

# Métodos Runge-Kuttas

March 5, 2023

## 1 Programa 1

```
[1]: import pandas as pd
import numpy as np
pd.set_option('display.max_rows', None)
```

### 1.1 Métodos de Runge-Kutta-Merson y de grado 4

#### 1.1.1 Rubrica

Elemento	Pts.
Cambia PVI	3
Lee valores iniciales	2
Pide $h$ y tolerancia	2
Presenta tabla $(x, y)$ correcta [R-K-4]	4
Presenta tabla $(x, y)$ correcta [R-K-M]	4
Da opción de presentar tabla (K's)	3
Compara métodos con diferencia entre ellos	2
Permite volver a ejecutar y cambiar valores iniciales	2
Aplica control de error (Extra)	2

### 1.2 Código

```
[2]: class RungeKuttas(object):

    # Encabezados
    header=list(("x", "y", "k1", "k2", "k3", "k4", "k5", "Error"))

    # Constructor
    def __init__(self, initialValue:list, point:float, h_value:float, error:
↪float = 0.0, equation:str="0") -> None:
        self._initialValue = initialValue
        self.h_value = h_value
        self.error = error
        self.solTab = np.zeros((1,8),dtype=float)
        self.point = point
        self.equation = equation
```

```

# Lo que muestra al llamar la función print
def __str__(self:any) -> str:
    self.rkmMethod()
    return "Objeto de tipo Método Runge-Kutta"

#region Método de Runge-Kutta-4
def rk4(self:any):
    self.firstRowOrder4()
    self.iterationsOrder4()
    return pd.DataFrame(self.solTab, columns=self.
↳header)[['x', 'y', 'k1', 'k2', 'k3', 'k4', 'Error']]

# Método para crear la primera iteración de RK4
def firstRowOrder4(self:any) -> None:
    x,y = self._initialValue[0], self._initialValue[1]
    self.solTab[0,0] = x
    self.solTab[0,1] = y
    self.solTab[0,2] = self.k1(x,y)
    self.solTab[0,3] = self.k2(x,y,self.solTab[0,2])
    self.solTab[0,4] = self.k3(x,y,self.solTab[0,3])
    self.solTab[0,5] = self.k4(x,y,self.solTab[0,2],self.solTab[0,3],self.
↳solTab[0,4])

# Método para crear el resto de las iteraciones de RK4
def iterationsOrder4(self:any) -> None:
    rango = int(np.abs((self._initialValue[0]-self.point)/self.h_value))
    for i in range(0,rango):
        yn = np.zeros(shape=(1,8))
        x,y = self.solTab[i,0] + self.h_value,self.solTab[i,1]
        yn[0,0] = x
        yn[0,1] = self.get_y(y=y, k1=self.solTab[i,2], k2=self.solTab[i,3],
↳k3=self.solTab[i,4], k4=self.solTab[i,5])
        y = yn[0,1]
        yn[0,2] = self.k1(x,y)
        yn[0,3] = self.k2(x,y,yn[0,2])
        yn[0,4] = self.k3(x,y,yn[0,3])
        yn[0,5] = self.k4(x,y,yn[0,2],yn[0,3],yn[0,4])
        self.solTab = np.append(self.solTab,yn, axis=0)
        del yn,x,y

# Métodos para obtener las k del metodo de RK4
def k1(self, x:float, y:float) -> float:
    return self.fdexy(x,y)

def k2(self, x:float, y:float, k1:float) -> float:
    return self.fdexy(x + self.h_value/2, y + k1 * self.h_value /2)

