0. Imports and Setting up Anthropic API Client

```
from google.colab import drive
drive.mount('/content/drive')

→ Mounted at /content/drive
!pip install python-dotenv
import os
import dotenv
dotenv.load_dotenv('/content/drive/MyDrive/.env')

→ Collecting python-dotenv

      Downloading python_dotenv-1.0.1-py3-none-any.whl (19 kB)
    Installing collected packages: python-dotenv
    Successfully installed python-dotenv-1.0.1
# Load Prompts and Problem Description
prompt1_path = '/content/drive/MyDrive/Thesis/Prompts/Prompt1_MathematicalModel.txt'
prompt2_path = '/content/drive/MyDrive/Thesis/Prompts/Prompt2_PyomoCode.txt'
problem_desc_path = '/content/drive/MyDrive/Thesis/ProblemDescriptions/NL/NL2.txt'
prompt1_file = open(prompt1_path, "r")
prompt2_file = open(prompt2_path, "r")
problem_desc_file = open(problem_desc_path, "r")
prompt1 = prompt1_file.read()
print("Prompt 1:\n", prompt1)
prompt2 = prompt2_file.read()
print("Prompt 2:\n", prompt2)
problem_desc = problem_desc_file.read()
print("Problem Description:\n", problem_desc)
→ Prompt 1:
     Please write a mathematical optimization model for this problem. Include parameters, decision variables, the objective
    Prompt 2:
     Please write a python pyomo code for this optimization problem.
    Use sample data where needed.
    Indicate where you use sample data.
    Problem Description:
     You are a chemist in charge of a process that requires two liquids to reach the end product. Your goal is to maximize t
!pip install anthropic
     Show hidden output
# Importing Anthropic & Setting Headers
import anthropic
client = anthropic.Anthropic(
   # defaults to os.environ.get("ANTHROPIC_API_KEY")
   api_key=os.environ.get("ANTHROPIC_API_KEY"),
```

1. Prompt 1: Create Mathematical Model

4. $X_2 \ge 0$

```
# Print response
print(response_p1)
🚁 Let's formulate the mathematical optimization model for the given problem. We will define the parameters, decision varia
     - Let the maximum capacity of the mixture tank be denoted as C, which is 80 liters.
    Decision Variables:
    - Let x1 be the number of liters of the first liquid component used.
     - Let x_2 be the number of liters of the second liquid component used.
     - The quality of the product is measured by the difference between the Napierian logarithm of the product of the liters
     - Maximize: \ln(x_1 \times x_2) - \sqrt[3]{(x_1 + 2x_2)}
    Constraints:
    1. Stability Constraint:
        - The squared difference between the liters used of each component and the mean liters used of both components should
        -(x_1 - (x_1 + x_2) / 2)^2 + (x_2 - (x_1 + x_2) / 2)^2 \le 10
    2. Capacity Constraint:
        - The sum of the liters used of both components should not exceed the maximum capacity of the mixture tank.
        - X_1 + X_2 \leq C
    3. Non-negativity Constraints:
        - The number of liters used for each component should be non-negative.
        - X_1 \ge 0
        - X_2 \ge 0
    Optimization Model:
    Maximize: ln(x_1 \times x_2) - \sqrt[3]{(x_1 + 2x_2)}
     1. (x_1 - (x_1 + x_2) / 2)^2 + (x_2 - (x_1 + x_2) / 2)^2 \le 10
    2. X_1 + X_2 \le 80
    3. X_1 \ge 0
```

This optimization model aims to maximize the quality of the product while satisfying the stability constraint, capacity

2. Prompt 2: Write Code based on Mathematical Model

```
message2 = client.messages.create(
   model="claude-3-opus-20240229",
    system=prompt2,
   max tokens=4069,
   messages=[
       {"role": "user", "content": response_p1}
   1
)
response p2 = message2.content[0].text
# Print response
print(response_p2)
    # create the mode:
⇒ model = ConcreteModel()
    # Define the parameters
    model.C = Param(initialize=80) # Maximum capacity of the mixture tank
    # Define the decision variables
    model.x1 = Var(domain=NonNegativeReals) # Liters of the first liquid component
    model.x2 = Var(domain=NonNegativeReals) # Liters of the second liquid component
    # Define the objective function
    def quality_rule(model):
        return log(model.x1 * model.x2) - (model.x1 + 2 * model.x2) ** (1/3)
    model.quality = Objective(rule=quality_rule, sense=maximize)
    # Define the constraints
    def stability_rule(model):
        mean = (model.x1 + model.x2) / 2
        return (model.x1 - mean)**2 + (model.x2 - mean)**2 <= 10
    model.stability = Constraint(rule=stability_rule)
```

```
# Print the results
print("Optimal Solution:")
print("x1 =", value(model.x1))
print("x2 =", value(model.x2))
print("Quality =", value(model.quality))
```

Explanation:

- 1. We import the necessary components from the `pyomo.environ` module.
- 2. We create a concrete model using `ConcreteModel()`.
- 3. We define the parameter `C` to represent the maximum capacity of the mixture tank, which is set to 80 liters.
- 4. We define the decision variables `x1` and `x2` to represent the liters of the first and second liquid components, r
- 5. We define the objective function `quality_rule` using the mathematical expression provided. The objective is to max
- 6. We define the stability constraint `stability_rule` using the given inequality. It ensures that the squared differe
- 7. We define the capacity constraint `capacity_rule` to ensure that the sum of the liters used of both components does
- 8. We create an instance of the solver using `SolverFactory('ipopt')`. You can choose a different solver if desired.
- 9. We solve the optimization problem using `solver.solve(model)`.
- 10. Finally, we print the optimal solution, including the values of `x1`, `x2`, and the quality objective.

4. Input Problem Data and Test Model Code

```
# Installing pyomo nd solver
!pip install -q pyomo
!wget -N -q "https://matematica.unipv.it/gualandi/solvers/ipopt-linux64.zip"
!unzip -o -q ipopt-linux64
                                                  - 12.8/12.8 MB 52.4 MB/s eta 0:00:00
\overline{2}
                                                  - 49.6/49.6 kB 5.0 MB/s eta 0:00:00
from pyomo.environ import *
# Create the model
model = ConcreteModel()
# Define the parameters
model.C = Param(initialize=80) # Maximum capacity of the mixture tank
# Define the decision variables
model.x1 = Var(domain=NonNegativeReals) # Liters of the first liquid component
model.x2 = Var(domain=NonNegativeReals) # Liters of the second liquid component
# Define the objective function
def quality_rule(model):
    return log(model.x1 * model.x2) - (model.x1 + 2 * model.x2) ** (1/3)
model.quality = Objective(rule=quality_rule, sense=maximize)
# Define the constraints
def stability_rule(model):
   mean = (model.x1 + model.x2) / 2
    return (model.x1 - mean)**2 + (model.x2 - mean)**2 <= 10
model.stability = Constraint(rule=stability_rule)
def capacity_rule(model):
    return model.x1 + model.x2 <= model.C
model.capacity = Constraint(rule=capacity_rule)
# Solve the optimization problem
solver = SolverFactory('ipopt')
solver.solve(model)
# Print the results
print("Optimal Solution:")
print("x1 =", value(model.x1))
print("x2 =", value(model.x2))
print("Quality =", value(model.quality))
→ Optimal Solution:
    x1 = 42.236067853543105
    x2 = 37.76393234768411
```

Quality = 2.473033919646447

5. Correct The Model Code to Test Mathematical Model (if applicable)