

# Project Study: Tracking Drone Orientation with Multiple GPS Receivers

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## I. INTRODUCTION

WITHOUT a good sense of orientation and balance, a drone will not be able to properly adjust its rotors to fly, even hovering becomes impossible. Thus, many inertial measurement units (IMUs) were installed in an attempt to fix this issue. An IMU is an electronic device that measures and reports a body's specific force and angular rate as well as the magnetic field surrounding the body, using a combination of accelerometers and gyroscopes and sometimes magnetometers too.

IMUs are typically used to maneuver aircraft, including unmanned aerial vehicles (UAVs), among many others, and spacecraft, including satellites and landers.

Recent developments allow for the production of IMU-enabled GPS devices[1], in which the IMU allows the GPS receiver to work when GPS-signals are unavailable, such as in tunnels and inside buildings as well as when electronic interference is present. Unfortunately, the redundancy of IMU installations creates issues that result in unreliable hardware. Various noise sources, including motor vibrations, electromagnetic interferences, and ambient ferromagnetic influences, provided unreliable recordings for the IMU. Worse, the errors would accumulate over time, causing the IMUs to be prone to various types of correlated failures. This paper introduces the development SafetyNet, which is a fail-safe mechanism for IMU failures. The basic idea is to use multiple GPS units to track the 3D orientation of the UAV. The SafetyNet design includes four GPS receivers at four arms of a single drone upon IMU failure. This design utilizes these GPS receivers to estimate the drone's 3D orientation.

As an alternative to the IMUs, SafetyNet uses GPS signals to estimate the real time orientation of the drone without any inertial or magnetometer assistance. Challenge states that the traditional GPS system has an error of around 2 to 3 meters, and the more advanced Differential GPS technology would still have a relative error in the scale of 10 to 20 centimeters (which equals to 20 degrees in orientation). However, relative GPS signal information can still provide data for analysis, and this study utilizes the spatio-temporal information to achieve better accuracy.

The core aspects of the SafetyNet design can be distilled as follows::

- Manipulate measurements across pairs of GPS receivers, satellites, and consecutive time points and capture the 3D orientation from two different perspectives, which can institute the transition model and the measurement model of filters.
- GPS carrier-phase measurements can be used to achieve very precise positioning solutions. Carrier-phase measurements are much more precise than pseudo-range measurements, but they are ambiguous by an integer number of cycles. The integer number of cycles is an unknown portion of GPS phase measurements, called "integer ambiguity".

In attempting to resolve this ambiguity, past studies have adopted techniques akin to hard decoding, where the most likely state estimate is propagated across time. This study's design is the equivalent of soft decoding, whereby top-K possibilities of the ambiguity are propagated, each associated with an inferred probability.

A particle filter is used to execute this idea with the particle filter degenerating back into the Kalman Filter when the ambiguity is resolved confidently.

- This study breaks away from the classical particle filter approach and adjusts the state of the particles based on available measurements. This speeds up the convergence of the system while requiring fewer particles (considerably reducing the computational complexity). As a result, the overall SafetyNet system lends itself to real time operation on today's drone hardware.[2]

## II. PROBLEM FORMULATION

### A. Drone Model

In this study, the drone is modeled with four GPS receivers installed on its four arms with a distance of ten centimeters to the center. Therefore, a baseline matrix is generated, as shown in figure 1 to model the ground truth relation between different receivers at different states.

The baseline matrix has the formula::

$$B = \begin{bmatrix} \rho_{41} & \rho_{42} & \rho_{43} \end{bmatrix} \quad (1)$$

