

# RIAJUDDIN \_ Master Theorem Solution

1.  $T(n) = 3T(n/2) + n$  ----->  $\Theta(n^{\log_3 2}) = \Theta(n)$
2.  $T(n) = 64T(n/8) - n^2(\log n)$  -----> Not Applicable
3.  $T(n) = 2nT(n/2) + n^n$  -----> Not Applicable
4.  $T(n) = 3T(n/3) + n/2$  ----->  $\Theta(n^{\log_3 3} \log^{1/2+1} n) = \Theta(n \log n)$ .
5.  $T(n) = 7T(n/3) + n^2$  ----->  $\Theta(n^d) = \Theta(n^2)$ .

Solution...

1)  $T(n) = 3T(n/2) + n$ .

Here  $a=3, b=2$  as per master theorem case -3  $\Theta(n^{\log_b a})$  if  $a > (b^d)$  the time complexity for is  $\Theta(n^{\log_3 2}) = \Theta(n)$ .

2)  $T(n) = 64T(n/8) - n^2(\log n)$ .

In this case master theorem will not apply.

3)  $T(n) = 2nT(n/2) + n^n$ .

In this case  $a$  is not constant so master theorem will not apply.

4)  $T(n) = 3T(n/3) + n/2$ .

Here  $a=3, b=3, d=2$  as per master theorem case -2  $\Theta(n \log_b^a \log^{k+1} n)$  the time complexity for is  $\Theta(n^{\log_3 3} \log^{1/2+1} n) = \Theta(n \log n)$ .

5)  $T(n) = 7T(n/3) + n^2$

Here  $a=7, b=2$  as per master theorem case -1  $\Theta(n^d)$  if  $a < (b^d)$  the time complexity for is  $\Theta(n^d) = \Theta(n^2)$ .