

message passing →

```
int MPI_send()
```

```
void *msg_buff;
int msg_size;
MPI_datatype msg_type;
int dest;
int tag;
MPI_comm comm;
```

→ message
buffer

content
↓
message
buffer

dest. address
↓
message
envelope

→ send(dest, string, 10)
receive(source, string, 10)

⇒ MPI_send has 6 parameters, The first three parameters constitutes of message buffer and signifies the content of the message.

- (i) The first one is msg_buff, the pointer to the block of memory containing the content of the message. the msg address could be the any address in the ~~msg~~ sender's address and refers to the starting of the data.
- (ii) The second argument is msg_size, it is also called the message count and specific the no. of occurrences of data item of the message data type starting at the msg-add, count argument can be used to group continuous array element into the group.
- (iii) The MPI datatype parameter is used to support heterogeneous computing, and allow messages from non-contiguous memory location.

```
MPI_send(dest, string, 10, MPI_CHAR, ...)
MPI_receive(B, 10, MPI_char, ...)
```

Here, 10 no longer signifies the message length in bytes but it specifies the occurrence of data items of the message type MPI_CHAR. This data type MPI-char is implemented as 1 byte in sending machine but 2 bytes in receiving machine, the implementation is responsible for the conversion b/w 8 bits and 16-bits format.

C-data type

signed char, unsigned char
 signed short int, signed int
 float
 signed
 bool
 double
 signed long int
 short
 unsigned short int
 unsigned long int
 long double

~~int MPI-Pack~~

void *

int MPI-Pack

```
void * inbuf,
int in-buf-count,
MPI_Datatype datatype,
void * pack-buf;
int pack-buf-size,
int * position-p;
MPI_Comm comm;
```

to pack the data into the
 contiguous memory space

MPI-data type

MPI-CHAR,
 MPI-SHORT, MPI-INT
 MPI-FLOAT

MPI-DOUBLE
 MPI-LONG

MPI-UNSIGNED-SHORT
 MPI-UNSIGNED-LONG
 MPI-LONG-DOUBLE

MPI-BYTE → when a message is sent in bit
 MPI-PACKED
 ↳ non-continuous data to sent

int MPI-Unpack

```
void * pack-buf,
int pack-buf-size,
int * position-p,
void * out-buf,
int out-buf-count,
MPI_Datatype datatype,
MPI_Comm comm;
```

↳

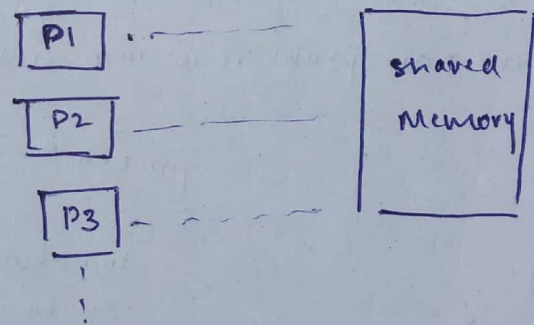
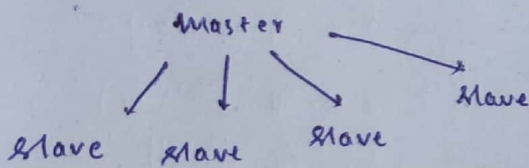
MPI pack takes the data to be packed, and packs it into contiguous buffer, the position-p element keeps track in where we are in our contiguous buffer. When the function is called it refers to the first available location in the buffer before data to be packed is added.

When function returns, it refers to first available location in the packed buffer after data to be packed is added.

MPI unpack reverses the process, it takes the data in contiguous buffer and unpacks it into unpacked data.

When the function is called position-p refers to first location in contiguous buffer that hasn't been unpacked and it returns the *position-p next location in contiguous buffer after the data that was just unpacked.

Shared Memory Program →



Processes are created using fork().
and are terminated using join().

- In shared memory programming, programmers view their program as a collection of cooperating processes, accessing a common pool of shared variables.
- Each processor may not have private data memory, A common program and data are stored in the main memory and are shared by all the processors.
- Each processor can be assigned different part of the program stored in memory to execute with data, also stored in the specified locations.