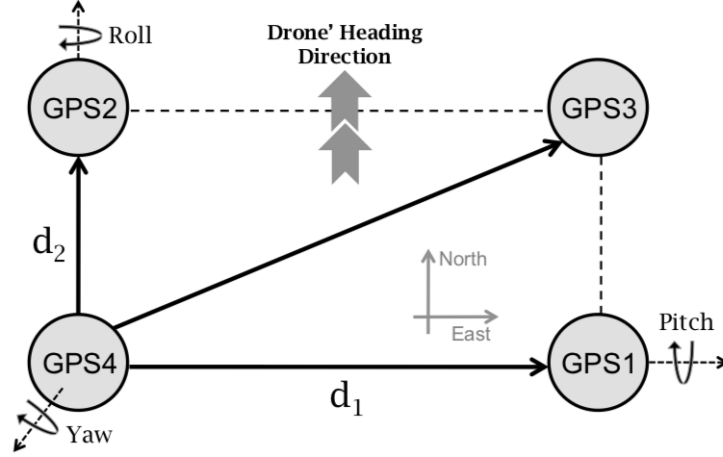


Fig. 1: Baseline Matrix

where  $\rho_{ij}$  is the vector between receiver  $i$  and  $j$

$$\rho_{ij} = \rho_i - \rho_j \quad (2)$$

### B. Pseudorange

Generally, the GPS operates in measuring the the time difference between the transmitters and receiving their pseudo-ranges, which are the estimated distances between both ends as shown in equation 3.

$$Pseudorange = ToF * c \quad (3)$$

where  $ToF$  is the time difference and  $c$  represents the speed of light.

However, when a satellite transmits a signal, it includes clock error as the starting time of transmission which is obtained from its atomic clock. The reception time of the ground receiver is also recorded by a less accurate local clock, as the clock of a typical GPS receiver is not synchronized to the GPS satellites. The resulting error can be up to 300 km as a GPS signal can get delayed when it enters the Earth's atmosphere because of refractions in the Ionosphere and the troposphere. When the signal passes through a multi-path channel, more errors would be introduced. In this study, the error was modeled in pseudo-range at receiver  $i$  from the satellite  $s$  as shown in equation 4.

$$Pseudorange_i^s = \rho_i^s + ct_i - ct^s + A^s + M_i + \epsilon_i^s \quad (4)$$

Here,  $\rho_i^s$  represents the real range,  $t_i$  and  $t^s$  stand for the clock error at the receiver and transmitter sides correspondingly.  $A$  models the interference by the atmosphere,  $M_i$  stands for the multipath interference and  $\epsilon_i^s$  represents the hardware noise in measuring.

The operation error from the system would be as large as one to four meters which is far from satisfactory measures. Thus, the Differential GPS technology is introduced to leverage the difference in the signal phase and therefore highly improving the system's accuracy.

### C. Differential GPS

The differential GPS technology leverages the phase of received GPS signals to improve the accuracy. One advantage of carrier phase is that its changes over time can be tracked reliably by utilizing the doppler shift in the signals.

The phase model is shown in equation 5 by ignoring the multipath and hardware noise error. Another advantage of carrier phase is that its changes over time can be tracked reliably by utilizing the doppler shift in the signal.

$$\lambda\phi_i^s = \rho_i^s + ct_i - ct^s + A^s - N_i^s \quad (5)$$

While  $N_i^s$  is Integer Ambiguity the number of whole cycles on the path from satellite to receiver.[3] The unknown property of  $N_i^s$  is called integer ambiguity solve from the phase measurement, and estimating the integer ambiguity is one of the major concern in the SafetyNet implementation. More discussion on integer ambiguity would come in later sections.

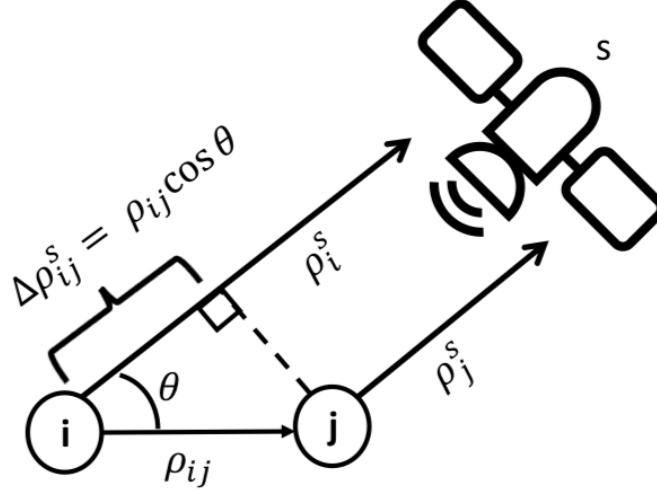


Fig. 2:  $\lambda \Delta \phi_{ij}^s = \rho_{ij} \cdot \hat{l}_s + c \Delta t_{ij} - \lambda N_{ij}$

