Project 1 Documentation

Why did you choose the implementation you did?

I decided to store the matrix in a linked list that held the value, row, and column of each element. I only added nonzero elements. I then checked whether the matrix was a square, using counters altered when reading in the data, and threw an error if a square matrix was not entered. Using a single linked list seemed like the best option because I didn't want to keep track of multiple lists and using other data structures didn't make sense.

In determining the matrix, I wanted to get down the matrix to a 2x2 base case because its simple do solve arithmetically. So, anything bigger than a 2x2 matrix will recursively call the determinant function until 2x2 matrices are called.

What did you learn from doing this assignment?

I learned about the benefits of a sparse matrix memory wise. It wasn't as difficult to implement as I thought it would be, and I learned about dealing with nonexistent values using a variety of counters and other tricks.

What is the computational complexity of the operations in your matrix implementation?

Reading in the data is dependent on the number of elements in the matrix so its complexity is O(n). Checking whether or not the matrix is a square is O(1) because it's a simple if statement that checks some math with counters created while reading in the elements. Determining the determinant for a null matrix or 1x1 matrix has a complexity of O(1) because it either returns a zero or the only value in the array.

The complexity of finding the determinant of a 2x2 matrix takes O(n) and O(1) per each nonzero value in the first row in the matrix. O(n) because I employed a search function that looks through the entire list to find a specific value. In total is should take O(4n + 4) which simplifies down to O(n) for a 2x2 matrix. For anything bigger each row would recursively find get the minor until I find a 2x2 submatrix. So, for any square matrix it would take $O(n^{(s-1)})$ where s is the size of the total rows of the matrix.

What was the hardest part of this assignment?

The hardest part initially was getting my head around the sparse matrix idea conceptually. It took me a while to figure out how to do the determinant calculations without storing zero values, but I realized that using some counters and other programming tricks made it easy. After that, making the minor was a bit of work; making the new smaller matrix was easy but it took me a while to make sure I changed the row and column values of each node correctly.