```

```

def k3(self, x:float, y:float, k2:float) -> float:
    return self.fdexy(x + self.h_value/2, y + k2 * self.h_value /2)

def k4(self, x:float, y:float, k1:float, k2:float, k3:float) -> float:
    return self.fdexy(x + self.h_value, y + k3 * self.h_value )

def get_y(self,y:float, k1:float, k2:float, k3:float, k4:float) -> float:
    """Return the next y with a global error of  $O(h^3)$ """
    return y + (k1 + 2 * k2 + 2 * k3 + k4) * self.h_value/6

#endregion

#region Método de Runge-Kutta-Merson
def rkmMethod(self:any) -> pd.DataFrame:
    self.firstRowMerson()
    self.iterationsMerson()
    return pd.DataFrame(self.solTab, columns=self.
↪header)[['x', 'y', 'k1', 'k2', 'k3', 'k4', 'k5', 'Error']]

# Método para crear la primera iteración de Merson
def firstRowMerson(self:any) -> None:
    x,y = self._initialValue[0], self._initialValue[1]
    self.solTab[0,0] = x
    self.solTab[0,1] = y
    self.solTab[0,2] = self.mersonk1(x,y)
    self.solTab[0,3] = self.mersonk2(x,y,self.solTab[0,2])
    self.solTab[0,4] = self.mersonk3(x,y,self.solTab[0,2],self.solTab[0,3])
    self.solTab[0,5] = self.mersonk4(x,y,self.solTab[0,2],self.
↪solTab[0,3],self.solTab[0,4])
    self.solTab[0,6] = self.mersonk5(x,y,self.solTab[0,2],self.
↪solTab[0,3],self.solTab[0,4],self.solTab[0,5])

# Método para crear el resto de las iteraciones de Merson
def iterationsMerson(self) -> None:
    rango = int(np.abs((self._initialValue[0]-self.point)/self.h_value))
    for i in range(0,rango):
        yn = np.zeros(shape=(1,8))
        x,y = self.solTab[i,0] + self.h_value,self.solTab[i,1]
        yn[0,0] = x
        yn[0,1] = self.get_yMerson(y=y, k1=self.solTab[i,2], k3=self.
↪solTab[i,4], k4=self.solTab[i,5], k5=self.solTab[i,6])
        y = yn[0,1]
        yn[0,2] = self.mersonk1(x,y)
        yn[0,3] = self.mersonk2(x,y,yn[0,2])
        yn[0,4] = self.mersonk3(x,y,yn[0,2],yn[0,3])
        yn[0,5] = self.mersonk4(x,y,yn[0,2],yn[0,3],yn[0,4])

```

```

        yn[0,6] = self.mersonk5(x,y,yn[0,2],yn[0,3],yn[0,4],yn[0,5])
        self.solTab = np.append(self.solTab,yn, axis=0)
        del yn,x,y

    # Esta función recibirá una cadena que representará la función, usaremos la
    ↪función "eval"
    def fdexy(self,x:float, y:float) -> float:
        """This is the equation we want to get the numeric solution"""
        # Notita: las variables x, y si se ocupan ;aunque no lo parezca!
        return eval(self.equation)

    # Métodos para obtener las k del metodo de Merson
    def mersonk1(self, x:float, y:float) -> float:
        return self.h_value * self.fdexy(x,y)

    def mersonk2(self, x:float, y:float, k1:float) -> float:
        return self.h_value * self.fdexy(x + self.h_value/3, y + k1/3)

    def mersonk3(self, x:float, y:float, k1:float, k2:float) -> float:
        return self.h_value * self.fdexy(x + self.h_value / 3, y + k1/6 + k2/6)

    def mersonk4(self, x:float, y:float, k1:float, k2:float, k3:float) -> float:
        return self.h_value * self.fdexy(x + self.h_value / 2, y + k1 / 8 + 3/8
    ↪* k3)

    def mersonk5(self,x:float,y:float, k1:float, k2:float, k3:float, k4:float)
    ↪-> float:
        return self.h_value * self.fdexy(x + self.h_value, y + k1/2 - 3/2 * k3
    ↪+ 2*k4)

    def mersonk6(self, x:float, y:float, k1:float, k2:float, k3:float, k4:
    ↪float, k5:float) -> float:
        return self.h_value * self.fdexy(x + self.h_value/2, y - 8/27*k1 + 2*k2
    ↪- 3544/2565*k3 + 1859/4104*k4 - 11/40*k5)

    # Regresa la y de Merson
    def get_yMerson(self,y:float, k1:float, k3:float, k4:float, k5:float) ->
    ↪float:
        """Return the next y with a global error of  $O(h^4)$ """
        return y + (k1 + 4*k4 + k5)/6

    #endregion