Process Creation →

- The main program creates separate processes for each processor and allocates them along with the information on the location, where data are stored for each process.
- Each processor computes independently.
- When all processors complete their assigned tasks they have to rejoin with the main program.

- The main program will execute; after all processes created by it finished.
- Statements for parallel execution are added in the programming lang to enable creation of processes and for waiting for them to complete.
- Two statements that are used for this purpose →

(1) `fork()` → which is used to create a process.

(2) `Join()` → which is used when the invoking process needs the result of the invoked processes to continue.

4

```

Process X
{
    _____
    _____
    _____
    fork(Y)
    _____
    join(Y)
    end(X)
}

Process Y
{
    _____
    _____
    _____
    end(Y);
}
  
```

The one of the main problem is inconsistency which can be resolved using semaphores.

```

Process A
{
    fork(B)
    lock(sum)
    sum += A
    unlock(sum)
    join(B)
    end(A)
}

Process B
{
    lock(sum);
    sum += B
    unlock(sum);
    end(B);
}
  
```

// main program PD - master, PI → slave
begin (main)

global sum, Array[1:N]

for i = 1 to N

read A[i]

end (for)

sum = 0;

Processor 1 executes

```
fork(1) Add_array (input A[N/2+1; N], output sum);
```

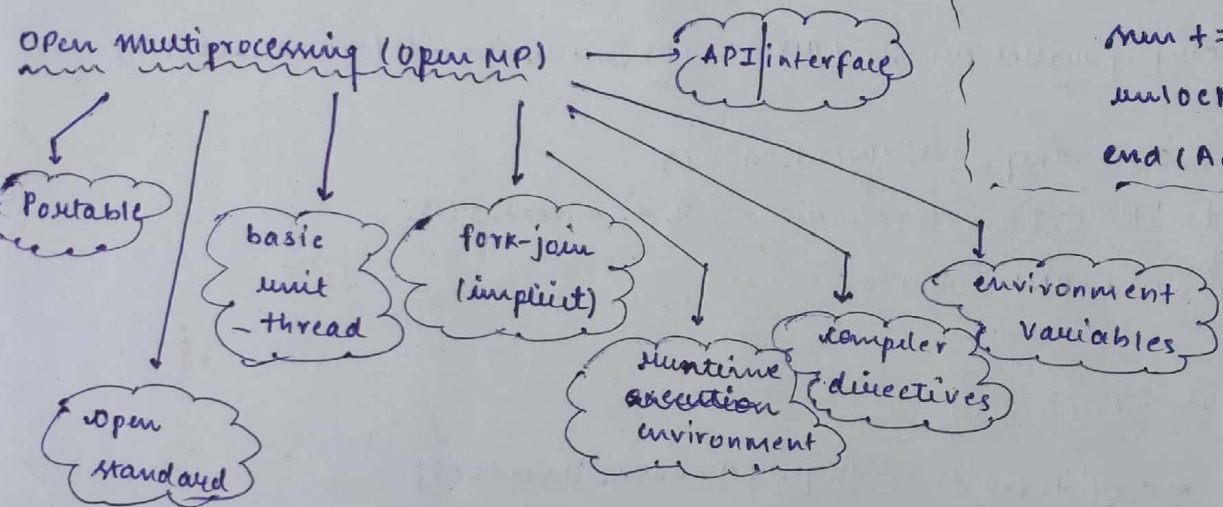
Processor 0 executes

```
Add_array (input A[1; N/2], output sum)
join(1)
write(sum);
end(main);
```

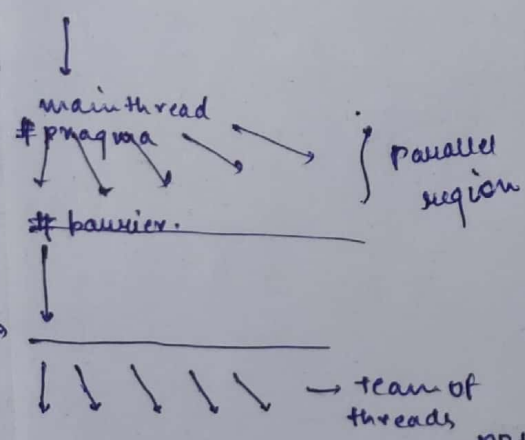
```
Add_array [input: A[P:M],
            output: sum];
```

```
begin Add_array
sum-local = 0;
for i = p to m:
    sum-local += A[i];
endfor
lock(sum)
sum += sum-local;
unlock(sum);
end Add_array;
```

