

1. Binomial tree option pricing

Write a **function** to estimate the price of a standard **European** option. It receives all required inputs as **function arguments** including the number of steps and the type of option (Call or Put)

- A. The program should display the tree.
- B. Report a comparison of your results with the results obtained by DerivaGem only for one sample.

2. Gap option & Standard option using Monte Carlo simulation

In this problem, the goal is to determine two types of options prices by using Monte Carlo simulation. you are required to **randomly** select **10** European call options **exercise prices** and **S_0** . Then, you estimate the prices of both **gap** and **standard** call using Monte Carlo simulation approach, assume that the asset $S(t)$ follows the Geometric Brownian motion. Simulate at least 1000 paths for each estimation. The option price corresponds to the average value of its discounted future payouts under the risk- neutral probability.

- A. Report the results in only **one** table that includes following results: (hint: pandas DataFrame can be used for this purpose)
 - I. Stock price
 - II. Strike price (K_1)
 - III. Second strike price (K_2)
 - IV. Gap option price using Monte Carlo
 - V. Standard option prices using Monte Carlo
 - VI. Standard option prices using BSM model
 - VII. Column 4 – Column 5
 - VIII. $(K_2 - K_1)e^{-rt}N(d_2)$
- B. Plot one of the path price movement in Monte Carlo
- C. Compare seventh and eighth columns.
- D. Is GBM-based estimation reliable? (hint: it can be resulted from comparison of fourth and fifth columns)

S_0	K_1	K_2	T	Volatility	Risk-free rate
Lognormal distribution with $\mu=95$, $\sigma=10$	Integers in range [80,90]	Integers in range [90,100]	1 year	25%	12%

Gap option:

If $S_T \geq K_1 \Rightarrow \text{call payoff} = S_T - K_2$