```

### 1.2.1 Tabla con el método de grado 4

```
[3]: tab1=RungeKuttas(initialValue=(0,3),h_value=0.5, point=7, equation="-0.06*y**(1/
↪2)").rk4()
tab1
```

```
[3]:      x      y      k1      k2      k3      k4      Error
0  0.0  3.000000 -0.103923 -0.103472 -0.103474 -0.103023  0.0
1  0.5  2.948263 -0.103023 -0.102572 -0.102574 -0.102123  0.0
2  1.0  2.896977 -0.102123 -0.101672 -0.101674 -0.101223  0.0
3  1.5  2.846140 -0.101223 -0.100772 -0.100774 -0.100323  0.0
4  2.0  2.795754 -0.100323 -0.099872 -0.099874 -0.099423  0.0
5  2.5  2.745817 -0.099423 -0.098972 -0.098974 -0.098523  0.0
6  3.0  2.696331 -0.098523 -0.098072 -0.098074 -0.097623  0.0
7  3.5  2.647294 -0.097623 -0.097172 -0.097174 -0.096723  0.0
8  4.0  2.598708 -0.096723 -0.096272 -0.096274 -0.095823  0.0
9  4.5  2.550571 -0.095823 -0.095372 -0.095374 -0.094923  0.0
10 5.0  2.502885 -0.094923 -0.094472 -0.094474 -0.094023  0.0
11 5.5  2.455648 -0.094023 -0.093572 -0.093574 -0.093123  0.0
12 6.0  2.408862 -0.093123 -0.092672 -0.092674 -0.092223  0.0
13 6.5  2.362525 -0.092223 -0.091772 -0.091774 -0.091323  0.0
14 7.0  2.316639 -0.091323 -0.090872 -0.090874 -0.090423  0.0
```

### 1.2.2 Tabla con el método de R-K-M

```
[4]: tab2=RungeKuttas(initialValue=(0,3),h_value=0.5, point=7, equation="-0.06*y**(1/
↪2)").rkMethod()
tab2
```

```
[4]:      x      y      k1      k2      k3      k4      k5      Error
0  0.0  3.000000 -0.051962 -0.051811 -0.051812 -0.051737 -0.051512  0.0
1  0.5  2.948263 -0.051512 -0.051361 -0.051362 -0.051287 -0.051062  0.0
2  1.0  2.896977 -0.051062 -0.050911 -0.050912 -0.050837 -0.050612  0.0
3  1.5  2.846140 -0.050612 -0.050461 -0.050462 -0.050387 -0.050162  0.0
4  2.0  2.795754 -0.050162 -0.050011 -0.050012 -0.049937 -0.049712  0.0
5  2.5  2.745817 -0.049712 -0.049561 -0.049562 -0.049487 -0.049262  0.0
6  3.0  2.696331 -0.049262 -0.049111 -0.049112 -0.049037 -0.048812  0.0
7  3.5  2.647294 -0.048812 -0.048661 -0.048662 -0.048587 -0.048362  0.0
8  4.0  2.598708 -0.048362 -0.048211 -0.048212 -0.048137 -0.047912  0.0
9  4.5  2.550571 -0.047912 -0.047761 -0.047762 -0.047687 -0.047462  0.0
10 5.0  2.502885 -0.047462 -0.047311 -0.047312 -0.047237 -0.047012  0.0
11 5.5  2.455648 -0.047012 -0.046861 -0.046862 -0.046787 -0.046562  0.0
12 6.0  2.408862 -0.046562 -0.046411 -0.046412 -0.046337 -0.046112  0.0
13 6.5  2.362525 -0.046112 -0.045961 -0.045962 -0.045887 -0.045662  0.0
14 7.0  2.316639 -0.045662 -0.045511 -0.045512 -0.045437 -0.045212  0.0
```

