attachment?	0.2127	0.0572	3.72	0.0002
actuellinent.	0.2121	0.0012	3.12	0.0002

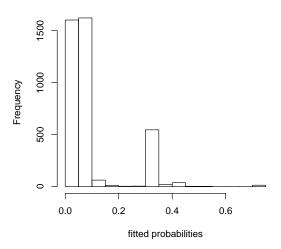
## Fitted Model Using Backwards Regression

The following variables decrease the probability that the email is spam, since b < 0

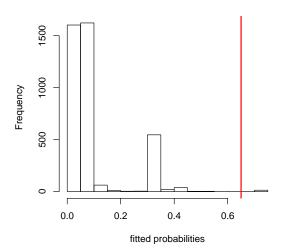
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#### Fitted Probabilities

These are all 3921 fitted probabilities  $\hat{p}$ :



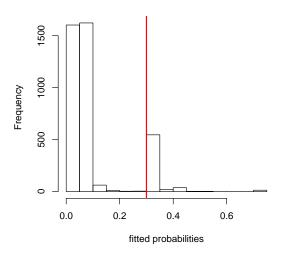
Say we use a cutoff of 65% to classify an email spam or not:



Using a cutoff of 65%:

		Classification		
		Not Spam Spam $\widehat{p}_i < .65$ $\widehat{p}_i \geq .6$		
		$\widehat{p}_i < .65$	$\widehat{p}_i \geq .65$	
Truth	Not Spam: $Y_i = 0$	3351	3	
	Spam: $Y_i = 1$	357	10	

Now say we use a cutoff of 30% to classify an email spam or not:



Using a cutoff of 30%:

		Classification		
		Not Spam $\widehat{p}_i < .30$	Spam	
		$\widehat{p}_i < .30$	$\widehat{p}_i \geq .30$	
Truth	Not Spam: $Y_i = 0$	3138	416	
	Spam: $Y_i = 1$	166	201	

## Conditions for Logistic Regression