Factorization in Deep Neural Networks



Factorization in Deep Neural Networks



Course organisation

Sessions

- Deep Learning and Transfer Learning,
- 2 Data Augmentation and Self Supervised Learning,
- 3 Quantization,
- 4 Pruning,
- 5 Factorization,
- 6 Distillation,
- **7** Embedded Software and Hardware for DL.
- 8 Presentations for challenge.

Factorization in Deep Neural Networks

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- Pruning.
- Factorization
- Distillation. ■ Embedded Software and Hardware for DL. Presentations for challenge.

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Factorization in Deep Neural Networks

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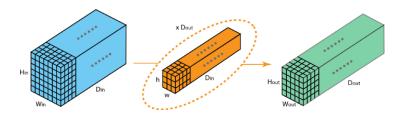
Factorization of Convolutional Networks

Why?

- Reduce memory footprint
- Reduce number of operations

How?

Modifying (decomposing, simplifying) convolutional filters structure



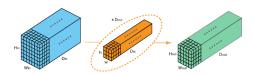
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Factorization in Deep Neural Networks

-Factorization of Convolutional Networks

Terminology: kernel: small filter of dimension h x w, filter: ensemble of kernels channels-features map: Din, Dout

General principle



Complexity of 2D Convolutions

 $N_{ops} = H_{out} \cdot W_{out} \cdot h \cdot w \cdot D_{in} \cdot D_{out}$ with kernel size (h, w), D_{in} the number of input feature maps, D_{out} the number of output feature maps of height H_{out} and width W_{out} .

To reduce the number of parameters, we can:

- Reduce the size of kernels
- Reduce the number of feature maps

Different strategies:

- Decompose kernels (Spatial separable convolutions)
- Depthwise Separable Convolutions
- Grouped



Factorization in Deep Neural Networks

—General principle

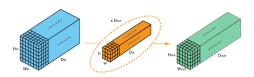


Reduce the number of feature map

Different strategies :

Depthwise Separable Convolutions

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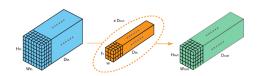


Factorization in Deep Neural Networks

—General principle



General principle



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Factorization in Deep Neural Networks

-General principle



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Decompose Kernels

Spatially separable convolutions

To simplify, assuming $D_{in} = D_{out}$, decompose (h, w) kernel by (h, 1) and (1, w):

$$N_{ops} = h \cdot 1 \cdot D_{in} + 1 \cdot w \cdot D_{in} = (h + w) \cdot D_{in}$$
 with kernel size (h, w) , D_{in} input and out number of feature maps.

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} \times \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}$$

Factorization in Deep Neural Networks $\frac{\text{Softman}}{\text{Response}} = \frac{\text{Softman}}{\text{Response}} = \frac{\text{Response}}{\text{Response}} = \frac{\text{Response}}{\text{Response}}$

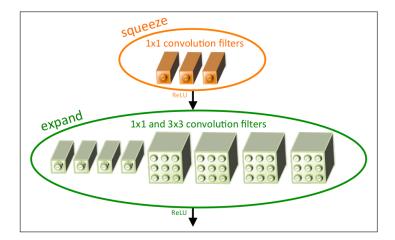
-Decompose Kernels

is Astronectic convolutions $\sum_{i=1}^{n} \sum_{k=1}^{n} \sum_{i=1}^{n} \sum_{k=1}^{n} \sum_{i=1}^{n} \sum_{k=1}^{n} \sum_{i=1}^{n} \sum_{k=1}^{n} \sum_{i=1}^{n} \sum_{k=1}^{n} \sum_{i=1}^{n} \sum_{k=1}^{n} \sum_{i=1}^{n} \sum_{i=1}^{n}$

In convolution, the 3x3 kernel directly convolves with the image. In spatially separable convolution, the 3x1 kernel first convolves with the image. Then the 1x3 kernel is applied. This would require 6 instead of 9 parameters while doing the same operations. Although decomposing kernels (spatially separable convolutions) saves cost, it is rarely used in deep learning. One of the main reason is that not all kernels can be divided into two, smaller kernels

Example: SqueezeNet

Introducing the Fire Module



landola et al. 2016, https://arxiv.org/abs/1602.07360



Factorization in Deep Neural Networks

transpire SqueezeNet

Introducing the Five Models

The Additional Control of the Control of the

Example: SqueezeNet

We can however cite an example based on the same principle of reducing kernel size SqueezeNet. Two main strategies: replace 3x3 filters with 1x1 filters and reduce the channels in input to 3x3 filters -squeeze layers- then in the expand layers has a mix of 1x1 and 3x3 filters. They also use stride > 1 to downsample activation maps later towards the end of the architecture to maximize accuracy on a limited budget of parameters. Reduce x50 number of parameters with AlexNet level accuracy.