## 2 Interfaz

```
[5]: import wx
```

```
-----  
ModuleNotFoundError                                Traceback (most recent call last)  
Cell In[5], line 1  
----> 1 import wx  
  
ModuleNotFoundError: No module named 'wx'
```

```
[ ]: # Create the Application Object  
app = wx.App()  
# Now create a Frame (representing the window)  
frame = wx.Frame(parent=None, title='Simple Hello World') # And add a text_  
    ↪label to it  
text = wx.StaticText(parent=frame, label='Hello Python')  
# Display the window (frame)  
frame.Show()  
# Start the event loop  
app.MainLoop()
```

```
[ ]: import tkinter as tk  
  
def save_info():  
    info = []  
    for entry in entries:  
        info.append(entry.get())  
    print(info)  
  
root = tk.Tk()  
root.title("Mi Ventana")  
  
entries = []  
  
for i in range(5):  
    label = tk.Label(root, text=f"Ingrese la cadena #{i+1}")  
    label.pack()  
    entry = tk.Entry(root)  
    entry.pack()  
    entries.append(entry)  
  
button = tk.Button(root, text="Guardar información", command=save_info)  
button.pack()  
  
root.mainloop()
```

```

[ ]: import tkinter as tk
from tkinter import ttk
import pandas as pd

class App:
    def __init__(self, master):
        self.master = master
        master.title("Interfaz gráfica")

        # Crear los widgets para la entrada de datos
        tk.Label(master, text="Valor x ").grid(row=0, column=0)
        self.float1_entry = tk.Entry(master)
        self.float1_entry.grid(row=0, column=1)
        tk.Label(master, text="Valor y").grid(row=1, column=0)
        self.float2_entry = tk.Entry(master)
        self.float2_entry.grid(row=1, column=1)
        tk.Label(master, text="Valor h").grid(row=2, column=0)
        self.float3_entry = tk.Entry(master)
        self.float3_entry.grid(row=2, column=1)
        tk.Label(master, text="Punto a interpolar").grid(row=3, column=0)
        self.float4_entry = tk.Entry(master)
        self.float4_entry.grid(row=3, column=1)
        tk.Label(master, text="Ecuación ").grid(row=5, column=0)
        self.cadena_entry = tk.Entry(master)
        self.cadena_entry.grid(row=5, column=1)

        # Crear el botón para enviar los datos y mostrar el DataFrame
        self.button = tk.Button(master, text="Mostrar DataFrame", command=self.
↪mostrar_dataframe)
        self.button.grid(row=6, column=1)

    def mostrar_dataframe(self, df:pd.DataFrame):
        # Obtener los datos de las entradas
        # float1 = float(self.float1_entry.get())
        # float2 = float(self.float2_entry.get())
        # float3 = float(self.float3_entry.get())
        # float4 = float(self.float4_entry.get())
        # cadena = self.cadena_entry.get()

        # # Crear un diccionario con los datos
        # data = {"Float 1": [float1], "Float 2": [float2], "Float 3": ↵
↪[float3], "Float 4": [float4], "Float 5": [float5], "Cadena": [cadena]}

        # Crear un DataFrame a partir del diccionario y mostrarlo en una tabla
        # df = pd.DataFrame(data)
        window = tk.Toplevel(self.master)
        window.title("DataFrame")

```

```

frame = tk.Frame(window)
frame.pack(fill="both", expand=True)
table = ttk.Treeview(frame, columns=df.columns, show="headings")
table.pack(side="left", fill="both", expand=True)
for col in df.columns:
    table.heading(col, text=col)
for index, row in df.iterrows():
    table.insert("", "end", values=[row[col] for col in df.columns])

root = tk.Tk()
app = App(root)
root.mainloop()

```

```

[ ]: import tkinter as tk
import pandas as pd

# Crear DataFrame de ejemplo
data = {'Nombre': ['Juan', 'Ana', 'Pedro'], 'Edad': [25, 30, 35]}
df = pd.DataFrame(data)

# Crear ventana de tkinter
root = tk.Tk()

# Crear widget Text para mostrar DataFrame
text_widget = tk.Text(root)
text_widget.pack()

# Convertir DataFrame a cadena y mostrarlo en el widget Text
text_widget.insert('1.0', df.to_string())

# Ejecutar loop principal de la ventana de tkinter
root.mainloop()

```

```

[ ]:

```