Environmental error sources in Equation 3 are correlated over short time periods and within small geographical areas (200 km). Thus, two GPS measurements across time can be subtracted (or differenced) to eliminate some of these factors. Similarly, simultaneous measurements from multiple GPS receivers can also be differenced. [4] This study propose 4 kind of differentials.

1) *Single Differential across Receivers ( $SD_{ij}^s(t)$ )*: Consider the carrier phase equations for two GPS receivers i and j from the same satellite s (let us ignore multipath and noise).

$$\begin{aligned} \lambda \Delta \phi_{ij}^s &= \phi_i^s - \phi_j^s \\ &= \Delta \rho_{ij}^s + c \Delta t_{ij} - \lambda N_{ij} \end{aligned} \quad (6)$$

By differencing the phases at different receivers, correlated error sources of atmospheric delays and satellite clock biases disappear.

For further simplification,  $\Delta \rho_{ij}^s$  is replaced by  $\rho_{ij} \cdot \hat{l}_s$ , where  $\rho_{ij}$  is the vector between two receivers and  $\hat{l}_s$  is the line-of-sight unit vector from the receiver to the satellite. The transformation relationship is shown in figure 2.

The equation then become:

$$\lambda \Delta \phi_{ij}^s = \rho_{ij} \cdot \hat{l}_s + c \Delta t_{ij} - \lambda N_{ij} \quad (7)$$

While by single differential equation, some errors have disappeared, there still exists a function of the clock bias errors,  $c \Delta t_{ij}$  still remains, this call the need for double differentials.

2) *Double Differential across Receivers and Satellites ( $DD_{ij}^{sk}(t)$ )*:

$$\begin{aligned} \lambda \nabla \Delta \phi_{ij}^{sk} &= \lambda \Delta \phi_{ij}^s - \lambda \Delta \phi_{ij}^k \\ &= \rho_{ij} \cdot (\hat{l}_s - \hat{l}_k) - \lambda \nabla \Delta N_{ij}^{sk} \end{aligned} \quad (8)$$

In this equation, i and j represents two different receivers, and k represents one satellite. Subtracting the single differential, we get double differential, the the clock biases is removed and the absolute orientation is achieved, but the residue is polluted by integer ambiguity.

In this study, the spatio double differential forms our measurement model in the filtering process. This paper assume the ambiguities are magically fixed, this provides us a reasonably precise estimate of relative positions between receiver pairs. The technology of Real Time Kinematics (RTK) technology can use the accurately known location of the reference receiver to calculate the location of the other.

3) *Single Differential across Time ( $SD_i^s(t_{12})$ )*: This paper also perform differentials across time for the same receiver. When there is no cycle slips, the equation can be listed as below,

$$\lambda \Delta \phi_i^s(t_{12}) = \rho_i(t_{12}) \cdot \hat{l}_s + c t_i(t_{12}) \quad (9)$$

Measurements across 4 satellites can help jointly estimate the relative displacement and clock bias. This estimated relative displacement is quite accurate since the integer ambiguity  $N_i^s$  does not included in it. This paper used a static receiver placed on the ground to verify the accrancy, and find that the estimation resulted in about 1cm/s of motion.

