MAIE 5421 Computer Vision: Assignment-1

September 26, 2025

Github URL: Rezela/Computer-Vision-Assignment-1

1 Simple Linear Regression (15 Points)

1.
$$SSR = \frac{1}{i+1} \left(\frac{1}{3}i - (\beta + \alpha x_i) \right)^{\frac{1}{2}}$$

$$0 \quad \frac{\partial SSR}{\partial \beta} = 2 \cdot \frac{1}{i+1} \left(\frac{1}{3}i - (\beta + \alpha x_i) \right) \cdot (-1)$$

let $\frac{\partial SSR}{\partial \beta} = 0$,

$$R\beta = \frac{1}{3} \left(\frac{1}{3}i - \alpha x_i \right)$$

$$\beta = \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} \left(\frac{1}{3}i \cdot \frac{1}{3} - \frac{1}{3}i \cdot \frac{1}{3} \right)$$
introduce $\beta = \frac{1}{3} \cdot \frac{$

2 Confusion Matrix (10 Points)

True Positive Rate: TPR =
$$\frac{TP}{TP+FN} = \frac{40}{40+10} = 0.8$$

True Negative Rate:
$$TNR = \frac{TN}{TN+FP} = \frac{45}{45+5} = 0.9$$

Precision =
$$\frac{TP}{TP+FP} = \frac{40}{40+5} = \frac{8}{9} = 0.889$$

$$Acc = \frac{TP+TN}{TP+FP+TN+FN} = \frac{8\Gamma}{100} = 0.8\Gamma$$

Fi-score =
$$\frac{2 \cdot \text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}} = \frac{2 \times \frac{8}{9} \times 0.8}{\frac{8}{9} + 0.8} = 0.842$$

3 K-Nearest Neighbors (10 Points)

```
E:\CV\Assignment1\pythonProject1\.venv\Scripts\python.exe E:\CV\Assignment1\pythonProject1\KNN.py
FULL Distance Table:

ID x y z Label L1_Distance Cosine_Distance
0 1 1.0 2.0 3.0 A 7.5 0.016393
1 2 0.5 1.8 2.7 B 8.5 0.044365
2 3 1.2 2.2 3.5 B 6.6 0.014618
3 4 4.6 5.6 3.7 A 5.0 0.069342
4 5 2.4 4.6 3.6 A 4.1 0.043839
5 6 3.5 2.0 4.1 B 3.9 0.026862
6 7 3.6 4.6 7.1 A 1.8 0.001298
7 8 6.2 4.1 1.3 B 7.5 0.241130
8 9 8.4 3.5 1.8 A 9.6 0.271068
9 10 5.8 3.4 2.7 B 6.2 0.137294

Top 3 Neighbors by L1 Distance:
ID Label L1_Distance
6 7 A 1.8
5 6 B 3.9
4 5 A 4.1

Top 3 Neighbors by Cosine Distance:
ID Label Cosine_Distance
6 7 A 0.001298
2 3 B 0.014618
0 1 A 0.016393

Final Classification by L1 Distance: A
Final Classification by L1 Distance: A
Final Classification by Cosine Distance: A
```

4 Naive Bayes Classifier (10 Points)

```
NN.py
            NaiveBayes.py ×
                             KMeans.py
                                           DecisionTree.py
                                                             CNN1.py
                                                                          CNN2.py
        'Humidity': 'Normal',
    total = len(df)
     yes_count = len(df[df['Play Golf'] == 'Yes'])
     no_count = len(df[df['Play Golf'] == 'No'])
     P_yes = yes_count / total
     P_no = no_count / total
     def conditional_prob(feature, value, label):
        subset = df[df['Play Golf'] == label]
        count = len(subset[subset[feature] == value])
     features = ['Outlook', 'Temperature', 'Humidity', 'Windy']
     P_X_given_yes = np.prod([conditional_prob(f, new_sample[f], label: 'Yes') for f in features])
     P_X_given_no = np.prod([conditional_prob(f, new_sample[f], |abel: 'No') for f in features])
     posterior_yes = P_X_given_yes * P_yes
     posterior_no = P_X_given_no * P_no
     prediction = 'Yes' if posterior_yes > posterior_no else 'No'
     print("Prior P(Yes):", round(P_yes, 3))
    print("Prior P(No):", round(P_no, 3))
    print("Likelihood P(X|Yes):", round(P_X_given_yes, 5))
    print("Likelihood P(X|No):", round(P_X_given_no, 5))
    print("Posterior P(Yes|X):", round(posterior_yes, 5))
    print("Posterior P(No|X):", round(posterior_no, 5))
     print("Prediction for new sample:", prediction)
运行
         📦 NaiveBayes 🛛 🗀
      E:\CV\Assignment1\pythonProject1\.ven
      Prior P(Yes): 0.5
      Prior P(No): 0.5
      Likelihood P(X|Yes): 0.04688
      Likelihood P(X|No): 0.01562
      Posterior P(Yes|X): 0.02344
3
      Posterior P(No|X): 0.00781
      Prediction for new sample: Yes
      进程已结束,退出代码为 0
```

