

0. Imports and Setting up Anthropic API Client

```
from google.colab import drive
```

```
drive.mount('/content/drive')
```

Mounted at /content/drive

```
!pip install python-dotenv
```

```
import os
import dotenv
```

```
dotenv.load_dotenv('/content/drive/MyDrive/.env')
```

Collecting python-dotenv
 Downloading python_dotenv-1.0.1-py3-none-any.whl (19 kB)
 Installing collected packages: python-dotenv
 Successfully installed python-dotenv-1.0.1
 True

```
# Load Prompts and Problem Description
```

```
prompt1_path = '/content/drive/MyDrive/Thesis/Prompts/Prompt1_MathematicalModel.txt'
```

```
prompt2_path = '/content/drive/MyDrive/Thesis/Prompts/Prompt2_PyomoCode.txt'
```

```
problem_desc_path = '/content/drive/MyDrive/Thesis/ProblemDescriptions/NL/NL1.txt'
```

```
prompt1_file = open(prompt1_path, "r")
```

```
prompt2_file = open(prompt2_path, "r")
```

```
problem_desc_file = open(problem_desc_path, "r")
```

```
prompt1 = prompt1_file.read()
```

```
print("Prompt 1:\n", prompt1)
```

```
prompt2 = prompt2_file.read()
```

```
print("Prompt 2:\n", prompt2)
```

```
problem_desc = problem_desc_file.read()
```

```
print("Problem Description:\n", problem_desc)
```

Prompt 1:
 Please write a mathematical optimization model for this problem. Include parameters, decision variables, the objective
 Prompt 2:
 Please write a python pyomo code for this optimization problem.
 Use sample data where needed.
 Indicate where you use sample data.
 Problem Description:
 A firm that packs refreshments and beers, situated in the province of Valencia (Spain) employs the same syrup to produc
 49000 times X1 minus X1 squared plus 30 times X2 minus two times X2 squared.
 It costs 150 dollars to buy and process each hectolitre of syrup. The S1 packaging line has a net capacity of producing

```
!pip install anthropic
```

Show hidden output

```
# Importing Anthropic & Setting Headers
```

```
import anthropic
```

```
client = anthropic.Anthropic(
```

```
    # defaults to os.environ.get("ANTHROPIC_API_KEY")
```

```
    api_key=os.environ.get("ANTHROPIC_API_KEY"),
```

```
)
```

1. Prompt 1: Create Mathematical Model

```
message = client.messages.create(
    model="claude-3-opus-20240229",
    system=prompt1,
    max_tokens=4096,
    messages=[
        {"role": "user", "content": problem_desc}
    ]
)
```

```
response_p1 = message.content[0].text
```

```
# Print response
print(response_p1)
```

↩ Let's formulate the mathematical optimization model for this problem.

Parameters:

- Cost of buying and processing each hectolitre of syrup: \$150
- Hourly production capacity of S1 packaging line: 7100 units
- Daily working hours: 8 hours
- 1 hectolitre of syrup produces 40 units of 1.5 l COLI and 20 units of 1.5 l PEPSA

Decision Variables:

- X1: Units of 1.5 l COLI product produced daily
- X2: Units of 1.5 l PEPSA product produced daily

Objective Function:

Maximize the daily profit (in dollars):

$$49000X1 - X1^2 + 30X2 - 2X2^2 - 150(X1/40 + X2/20)$$

Constraints:

1. Production capacity constraint:

$$X1 + X2 \leq 7100 \times 8 = 56800$$

2. PEPSA production constraint:

$$X2 \geq 0.5X1$$

3. Non-negativity constraints:

$$X1 \geq 0$$

$$X2 \geq 0$$

The complete optimization model can be written as follows:

Maximize:

$$49000X1 - X1^2 + 30X2 - 2X2^2 - 150(X1/40 + X2/20)$$

Subject to:

$$X1 + X2 \leq 56800$$

$$X2 \geq 0.5X1$$

$$X1 \geq 0$$

$$X2 \geq 0$$

This model aims to maximize the daily profit by determining the optimal production quantities of 1.5 l COLI (X1) and 1.5