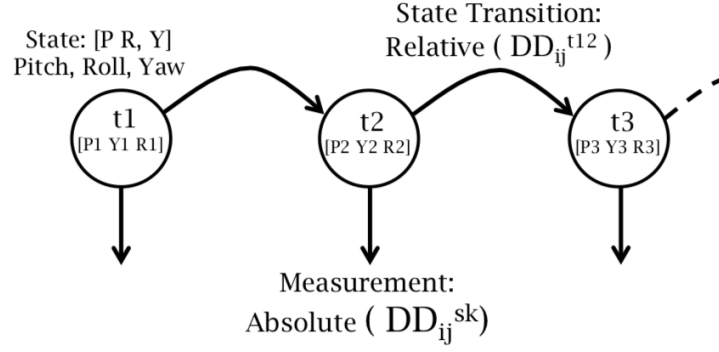


Fig. 3: System Model

4) *Double Differential across Receivers and Time* ( $DD_{ij}^s(t_1t_2)$ ): By taking the difference between the two single differentials across time, this paper achieved a measurement of the change in orientation, totally unpolluted by integer ambiguity. This measurement forms the system transition model in the filtering process. Under the no cycle slips assumption, the interger ambiguity can be eliminated by subtracting two equation of single differential across time.

$$\begin{aligned} \lambda \nabla \Delta \phi_{ij}^s(t_{12}) &= \lambda \Delta \phi_i^s(t_{12}) - \lambda \Delta \phi_j^s(t_{12}) \\ &= (\rho_{ij}(t_1) - \rho_{ij}(t_2)) \cdot \hat{l}_s + c \Delta t_{ij}(t_{12}) \end{aligned} \quad (10)$$

### III. SYSTEM MODEL

SafetyNet treat model orientation tracking as a state estimation problem, where the state is defined as 3D orientation and represent by quaternion. With both the temporal and spatial differentials, we are able to model the orientation estimation problem by forming the transition state and absolute measurements. The system diagram is provided in figure 3.

1) *Transition State*: The temporal differential provides an accurate estimation upon the transition state as the integer ambiguity is cancelled. By minimizing the relative clock error, we can solve the equation to track the orientation change  $\delta q$  between states. Here we introduced the 3-dimensional vector representation of orientation  $\delta \theta$  whose magnitude is the angle it rotates and direction is the axis it rotates around. By changing the representation metric, we are able to get rid of the constraint from quaternion and the estimation becomes a simple Least Square problem:

$$\lambda \nabla \Delta \phi_{ij}^s(t_{12}) = \rho_{ij}(q_0) [A(q_1) \hat{l}_s]_{\times} \delta \theta + c \Delta t_{ij}(t_{12}) \quad (11)$$

where  $A(q)$  is the rotation matrix corresponding to the quaternion.

The solved  $\delta \theta$  cannot be directly applied for transition state as the computation of rotation vector is not immuneable in large scale. We convert it back to quaternion form and the transition state becomes:

$$q_{k+1} = \delta q \otimes q_k \quad (12)$$

2) *Absolute State*: The spatial differential is transformed as our absolute measurement at each state.

$$\lambda \nabla \Delta \phi_{ij}^{sk} = \rho_{ij} \cdot (\hat{l}_s - \hat{l}_k) + \lambda \nabla \Delta N_{ij} \quad (13)$$

We can transform the measurement to a function of last state quaternion and a change in orientation in the vector form.

$$\lambda \nabla \Delta \phi_{ij}^{sk} - \rho_{ij}(q_0) A(q_n) \cdot (\hat{l}_s - \hat{l}_k) = \rho_{ij}(q_0) [A(q_n) \cdot (\hat{l}_s - \hat{l}_k)]_{\times} \delta \theta + \lambda \nabla \Delta N_{ij} \quad (14)$$

The measurement form would be further transformed in Extended Kalman Filter section for system linearization.

### IV. ALGORITHMS

#### A. Extended Kalman Filter

Referring back to equation 12, the transition function is intrinsically a nonlinear operation (the quaternion multiplication), we make linearized approximations using Extended Kalman Filter (EKF). Now, linearizing transition model around the estimated rotation vector associated with quaternion  $q_k$  by applying Taylor Expansion, we have:

$$\delta \theta_{k+1} = F \delta \theta_k + \omega_k \quad (15)$$

where  $\omega_k$  is the system noise.

With the linearization process, the absolute state is transformed from absolute rotation in form of quaternion to change in rotation vector ( $\delta\theta$ ), as the rotation vector has the property of having muteable operation in small scales and removes the constraint in magnitude.