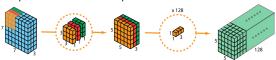
Depthwise separable convolutions

Instead of learning parameters that recombine all input feature maps to compute each output feature map:



$$N_{mul}^{N} = H_{out} \cdot W_{out} \cdot h \cdot w \cdot D_{in} \cdot D_{out} = 5 \cdot 5 \cdot 3 \cdot 3 \cdot 3 \cdot 128 = 86400$$

One can separate the operations into two steps:



$$\begin{split} N_{mul}^D &= H_{out} \cdot W_{out} \cdot h \cdot w \cdot D_{in} \cdot 1 + H_{out} \cdot W_{out} \cdot 1 \cdot 1 \cdot D_{in} \cdot D_{out} \\ N_{mul}^D &= 5 \cdot 5 \cdot 3 \cdot 3 \cdot 3 \cdot 1 + 5 \cdot 5 \cdot 1 \cdot 1 \cdot 3 \cdot 128 = 10275 \\ N_{mul}^D &= \left(\frac{1}{D_{out}} + \frac{1}{h^2}\right) \cdot N_{mul}^N, h = w \end{split}$$

https://towardsdatascience.com/

Factorization in Deep Neural Networks

-Depthwise separable convolutions

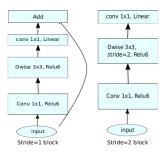
A standard convolution both filters and combines inputs into a new set of outputs in one step. The depthwise separable convolution splits this into two layers, depthwise convolutions and pointwise convolutions. We use depthwise convolutions to apply a single filter per each input channel (input depth). Pointwise convolution, a simple 1×1 convolution, is then used to create a linear combination of the output of the depthwise layer. Drawbacks: Depthwise separable convolutions reduces the number of parameters in the convolution. As such, for a small model, the model capacity may be decreased significantly if the 2D convolutions are replaced by depthwise separable convolutions. As a result, the model may become sub-optimal. However, if properly used, depthwise separable convolutions can give you the efficiency without dramatically damaging your model performance.

Example: MobileNet

MobileNetV1

Dwise 3x3, stride=s, Relu6

MobileNetV2



https://arxiv.org/abs/1704.04861, https://arxiv.org/abs/1801.04381



Factorization in Deep Neural Networks

Example: MobileNet



Depthwise separable convolutions were first introduced in the MobileNet paper (2017), that is a still a reference for embedded and mobile applications (small and low latency networks). For SqueezeNet and MobileNet factorized convolutions are used to drastically reduce parameters and operations wrt their counterpart. In Mobile Net 2, on the assumption that there is a lower dimension manifold in with the features space can be mapped, a linear bottleneck layer is added in the convolutional blocks (maps into lower dim, but without non linearity that destroy too much info). Also, shortcuts between bottleneck are added (same reason that for classical residual connections). MobileNet2 further decrease memory footprint wtr V1.

Example: MobileNet

Table 9. Smaller MobileNet Comparison to Popular Models

ImageNet	Million	Million
Accuracy	Mult-Adds	Parameters
60.2%	76	1.32
57.5%	1700	1.25
57.2%	720	60
	Accuracy 60.2% 57.5%	Accuracy Mult-Adds 60.2% 76 57.5% 1700

Table 10. MobileNet for Stanford Dogs

Model	Top-1	Million	Million
	Accuracy	Mult-Adds	Parameters
Inception V3 [18]	84%	5000	23.2
1.0 MobileNet-224	83.3%	569	3.3
0.75 MobileNet-224	81.9%	325	1.9
1.0 MobileNet-192	81.9%	418	3.3
0.75 MobileNet-192	80.5%	239	1.9

https://arxiv.org/abs/1704.04861.https://arxiv.org/abs/1801.04381



Factorization in Deep Neural Networks

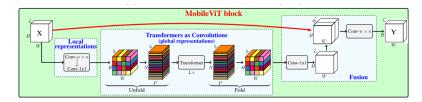
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More recent examples: MobileVit and VMamba