5 Decision Tree (15 Points)

```
NN.py
            CNN2.py
      def id3(df, target='Class', attributes=None, depth=0):
          indent = " " * depth
          classes = Counter(df[target])
             return list(classes.keys())[0]
          if attributes is None:
             attributes = [col for col in df.columns if col not in [target, 'ID']]
          current_entropy = entropy(df[target])
          print(f"\n{indent}Tree node (Depth {depth})")
          print(f"{indent}Current Entropy: {current_entropy:.4f}")
          gains = {attr: info_gain(df, attr, target) for attr in attributes}
          for attr, g in gains.items():
          best_attr = max(gains, key=gains.get)
          print(f"{indent}Choose: {best_attr}")
          tree = {best_attr: {}}
          for v in df[best_attr].unique():
             subset = df[df[best_attr] == v]
             branch_entropy = entropy(subset[target])
             branch_counts = dict(Counter(subset[target]))
             print(f"{indent} Branch {best_attr}={v}: distribution {branch_counts}, entropy={branch_entropy:.4f}")
             if len(subset) == 0:
                 tree[best_attr][v] = classes.most_common(1)[0][0]
                 new_attrs = [a for a in attributes if a != best_attr]
                 tree[best_attr][v] = id3(subset, target, new_attrs, depth + 1)
          return tree
```

```
DecisionTree ×
E:\CV\Assignment1\pythonProject1\.venv\Scripts\python.exe E:\CV\Assignment1\pythonProject1\DecisionTree.py
Tree node (Depth 0)
Current Entropy: 0.7642
Information Gain for - Weather: 0.4581
Information Gain for - Temperature: 0.1409
Information Gain for - Wind: 0.2248
Choose: Weather
 Branch Weather=Sunny: distribution {'No': 2, 'Yes': 1}, entropy=0.9183
 Tree node (Depth 1)
 Current Entropy: 0.9183
  Information Gain for - Temperature: 0.2516
 Information Gain for - Wind: 0.9183
 Choose: Wind
   Branch Wind=High: distribution {'No': 2}, entropy=-0.0000
   Branch Wind=Medium: distribution {'Yes': 1}, entropy=-0.0000
 Branch Weather=Overcast: distribution {'Yes': 3}, entropy=-0.0000
 Branch Weather=Rain: distribution {'Yes': 3}, entropy=-0.0000
Final Decision Tree:
{'Weather': {'Sunny': {'Wind': {'High': 'No', 'Medium': 'Yes'}}, 'Overcast': 'Yes', 'Rain': 'Yes'}}
进程已结束,退出代码为 0
```

6 K-Means (10 Points)

```
NN.py
                         NaiveBayes.py
                                                   CNN1.py
                                                              CNN2.pv
    import pandas
          distance1 = np.linalg.norm(p-point1)
         distance2 = np.linalg.norm(p-point2)
         clusters[0 if distance1 < distance2 else 1].append(j+1) # 保存点的索引到对应的簇
       print("cluster[0]: "_cclusters[0])
print("cluster[1]: "_cclusters[1])
      ■ IVIAIL 342 1-Assignment 1-
运行
        KMeans ×
G 🔳 🗄
     E:\CV\Assignment1\pythonProject1\.ven
     Iteration: 1
     cluster[0]: [1, 2, 5, 7]
     cluster[1]: [3, 4, 6, 8]
     centroid 1: [1.95 2.95 1.2]
     centroid 2: [7.75 6.75 8.75]
Iteration: 2
     cluster[0]: [1, 2, 5, 7]
     cluster[1]: [3, 4, 6, 8]
     centroid 1: [1.95 2.95 1.2 ]
     centroid 2: [7.75 6.75 8.75]
     进程已结束,退出代码为 0
```

7 CNN Q1 (15 Points)

Model: "sequential"

Layer (type)	Output Shape	Param #
conv2d (Conv2D)	(None, 32, 32, 8)	80
conv2d_1 (Conv2D)	(None, 16, 16, 16)	1,168
conv2d_2 (Conv2D)	(None, 16, 16, 32)	4,640
max_pooling2d (MaxPooling2D)	(None, 8, 8, 32)	0
flatten (Flatten)	(None, 2048)	0
dense (Dense)	(None, 10)	20,490

Total params: 26,378 (103.04 KB)
Trainable params: 26,378 (103.04 KB)
Non-trainable params: 0 (0.00 B)

进程已结束,退出代码为 0

8 CNN Q2 (15 Points)

```
W KNN.py
          DecisionTree.py
                                                   CNN1.py

<sup>♠</sup> CNN2.py ×

      tf.keras.layers.Conv2D(1, (3, 3), strides=1, padding="valid", input_shape=(5, 5, 1), use_bias=False),
   model.layers[0].set_weights([K])
   model.layers[-1].set_weights([W])
36 print("Output: ", output.numpy().item())
   Output: 4.0
   进程已结束,退出代码为 0
```