

## ✓ 0. Imports and Setting up Anthropic API Client

```
from google.colab import drive
```

```
drive.mount('/content/drive')
```

Mounted at /content/drive

```
!pip install python-dotenv
```

```
import os
import dotenv
```

```
dotenv.load_dotenv('/content/drive/MyDrive/.env')
```

Collecting python-dotenv  
 Downloading python\_dotenv-1.0.1-py3-none-any.whl (19 kB)  
 Installing collected packages: python-dotenv  
 Successfully installed python-dotenv-1.0.1  
 True

```
# Load Prompts and Problem Description
```

```
prompt1_path = '/content/drive/MyDrive/Thesis/Prompts/Prompt1_MathematicalModel.txt'
```

```
prompt2_path = '/content/drive/MyDrive/Thesis/Prompts/Prompt2_PyomoCode.txt'
```

```
problem_desc_path = '/content/drive/MyDrive/Thesis/ProblemDescriptions/MIP/MIP1.txt'
```

```
prompt1_file = open(prompt1_path, "r")
```

```
prompt2_file = open(prompt2_path, "r")
```

```
problem_desc_file = open(problem_desc_path, "r")
```

```
prompt1 = prompt1_file.read()
```

```
print("Prompt 1:\n", prompt1)
```

```
prompt2 = prompt2_file.read()
```

```
print("Prompt 2:\n", prompt2)
```

```
problem_desc = problem_desc_file.read()
```

```
print("Problem Description:\n", problem_desc)
```

Prompt 1:  
 Please write a mathematical optimization model for this problem. Include parameters, decision variables, the objective  
 Prompt 2:  
 Please write a python pyomo code for this optimization problem.  
 Use sample data where needed.  
 Indicate where you use sample data.  
 Problem Description:  
 You are a city planner, looking to open facilities at some locations. We have a set of customers and a set of possible  
 The goal is to minimize the overall costs, which include both the fixed activation costs for any opened facilities and t  
 Please formulate this as a mathematical optimization model.

```
!pip install anthropic
```

Show hidden output

```
# Importing Anthropic & Setting Headers
```

```
import anthropic
```

```
client = anthropic.Anthropic(
    # defaults to os.environ.get("ANTHROPIC_API_KEY")
    api_key=os.environ.get("ANTHROPIC_API_KEY"),
)
```

## ✓ 1. Prompt 1: Create Mathematical Model

```

message = client.messages.create(
    model="claude-3-opus-20240229",
    system=prompt1,
    max_tokens=4096,
    messages=[
        {"role": "user", "content": problem_desc}
    ]
)

```

```
response_p1 = message.content[0].text
```

```

# Print response
print(response_p1)

```

Great! Let's formulate this problem as a mathematical optimization model. We'll define the necessary sets, parameters, d

Sets:

- I: Set of customers
- J: Set of potential facility locations

Parameters:

- $d_i$ : Demand of customer  $i \in I$
- $f_j$ : Fixed annual activation cost for facility  $j \in J$
- $c_{ij}$ : Transportation cost for servicing customer  $i \in I$  from facility  $j \in J$
- $M_j$ : Maximum annual service volume for facility  $j \in J$

Decision Variables:

- $x_{ij}$ : Fraction of customer  $i$ 's demand serviced by facility  $j$  (continuous variable,  $0 \leq x_{ij} \leq 1$ )
- $y_j$ : Binary variable indicating whether facility  $j$  is opened (1) or not (0)

Objective Function:

Minimize total costs = Fixed activation costs + Transportation costs  
 $\min \sum_{j \in J} f_j * y_j + \sum_{i \in I} \sum_{j \in J} c_{ij} * d_i * x_{ij}$

Constraints:

1. Each customer's demand must be fully met:  
 $\sum_{j \in J} x_{ij} = 1, \forall i \in I$
2. Each facility's service volume cannot exceed its maximum annual limit:  
 $\sum_{i \in I} d_i * x_{ij} \leq M_j * y_j, \forall j \in J$
3. Customers can only be serviced by opened facilities:  
 $x_{ij} \leq y_j, \forall i \in I, \forall j \in J$
4. Non-negativity and binary constraints:  
 $0 \leq x_{ij} \leq 1, \forall i \in I, \forall j \in J$   
 $y_j \in \{0, 1\}, \forall j \in J$

The objective function minimizes the total costs, which include the fixed activation costs for opened facilities and the

This formulation represents the problem as a mixed-integer linear programming (MILP) model, which can be solved using op

## 2. Prompt 2: Write Code based on Mathematical Model

```

message2 = client.messages.create(
    model="claude-3-opus-20240229",
    system=prompt2,
    max_tokens=4096,
    messages=[
        {"role": "user", "content": response_p1}
    ]
)

```

```
response_p2 = message2.content[0].text
```

```

# Print response
print(response_p2)