- MobileVit, a Light weight Vision Transformer https://arxiv.org/pdf/2110.02178.pdf
- VMamba, another efficient alternative to Vision Transformer https://arxiv.org/pdf/2401.10166.pdf





Factorization in Deep Neural Networks

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WidelyThink

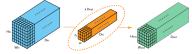
WidelyThin



Grouped Convolutions

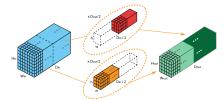
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feature map:



$$N_{mul}^{N} = H_{out} \cdot W_{out} \cdot h \cdot w \cdot D_{in} \cdot D_{out}$$

One can divide the kernels into multiple groups:



$$N_{mul}^{G} = H_{out} \cdot W_{out} \cdot h \cdot w \cdot \frac{D_{in}}{2} \cdot \frac{D_{out}}{2} + H_{out} \cdot W_{out} \cdot h \cdot w \cdot \frac{D_{in}}{2} \cdot \frac{D_{out}}{2}$$

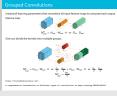
$$N_{mul}^{G} = \frac{N_{mul}^{N}}{2}$$

https://towardsdatascience.com/

a-comprehensive-introduction-to-different-types-of-convolutions-in-deep-learning-669281e58215

Factorization in Deep Neural Networks

-Grouped Convolutions



The first filter group (yellow) convolves with the first half of the input layer ([:, :, 0:Din/2]), while the second filter group (red) convolves with the second half of the input layer ([:, :, Din/2:Din]). As a result, each filter group creates Dout/2 channels that are stacked to obtain the output layer with Dout channels.

Examples

AlexNet filters



ResNeXt block

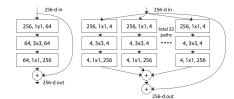


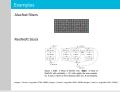
Figure 1. **Left**: A block of ResNet [14]. **Right**: A block of ResNeXt with cardinality = 32, with roughly the same complexity. A layer is shown as (# in channels, filter size, # out channels).

 ${\tt https://arxiv.org/abs/1704.04861, https://arxiv.org/abs/1801.04381, https://arxiv.org/abs/1611.05431.05431, https://arxiv.org/abs/1601.05431.05431, https://arxiv.org/abs/1601.05431.05431, https://arxiv.org/abs/1601.05431, https://arxiv.org$



Factorization in Deep Neural Networks

∟Examples



Grouped convolutions were first used in AlexNet to use 2 GPUs (parallelize efficiently). Authors showed that groups of filters were learning salient features (black-and-white and color filters). Grouped convolutions are used ResNeXt architecture from facebook: compared to a resnet block, an additional (to width and depth) dimension (cardinality) is added that exploits grouped convolutions and correspond to the number of groups. While for SqueezeNet and MobileNet grouped convolutions are used to reduce parameters and operation, in ResNeXt to boost accuracy (better than ResNet counterpart).

Combining Factorization with other Techniques: **Attention based Pruning**

Introducing Shift Attention Layer

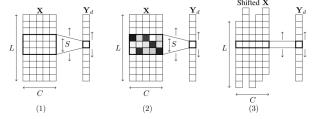


Figure 1: Overview of the proposed method: we depict here the computation for a single output feature map d, considering a 1d convolution and its associated shift version. Panel (1) represents a standard convolutional operation: the weight filter $\mathbf{W}_{d,...}$ containing SC weights is moved along the spatial dimension (L) of the input to produce each output in \mathbf{Y}_d . In panel (2), we depict the attention tensor A on top of the weight filter: the darker the cell, the most important the corresponding weight has been identified to be. At the end of the training process, A should contain only binary values with a single 1 per slice $A_{d.c.}$. In panel (3), we depict the corresponding obtained shift layer: for each slice along the input feature maps (C), the cell with the highest attention is kept and the others are disregarded. As a consequence, the initial convolution with a kernel size S has been replaced by a convolution with a kernel size 1 on a shifted version of the input X. As such, the resulting operation in panel (3) is exactly the same as the shift layer introduced in Wu et al. [2017], but here the shifts have been trained instead of being arbitrarily predetermined.

