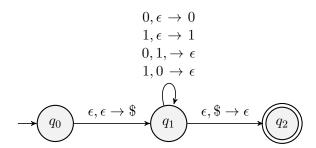
## CS F351 Theory of Computation Tutorial-7

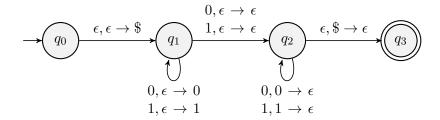
Problem 1 Find an equivalent CFG for the following PDAs:

(a)



Solution: See https://www.cse.cuhk.edu.hk/~siuon/csci3130-f18/slides/lec11.pdf

(b) \*



**Problem 2** Simplify the following CFG by removing useless symbols if any:

$$\begin{split} S &\rightarrow aSa \mid bB \mid bAA \\ A &\rightarrow abb \mid SbA \mid aB \\ B &\rightarrow AB \mid CaB \\ C &\rightarrow cC \mid Sa \mid bD \\ D &\rightarrow dD \mid \epsilon \end{split}$$

**Solution:**  $S \rightarrow aSa \mid bAA, A \rightarrow abb \mid SbA$ 

(see full solution at https://www.cs.scranton.edu/~mccloske/courses/cmps260/cfg\_remove\_useless.html.)

## Problem 3

Convert the following CFGs into chomsky normal form.

1.  $S \to aXbX$ ,  $X \to aY \mid bY \mid \epsilon$ ,  $Y \to X \mid c$ 

**Solution:** Remove  $\epsilon$  production:

$$S \rightarrow aXbX \mid abX \mid aXb \mid ab, \ X \rightarrow aY \mid bY \mid a \mid b, Y \rightarrow X \mid c$$

Remove unit production:

$$S \rightarrow aXbX \mid abX \mid aXb \mid ab, \ X \rightarrow aY \mid bY \mid a \mid b, \ Y \rightarrow aY \mid bY \mid a \mid b \mid c$$

Remove useless symbol:

$$S \rightarrow aXbX \mid abX \mid aXb \mid ab, \ X \rightarrow aY \mid bY \mid a \mid b, \ Y \rightarrow aY \mid bY \mid a \mid b \mid c$$

CNF:

$$S \to EF \mid AF \mid EB \mid AB$$

$$X \rightarrow AY \mid BY \mid a \mid b$$

$$Y \rightarrow AY \mid BY \mid a \mid b \mid c$$

$$E \to AX$$

$$F \to BX$$

$$A \to a$$

$$B \to b$$

$$C \rightarrow c$$

2. 
$$S \rightarrow aTb \mid bTa, T \rightarrow XTX \mid X \mid \epsilon, X \rightarrow a \mid b$$