15/02/21



- It is a portable standard for programming shared memory parallel computers.
- Like MPI, open MP is explicit programming model.
- open MP allows the programmer the facility of incremental parallelization



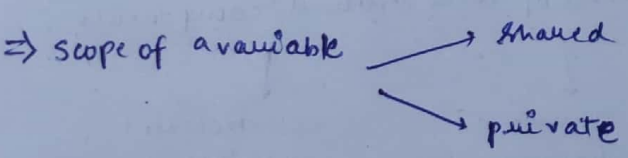
- open MP comprises of three distinct components
 - ↓ compiler directives
 - ↓ runtime library routines
 - ↓ environment variables

• The central entity in an open MP program is a thread not a process

- A open MP program creates multiple cooperating threads, which runs on multiple processor.
- The execution begins with the single thread called master thread, which executes the program sequentially until it encounters the first parallel construct.

- At the parallel construct, the master thread, creates a team of threads consisting of number of new threads called slaves.
- The fork and join operations are implicit
- At the end of the parallel region, there is a implicit barrier synchronization and only the master thread continues to further execution.

```
#include <stdio.h>
#include <omp.h>
int main() {
    int no_of_threads, thread_ID, THREAD_COUNT=4;
    #pragma omp parallel private (thread_ID) num_threads (THREAD_COUNT)
    {
        thread_ID = omp_get_thread_num();
        printf("Hello, I am thread number %d", thread_ID);
        * #pragma omp barrier;
        #pragma
        if (thread_ID == 0)
        {
            no_of_threads = omp_get_num_threads();
            printf("Master - My team, has %d threads", no_of_threads);
        }
    }
    return 0;
}
```



Loop-carried dependency

$X+1 = \text{Result}$ is dependent on the result of previous state

```
for (i = 1 to 10) {
    a[i] = a[i] + 3
    b[i] = b[i] + a[i-1]
}
```

→ these types of loops cannot be parallelized by open MP.

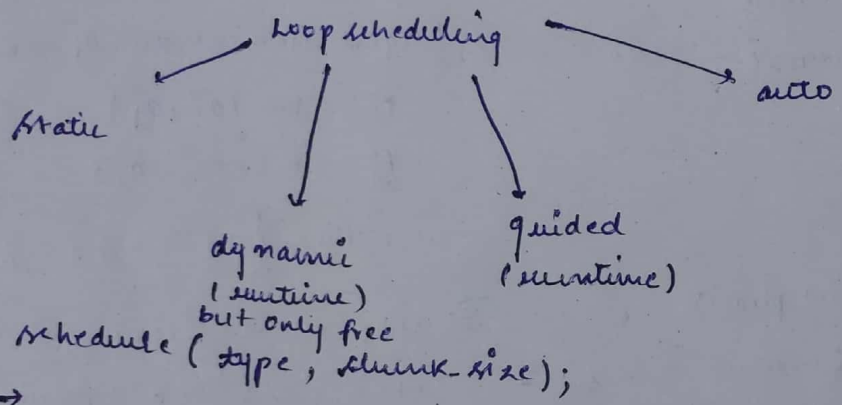
```
#pragma omp parallel for.
```

Loop scheduling in openMP

- It is possible to incrementally parallelize a sequential program, that has many for loops by successfully using openMP parallel for directive for each loop.
- However, this loop has 2 restrictions.

The total no. of iterations must be known in advanced

The iterations must be independent of each other.



- directives -> barrier
- critical -> multiple statements to restrict
- automatic -> single statements to lock (restrict) to avoid
- nowait -> synchronization delay at time of joining.
- reduction -> (operator, variable).

=> Environment variables -> or manipulate variables that are used at the time of runtime.
omp-dynanin, omp-^schedule
omp-stacksize, omp-no-of threads.

=> P-threads =

Odd even Transposition sort \rightarrow

carried out in 2 phases
odd phases
and even phase

compare
exchange
operation

compare exchange (P_i^o, P_j^o)

8

①

Let say there are 2 processors
 P_i and P_j having elements
 a_i and a_j . so in first steps both
processors exchange their values
such that both of them contains
both the elements.