Hacene et al. 2019, https://arxiv.org/abs/1905.12300



Factorization in Deep Neural Networks

-Combining Factorization with other Techniques: Attention based Pruning



A recent work from our lab that propose an alternative to classical convolutions using shift convolutions that are a combination of a shift layer + 1d convolution. This figure illustrates the principle for a 1d convolution example is considered. A shift layer is obtained when connections in W are pruned so that exactly one connection remains for each slice. Novelty of this work: method that learns which shifts to perform during the training process (attention based pruning during training, matrix of attention A is then binarized) instead of fixed shift. The Figure (7) is from the same paper compares SAL with some other compression methods. In our evaluation we compare SAL with Binary Connect (BC) to Resnet-20, MobileNetV2 and Squeezenet. SAL is also compared with another version denoted SAL2, in which we keep two weights per kernel instead of one. We use Resnet-20 with different number of weights and activations as baseline. SAL and SAL2 outperform all other methods

Combining Factorization with other Techniques: Attention based Pruning

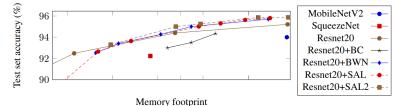


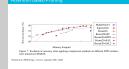
Figure 7: Evolution of accuracy when applying compression methods on different DNN architectures trained on CIFAR10.

Hacene et al. 2019, https://arxiv.org/abs/1905.12300



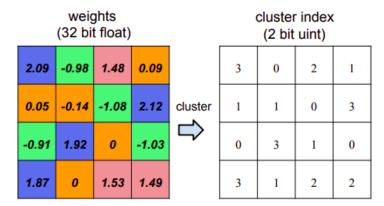
Factorization in Deep Neural Networks

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Combining Factorization with other Techniques: using clustering to share kernel weights



from https://arxiv.org/abs/1510.00149

Factorization in Deep Neural Networks

Combining Factorization with other
Techniques: using clustering to share kernel

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	weights (32 bit float)			cluster index (2 bit uint)				
.00	-0.98	1.48	0.09		3	۰	2	1
.05	-0.14	-1.08	2.12	cluster	1	1	۰	3
.91	1.92	0	-1.03	⇨	0	3	1	۰
.87	0	1.53	1,49		3	1	2	2

Lab Session

Factorizing a CNNs using Pytorch

- Read carefully the documentation of conv2d (https://pytorch.org/docs/stable/generated/torch.nn.Conv2d.html#conv2d) and play with the parameters in channels, out channels and groups to implement factorised convolutions
- Have a look at the MobileNet implementation for CIFAR10 (https://github.com/kuangliu/pytorch-cifar/blob/master/models/mobilenet.py)

Work for your Long Project

- If you haven't done it yet, familiarise yourself with the micronet-resources folder (profile.py and challenge rules)
- Combine/test different strategies to improve your MicroNet score!

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Factorization in Deep Neural Networks

Lab Session

Session

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-Overview of unsupervised learning

អ្ន Factorization in Deep Neural Networks

 Overview of unsupervised learning Clustering · Decomposition using Sparse Dictionary Learning

- Overview of unsupervised learning
 - Clustering
 - Decomposition using Sparse Dictionary Learning

Goal

Discover patterns/structure in *X*,

Unsupervised learning

- Unsupervised = no expert, no labels,
- Two main approaches:
 - Clustering = find a partition of X in K subsets.
 - Decomposition using K vectors.
- Applications:
 - Quantization,
 - Visualization...





Factorization in Deep Neural Networks

Overview of unsupervised learning

Unsupervised learning



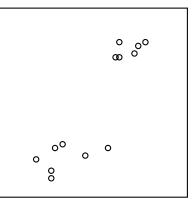
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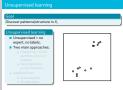




Factorization in Deep Neural Networks

Overview of unsupervised learning

Unsupervised learning



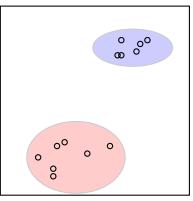
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Factorization in Deep Neural Networks Overview of unsupervised learning

-Unsupervised learning

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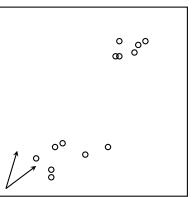
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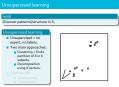
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Factorization in Deep Neural Networks Overview of unsupervised learning

-Unsupervised learning



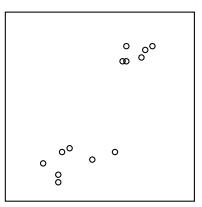
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Factorization in Deep Neural Networks Overview of unsupervised learning