As with the transition function above, the measurement function can be written in the following form:

$$y_{k+1} - y_0 = H\delta\theta_{k+1} + v_{k+1} \quad (16)$$

where:

$$y = \lambda \nabla \Delta\phi_{ij}^{sk} - \lambda \nabla \Delta N_{ij} \quad (17)$$

$$y_0 = \rho_{ij}(q_0)A(q_n) \cdot (\hat{l}_s - \hat{l}_k) \quad (18)$$

$$H = \rho_{ij}(q_0)[A(q_n) \cdot (\hat{l}_s - \hat{l}_k)]_{\times} \quad (19)$$

and  $v_{k+1}$  is the measurement noise.

The above EKF has been designed under the convenient assumption that integer ambiguity and cycle slips have been resolved. However, this resolution is challenging, as evident from the numerous papers written on this topic.[5-7] The transition model and measurment model can now be combined using an Extended Kalman Filter for a refined estimate of  $\theta^{k+1}$ .

In the measurement model, the integer ambiguity still exists. Here we make the assumption that the integer ambiguity is already solved such that we can ignore it for the filtering process and come back to it afterwards.

Once the drone is flying, additional multiples of wavelengths can also accumulate, called cycle slips. This paper first describe ways to mitigate the initial N and discuss cycle slips thereafter.

Therefore, this paper did not measure integer ambiguity directly, but make it as an index to identify the estimation they got is correct or not. Their core intuition is to compute a Cos function on the value of  $2\pi N_{ij}^{sk}$ , since  $N_{sk}$  should be an integer,  $Cos(2\pi N_{sk}^{ij})$  should equal to 1.

The process of Kalman filtering is listed as below:

- Using transition model to get estimation of the next time point:  $\delta\theta_{k+1}$ .
- Using measurement model to get the estimation of integer ambiguity. In an ideal case, the correct q should make the corresponding values of  $N_{ij}^{sk}$  equal to 1.
- Identify the correctness of integer ambiguity using the summation of cosmetrics:

$$M(q) = \sum_{ij,sk} \cos(2\pi N_{sk}^{ij}) \quad (20)$$

and compare  $M(q)$  to the number of possible combination pairs of receivers  $i, j$  and satellites  $s, k$ . If  $M(q)$  approximates the number we consider it as correct and incorrect otherwise.

- If the integer ambiguity is correct, we can continue using kalman filter to estimate the state.
- If the integer ambiguity is not correct, the problem is transformed into a maximization problem. The cosmetic value would always be less than 1 if the estimated integer ambiguity is not an integer so our intention goes to find the best q to maximize  $M(q)$ , i.e.:

$$q_{coarse} = \underset{q}{\operatorname{argmax}} M(q) \quad (21)$$

- We simply perform a naive grid search in all 3 dimensions of ruler angle (yaw, pitch and roll) with a 5 degree step to find the optimized solution  $q_{coarse}$  to maximize the cosmetic value.
- After maximization, we update the previous q with  $q_{coarse}$ , and go back to step 2.

The system diagram is shown in figure 4.

### B. Advanced Particle Filter

there exists one phenomenon called cycle slips, A cycle slips causes a jump in carrier-phase measurements when the receiver phase tracking loops experience a temporary loss of lock due to signal blockage or some other disturbing factor. It usually happens with highly aggressive flight drone. The process is listed as follows:

- Using kalman filtering, we can calculate the cosmetic of each  $q_i$
- if the cosmetic is lower than one, which means the confidence is verified as low, we switch from kalman filter to particle filter to solve the integer ambiguity problem. We select K values of orientation q the values whose corresponding Cos metric ranks in the top-K. We initialize K particles( from grid search with the top k confidence in cosmetic form) at each of these orientation states and update them via the transition model and measurement model.