②

Now, left processor contains
the smallest element and
right processor contains the
largest element out of them.

$$P_i^o = \min(a_i^o, a_j^o)$$

$$P_j^o = \max(a_i^o, a_j^o)$$

④ even phase \rightarrow (second phase)

$\langle a_2, a_3 \rangle$ same with even
 $\langle a_4, a_5 \rangle$ position elements

③ odd phase \rightarrow (first phase)

$\rightarrow \langle a_1, a_2 \rangle$ in odd phase elements of
 $\langle a_3, a_4 \rangle$ odd number/position is
compared to its right
element and.
compare exchange
operation is performed

for n number
of times

$n/2$
odd
phase

$n/2$
even
phase

\Rightarrow PRAM operations (sorting).

sort by
enumeration

\hookrightarrow each element compares itself
with other elements.

$S = \langle s_1, s_2, \dots, s_n \rangle$

$R = \langle r_1, r_2, \dots, r_n \rangle$

\hookrightarrow it is initially initialized to zero

\hookrightarrow The final position of the element s_i in the sorted sequence is given by placing
the element s_i in position $r_i + 1$.

Rank r_i of an element s_i is the number
of elements smaller than s_i in the
sorted sequence.

CRW sorting Implementation

9

for $i = 1$ to n do in parallel
 for $j = 1$ to n do in parallel
 if $s_i > s_j$ or $(s_i = s_j \text{ and } i > j)$ then
 $P_{i,j}$ writes 1 to r_i
 end if
end for
end for

P_1 (1,1)	P_2 (1,2)	P_3 (1,3)	P_4 (1,4)
P_5 (2,1)	P_6 (2,2)	P_7 (2,3)	P_8 (2,4)
P_9 (3,1)	P_{10} (3,2)	P_{11} (3,3)	P_{12} (3,4)
P_{13} (4,1)	P_{14} (4,2)	P_{15} (4,3)	P_{16} (4,4)

for $i = 1$ to n do in parallel
 $P_{i,1}$ puts in $(r_i + 1)$ position of S
end for

$S = \langle 12, 5, 7, 1 \rangle$

Here concurrent read and write operations are performed.

(12,12) (12,5)
 ↑
 no operation
 (12,7)
 ↓
 (12,1) " " " " " "
 ↓
 " " " " " "

$r_1 = [3 | 1 | 2 | 0]$ ←

So this rank matrix can be used to sort the arrays

after all the operations on r_i we add them all

CRWEW sorting

for $i = 1$ to n do in parallel ← concurrent read
 for $j = 1$ to n ← exclusive write
 if $(s_i > s_j)$ or $(s_i = s_j \text{ and } i > j)$ then
 $P_{i,j}$ adds 1 to r_i
 end if
end for

Here we only use n processors.

parallelly

s_1	s_2	s_3	s_4
s_1	s_1	s_1	s_1
s_2	s_2	s_2	s_2
s_3	s_3	s_3	s_3
s_4	s_4	s_4	s_4

This occurs serially

end for
 P_{i+1} puts s_i in $(r_i + 1)$ position of S
end for

EREW sorting

```

for i=1 to n do in parallel
  for j=0 to n-1
    k = (i+j) mod n
    if (s_i > s_k) or (s_i == s_k and i > k) then
      P_j adds .1 to r_j
    end if
  end for
  P_i put s_i in (r_i+1) position of
end for
  
```

Matrix Multiplication (PRAM)

```

for i=1 to m do
  for j=1 to k do
    c_ij = 0
    for s=1 to n do
      c_ij = c_ij + a_is x b_sj
    end for
  end for
end for
  
```

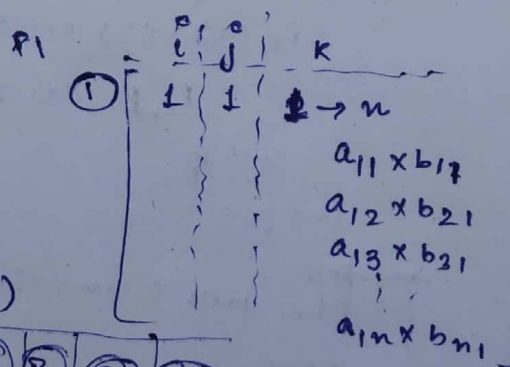
Simple matrix multiplication
 $[m \times k] \times [k \times n]$