-Unsupervised learning

expert, no labels, Two main approaches partition of X in K Decomposition using K vectors. Applications : Quantization Visualization



02-

Example: clustering using L_2 norm

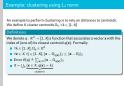
An example to perform clustering is to rely on distances to centroids. We define K cluster centroids Ω_k , $\forall k \in [1..K]$

Definitions

We denote $q: \mathbb{R}^d \to [1..K]$ a function that associates a vector **x** with the index of (one of) its closest centroid $q(\mathbf{x})$. Formally:

- $\forall k \in [1..K], \Omega_k \in \mathbb{R}^d$
- $\forall \mathbf{x} \in X, \forall j \in [1..K], \|\mathbf{x} \Omega_{q(\mathbf{x})}\|_2 \leq \|\mathbf{x} \Omega_j\|_2$
- Error $E(q) \triangleq \sum_{\mathbf{x} \in X} \|\mathbf{x} \Omega_{q(\mathbf{x})}\|_2$
- $X = \bigcup_{k} \{ \mathbf{x} \in X, q(\mathbf{x}) = k \}$

cluster k

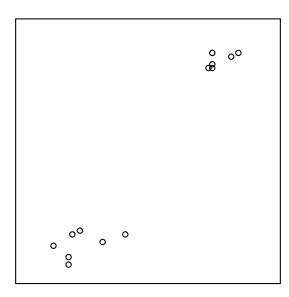


Here, we provide a formal definition of clustering using centroids. Note that there are other ways to define clustering, using regions, using density of spaces, using probabilities, etc...

The second point is the way to define the closest centroid.

The important point to note here is the definition of the error, which can be defined as the sum of all distances between points and their closest cluster centroid.

Example: clustering using L_2 norm



Factorization in Deep Neural Networks

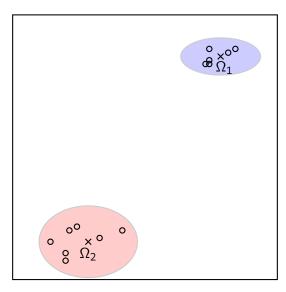
Overview of unsupervised learning

Clustering

Example: clustering using L_2 norm



Example: clustering using L_2 norm



Factorization in Deep Neural Networks

Overview of unsupervised learning

Clustering

Example: clustering using L_2 norm



Clustering using L_2 norm

Quantizing MNIST

- Replace **x** by $\Omega_{k(\mathbf{x})}$
- Compression factor $\kappa = 1 K/N$



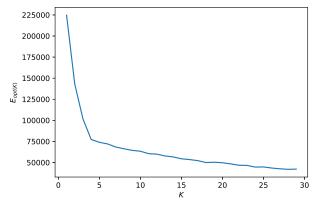
Factorization in Deep Neural Networks Overview of unsupervised learning -Clustering 2024--Clustering using L_2 norm

02-

Clustering using L_2 norm

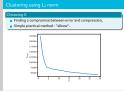
Choosing K

- Finding a compromise between error and compression,
- Simple practical method : "elbow".





Factorization in Deep Neural Networks -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47 -0.47

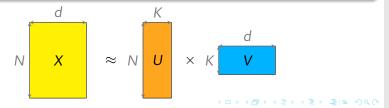


Sparse Dictionary Learning

Definitions

Dictionary learning solves the following matrix factorization problem:

- The set X is considered as a matrix $X \in \mathcal{M}_{N \times d}(\mathbb{R})$,
- We consider decompositions using a dictionary $V \in \mathcal{M}_{K \times d}(\mathbb{R})$ and a code $U \in \mathcal{M}_{N \times k}(\mathbb{R})$, with the lines of V being with norm 1,
- Error $E(U, V) \triangleq ||X UV||_2 + \alpha ||U||_1$
- Training: find U^* , V^* that minimizes $E(U^*, V^*)$
- α is a sparsity control parameter that enforces codes with soft (ℓ_1) sparsity



Factorization in Deep Neural Networks

Overview of unsupervised learning

Decomposition using Sparse Dictionary Learning -Sparse Dictionary Learning

- We consider decompositions using a dictionary $V \in \mathcal{M}_{\nu-1}(\mathbb{R})$ and a code U ∈ M_{N+1}(R), with the lines of V being with norm 1