✓ 2. Prompt 2: Write Code based on Mathematical Model

```
message2 = client.messages.create(
    model="claude-3-opus-20240229",
    system=prompt2,
    max_tokens=4069,
    messages=[
        {"role": "user", "content": response_p1}
    ]
)
```

```
response_p2 = message2.content[0].text
```

```
# Print response
print(response_p2)
```

↩ Great! Now that we have formulated the mathematical optimization model, let's implement it in Python using the Pyomo lib

```
```python
from pyomo.environ import *

Create a Concrete Model
model = ConcreteModel()

Define decision variables
model.X1 = Var(domain=NonNegativeReals)
model.X2 = Var(domain=NonNegativeReals)

Define the objective function
model.profit = Objective(expr=49000*model.X1 - model.X1**2 + 30*model.X2 - 2*model.X2**2 - 150*(model.X1/40 + model.X2/20))

Define constraints
model.capacity_constraint = Constraint(expr=model.X1 + model.X2 <= 56800)
model.pepsa_constraint = Constraint(expr=model.X2 >= 0.5*model.X1)

Solve the optimization problem
solver = SolverFactory('ipopt')
```

```

results = solver.solve(model)

Print the optimal solution
print("Optimal Solution:")
print("X1 (1.5 l COLI):", model.X1.value)
print("X2 (1.5 l PEPSA):", model.X2.value)
print("Maximum Profit:", model.profit())
` ``

```

In this code:

1. We import the necessary components from the `pyomo.environ` module.
2. We create a `ConcreteModel` instance named `model` to represent our optimization problem.
3. We define the decision variables `X1` and `X2` using `Var()` and specify their domain as non-negative real numbers using `NonNegativeReals`.
4. We define the objective function using `Objective()` and specify the expression for the daily profit. The `sense` parameter is set to `maximize`.
5. We define the constraints using `Constraint()`:
  - The production capacity constraint:  $X1 + X2 \leq 56800$
  - The PEPSA production constraint:  $X2 \geq 0.5 \times X1$
6. We create an instance of the solver using `SolverFactory('ipopt')`. You can use other solvers based on your preferences.
7. We solve the optimization problem using `solver.solve(model)` and store the results in the `results` variable.
8. Finally, we print the optimal solution, including the values of `X1` and `X2`, and the maximum profit obtained.

Note: In this code, we are not using any sample data as all the necessary information is already provided in the problem.

You can run this Python script to obtain the optimal solution for the given optimization problem.

## 4. Input Problem Data and Test Model Code

```

Installing pyomo and solver
!pip install -q pyomo
!wget -N -q "https://matematica.unipv.it/gualandi/solvers/ipopt-linux64.zip"
!unzip -o -q ipopt-linux64

```

```

12.8/12.8 MB 73.8 MB/s eta 0:00:00
49.6/49.6 kB 5.4 MB/s eta 0:00:00

```

```

from pyomo.environ import *

Create a Concrete Model
model = ConcreteModel()

Define decision variables
model.X1 = Var(domain=NonNegativeReals)
model.X2 = Var(domain=NonNegativeReals)

Define the objective function
model.profit = Objective(expr=49000*model.X1 - model.X1**2 + 30*model.X2 - 2*model.X2**2 - 150*(model.X1/40 + model.X2/20), sense=maximize)

Define constraints
model.capacity_constraint = Constraint(expr=model.X1 + model.X2 <= 56800)
model.pepsa_constraint = Constraint(expr=model.X2 >= 0.5*model.X1)

Solve the optimization problem
solver = SolverFactory('ipopt')
results = solver.solve(model)

Print the optimal solution
print("Optimal Solution:")
print("X1 (1.5 l COLI):", model.X1.value)
print("X2 (1.5 l PEPSA):", model.X2.value)
print("Maximum Profit:", model.profit())

Optimal Solution:
X1 (1.5 l COLI): 16335.8333333340004
X2 (1.5 l PEPSA): 8167.916666666004
Maximum Profit: 400289176.04199195

```

## 5. Correct The Model Code to Test Mathematical Model (if applicable)