CREW $\rightarrow n^2$
 EREW $\rightarrow n^2$
 CRCW $\rightarrow n^3$
 ERCW $\rightarrow \times$

for CREW \rightarrow

```

for i=1 to n do in parallel
  for j=1 to n do in parallel
    c_ij = 0
    for k=1 to n do
      c_ij = c_ij + (a_is x b_sj)
    end for
  end for
end for
  
```



	P_1	P_2	P_3	P_4	
$i=1$	1	2	3	4	$j=1$
$i=2$	5	6	7	8	$j=2$
$i=3$	9	10	11	12	$j=3$
$i=4$	13	14	15	16	$j=4$

EREW

for $i=1$ to n do in parallel

for $j=1$ to n do in parallel

$c_{ij} = 0$

for $k=1$ to n do

$rk = ((i+j+k) \bmod n) + 1$

$c_{ij} = c_{ij} + a_{ik} * b_{rkj}$

end for

end for

end for

$c_{11} += (a_{14} * b_{41})$ (11)

i	j	k	rk	
1	1	1	4	$a_{14} * b_{41}$
		2	1	$a_{11} * b_{11}$
		3	2	$a_{12} * b_{21}$
		4	3	$a_{13} * b_{31}$
1	2	1	1	$a_{11} * b_{12}$
		2	2	$a_{12} * b_{22}$
		3	3	$a_{13} * b_{32}$
		4	4	$a_{14} * b_{42}$
1	3	1	2	$a_{12} * b_{23}$
		2	3	$a_{13} * b_{33}$
		3	4	$a_{14} * b_{43}$
		4	1	$a_{11} * b_{13}$

P1

P2

P3

CRCW →

for $i=1$ to n do in parallel

for $j=1$ to n do in parallel

for $k=1$ to n do in parallel

$c_{ij} = 0$

$c_{ij} = a_{ik} * b_{rkj}$

end for

end for

end for

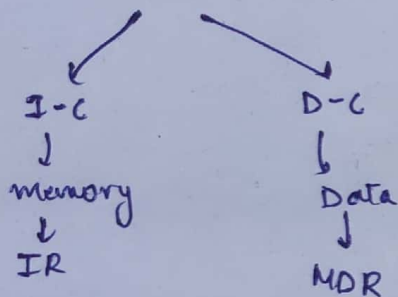
Inst. Level Parallelism

Ideal conditions

- (1) All instructions breakable into equal sized instructions. integer additions
floating point numbers add.
- (2) Sequential program (locality of references)
i.e. no branches.
- (3) switching time
- (4) Independent of each ~~resources~~ others.
- (5) sufficient resources.

RISC

Caches

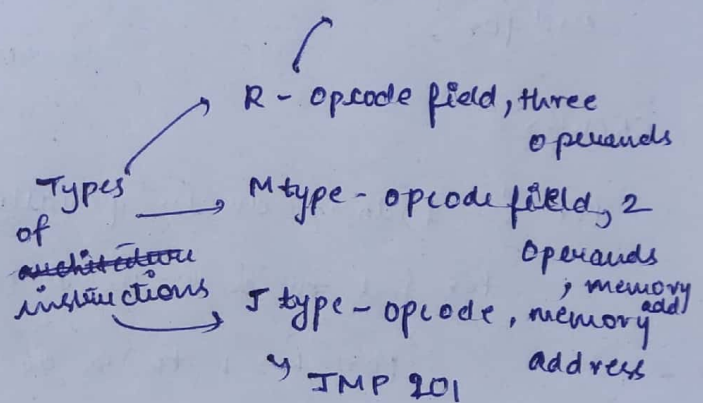


32 G PRS

Instruction execution cycle

- (1) Fetch instruction
- (2) Decode and fetch register
- (3) Execute and calculate ~~execution~~ effective address.
- (4) memory Access
- (5) Store in the memory.

ADD R1 R2 R1



- (2) program counter
- (3) only 2 operations can access your memory.
- (4) ALU at any single time
 - arithmetic
 - logical

clock cycle.