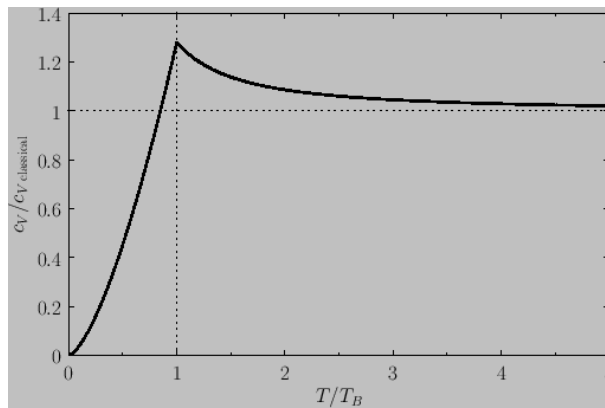


Coexistence region ($\mu=0$), $T < T_0$

$$U = \frac{3}{2} \frac{\gamma V}{\beta \lambda^3} g_{5/2}(1) \quad \text{internal energy}$$

$$N = \frac{\gamma V}{\lambda^3} g_{3/2}(1)$$

$$C_V = \frac{1}{N} \left(\frac{\partial U}{\partial T} \right)_{V,N} = \frac{15}{4} \frac{\gamma V k_B}{\lambda^3 N} g_{5/2}(1) \\ = c \left(\frac{V}{N} \right) T^{3/2}$$



if $\mu \rightarrow 0$ and $V \rightarrow \infty$

$$\frac{1}{V} \frac{Z}{1-Z} \rightarrow \frac{1}{V} \frac{1}{1-Z} \rightarrow \frac{N_0}{V}$$

$$\frac{1}{V} \ln(1-Z) \rightarrow 0$$

then,

$$P = \frac{1}{\beta V} \ln(\Xi(\beta, V, Z)) \rightarrow \gamma V \int_0^\infty \epsilon^{1/2} \ln(1 + \exp(-\beta \epsilon)) d\epsilon \\ = \frac{\gamma}{\beta \lambda^3} g_{5/2}(1)$$

$p \rightarrow 0$ if $T \rightarrow 0$ Different from Fermi!

$$S = - \left(\frac{\partial \Phi}{\partial T} \right)_{V, \mu} = V \left(\frac{\partial P}{\partial T} \right)_{\mu}$$

$$S(T, V, \mu=0) = V \left(\frac{\partial P}{\partial T} \right)_{\mu=0} = \frac{5 k_B \gamma V}{2 \lambda^3} g_{5/2}(1).$$