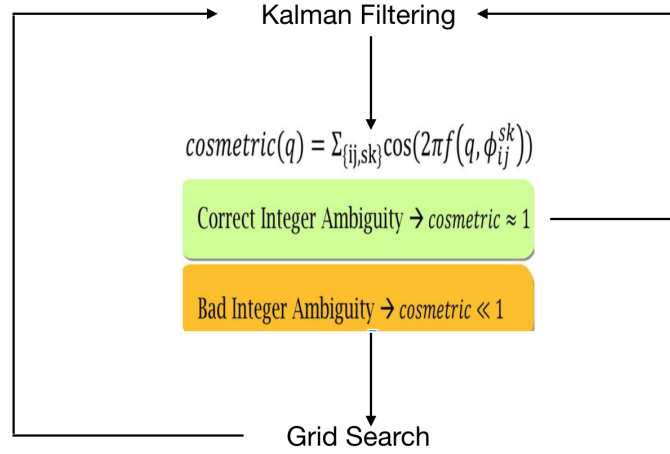


Fig. 4: Kalman Filter

- All things goes well, however, there is one problem of the slow convergence of particle filter. To solve this, this paper develop one advanced particle filter. In simple particle filter, we propagate to the next stage by transition model, and we weight them by the measurement model, and assign probability for later use for filtering and so on. This paper make a simple modification, they move the particle to a state that maximizes the likelihood, and then perform the resampling step. Thus, the net outcome is faster convergence for the correct ambiguities, while disappearing particles for incorrect ambiguities.
- Upon its convergence, and if the cosmetric close to 1, we switch back to Kalman filter again. If the cosmetric is much lower than 1, more particles are added and resampled. Resampling is performed such that the resulting particles are an equal mix of the (highest weighted) current and new particles, and continuing the particle filtering process until the cosmetric close to one, and we go back to step one.

The system diagram is shown in figure 5.

## V. SIMULATION

### A. Drone Simulation Platform

The simulation of the base drone is done based on Hector Quatercopter, an open-source implementation based on Robot Operation System (ROS) and Gazebo. The platform is shown in figure 6.

The ground truth data of the location and the orientation data is collected to simulate the multiple GPS receivers attached to the drone.

4 GPS receivers are simulated on the 4 arms of the drone, rotated according to the ground truth orientation and shifted to the real location.

Two satellites are fixed on the Medium Earth Orbit and the phases are simulated from the corresponding distance between the satellite and the receiver.

As the drones movement is relatively ignorable comparing to the distance to the satellites, the line-of-sight vector is considered as constant.

The Kalman and Advanced Particle filters are performed on the simulated data.[9]

## VI. REAL WORLD APPLICATIONS

With the booming increase in the applications of unmanned autonomous vehicles, reliable orientation estimation has become an important and necessary concern. SafetyNet proposes the novel algorithm to track the orientation with multiple GPS receivers to promise an error of two degrees in the environment where magnetic interferences and acceleration errors accumulate.

The reliability and the accuracy of SafetyNet makes it suitable in two major areas of applications.