```



```

model.x = Var(model.I, model.J, bounds=(0, 1))
model.y = Var(model.J, within=Binary)

# Define objective function
def obj_rule(model):
    return sum(model.f[j] * model.y[j] for j in model.J) + \
           sum(model.c[i, j] * model.d[i] * model.x[i, j] for i in model.I for j in model.J)
model.obj = Objective(rule=obj_rule, sense=minimize)

# Define constraints
def demand_constraint_rule(model, i):
    return sum(model.x[i, j] for j in model.J) == 1
model.demand_constraint = Constraint(model.I, rule=demand_constraint_rule)

def capacity_constraint_rule(model, j):
    return sum(model.d[i] * model.x[i, j] for i in model.I) <= model.M[j] * model.y[j]
model.capacity_constraint = Constraint(model.J, rule=capacity_constraint_rule)

def service_constraint_rule(model, i, j):
    return model.x[i, j] <= model.y[j]
model.service_constraint = Constraint(model.I, model.J, rule=service_constraint_rule)

# Solve the model
solver = SolverFactory('glpk')
results = solver.solve(model)

# Print the results
print("Objective value:", value(model.obj))
print("Facility openings:")
for j in model.J:
    if value(model.y[j]) > 0.5:
        print(f"Facility {j} is opened")
print("Customer assignments:")
for i in model.I:
    for j in model.J:
        if value(model.x[i, j]) > 0.001:
            print(f"Customer {i} is serviced by Facility {j}: {value(model.x[i, j]):.2f}")
...

```

In this code, I have used sample data for the demand, fixed activation costs, maximum annual service volumes, and tran

The code follows the mathematical formulation we discussed earlier. It creates sets for customers and facilities, defi

...

## ✓ 4. Input Problem Data and Test Model Code

```

# Installing pyomo and solver
!pip install -q pyomo
!apt-get install -y -qq glpk-utils
!pip install glpk

```

 Show hidden output

```

from pyomo.environ import *

# Sample data
customers = ['C1', 'C2', 'C3', 'C4', 'C5']
facilities = ['F1', 'F2', 'F3']

demand = {'C1': 80, 'C2': 270, 'C3': 250, 'C4': 160, 'C5': 180} # Sample demand data
fixed_cost = {'F1': 1000, 'F2': 1000, 'F3': 1000} # Sample fixed activation costs
max_capacity = {'F1': 500, 'F2': 500, 'F3': 500} # Sample maximum annual service volumes

# Sample transportation costs (c_ij)
trans_cost = {
    ('C1', 'F1'): 4, ('C1', 'F2'): 6, ('C1', 'F3'): 9,
    ('C2', 'F1'): 5, ('C2', 'F2'): 4, ('C2', 'F3'): 7,
    ('C3', 'F1'): 6, ('C3', 'F2'): 3, ('C3', 'F3'): 4,
    ('C4', 'F1'): 8, ('C4', 'F2'): 5, ('C4', 'F3'): 3,
    ('C5', 'F1'): 10, ('C5', 'F2'): 8, ('C5', 'F3'): 4
}

# Create the Pyomo model
model = ConcreteModel()

# Define sets
model.I = Set(initialize=customers)
model.J = Set(initialize=facilities)

# Define parameters
model.d = Param(model.I, initialize=demand)
model.f = Param(model.J, initialize=fixed_cost)

```

```

model.c = Param(model.I, model.J, initialize=trans_cost)
model.M = Param(model.J, initialize=max_capacity)

# Define decision variables
model.x = Var(model.I, model.J, bounds=(0, 1))
model.y = Var(model.J, within=Binary)

# Define objective function
def obj_rule(model):
    return sum(model.f[j] * model.y[j] for j in model.J) + \
           sum(model.c[i, j] * model.d[i] * model.x[i, j] for i in model.I for j in model.J)
model.obj = Objective(rule=obj_rule, sense=minimize)

# Define constraints
def demand_constraint_rule(model, i):
    return sum(model.x[i, j] for j in model.J) == 1
model.demand_constraint = Constraint(model.I, rule=demand_constraint_rule)


def capacity_constraint_rule(model, j):
    return sum(model.d[i] * model.x[i, j] for i in model.I) <= model.M[j] * model.y[j]
model.capacity_constraint = Constraint(model.J, rule=capacity_constraint_rule)

def service_constraint_rule(model, i, j):
    return model.x[i, j] <= model.y[j]
model.service_constraint = Constraint(model.I, model.J, rule=service_constraint_rule)

# Solve the model
solver = SolverFactory('glpk')
results = solver.solve(model)

# Print the results
print("Objective value:", value(model.obj))
print("Facility openings:")
for j in model.J:
    if value(model.y[j]) > 0.5:
        print(f"Facility {j} is opened")
print("Customer assignments:")
for i in model.I:
    for j in model.J:
        if value(model.x[i, j]) > 0.001:
            print(f"Customer {i} is serviced by Facility {j}: {value(model.x[i, j]):.2f}")

```

 Objective value: 5609.999999999998  
 Facility openings:  
 Facility F2 is opened  
 Facility F3 is opened  
 Customer assignments:  
 Customer C1 is serviced by Facility F2: 1.00  
 Customer C2 is serviced by Facility F2: 1.00  
 Customer C3 is serviced by Facility F2: 0.60  
 Customer C3 is serviced by Facility F3: 0.40  
 Customer C4 is serviced by Facility F3: 1.00  
 Customer C5 is serviced by Facility F3: 1.00

## ✓ 5. Correct The Model Code to Test Mathematical Model (if applicable)