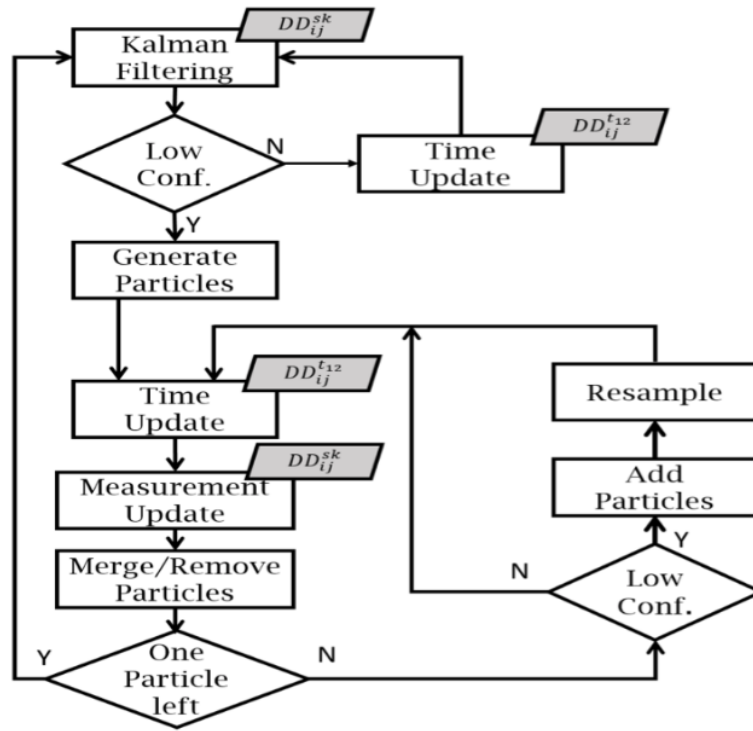


Fig. 5: Advanced Particle Filter

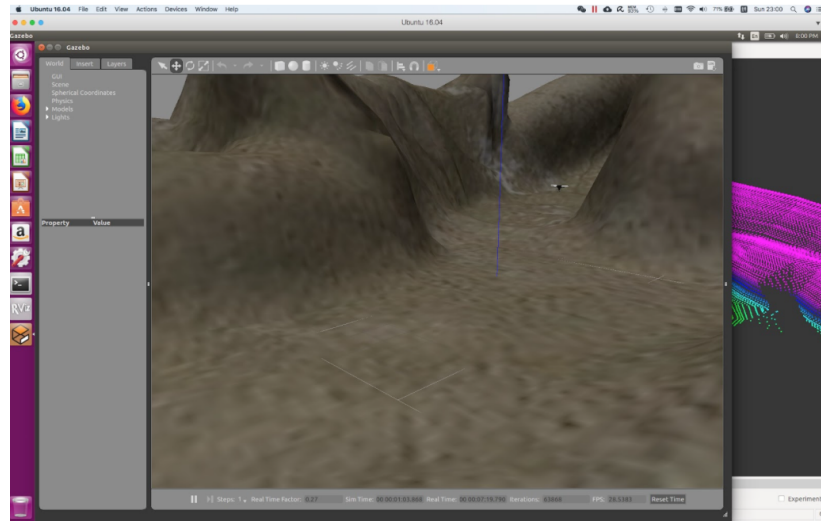


Fig. 6: Hector Quatercopter Simulation Platform

*a) Reliability:* The estimation in this study makes reliability suitable for large quatercopters in aggressive flying statuses and in highly interfered magnetic fields. Typical applications include flying in urban areas (interference in magnetic fields), obstacle avoidance in high speed flights (errors in accelerometers), etc.

*b) Accuracy:* The orientation estimation in this study powers up the accuracy in autonomous control algorithms. Thus, SafetyNet can increase the accuracy of the application of UAV. For example, accurate tracking of the camera pose makes it possible to achieve better vision-based antonomos flying. 3D reconstruction from the drones lens is another application that benefits from the accuracy.

## VII. CONCLUSION

SafeNet uses differential techniques, culminating in a novel particle filter framework running over multi-GNSS systems (GPS, GLONASS, and SBAS) to accurately compute the relative locations between each receiver pair and then to translate

these measurements into the drone's 3D orientation. Results from eleven sessions of five to seven minute flights report median orientation accuracies of 2 even under overcast weather conditions. The two filtering algorithm used in the paper are Kalman filter and particle filter, we compared the performance of Kalman Filters and Advanced Particle Filter. The performance of Kalman Filters and Advanced Particle Filters is similar with less aggressive flight, when comes in to highly aggressive flight, Advanced Particle Filters can better track the drone than Kalman Filter. And after the highly aggressive flight, Kalman Filter has large deviation, while Advanced Particle Filters still performs well. The reason can be listed as below:

- SafetyNet adopts a hybrid approach to satisfy the linearity and Gaussian assumptions required for Kalman Filter.
- Missing data in one or more of the receivers derails the state transition function.
- When the confidence is low, Kalman filter used "grid search" to find the best  $q_i$ , this method does not make use of the information from the previous time point and the following time point, and assume there is only one time point in the cycle slips period. In comparison, Advanced Particle Filters combines the information from the previous time point and the following time point, and do not forcefully assign there is only one time point in cycle slips period.

In conclusion, Advanced Particle Filters has better performance than Kalman Filters.

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