# The Hack VM I: Structure, arithmetic and logic COMSM1302 Overview of Computer Architecture

John Lapinskas, University of Bristol

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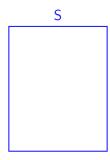
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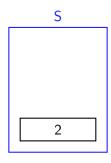
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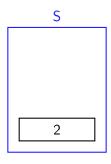
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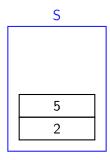
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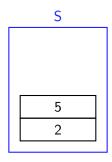
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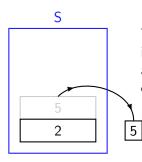
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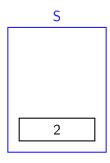
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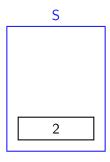
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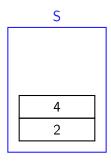
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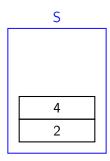
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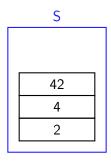
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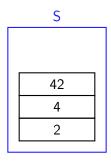
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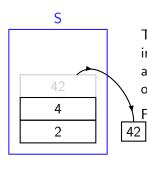
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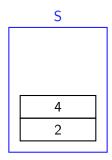
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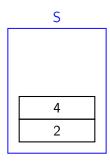
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Stacks are LIFO: "Last In, First Out".

(The JVM is also a stack machine, so there are good reasons to do this! We'll see these later.)

#### Virtual memory

In assembly, we use **physical memory** — every memory address is the exact logical signal sent to a physical latch on a physical chip, either ROM or RAM.

An intermediate representation should be portable, so instead we work with virtual memory. This acts like physical memory, storing one word at each address, but we don't worry about where each address is stored physically.

The (ISA-dependent) VM translator will then map virtual memory addresses to physical memory addresses during compilation.<sup>1</sup>

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In modern computers, virtual memory has a second, more important, role. Each process' assembly code assumes it's the only process running and has full access to any memory address. This is actually virtual memory. The operating system then uses dedicated machine code instructions to maintain a page table mapping each process' virtual memory space back to physical memory. This virtual memory may not even map to RAM — rarely-accessed data will be swapped to a page file.

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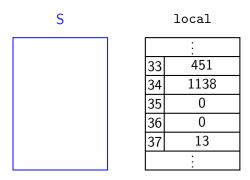
The Hack VM has 8(!) separate virtual memory banks, which our VM translator will map to different **segments** (continuous blocks) of the underlying RAM.

For now, we only care about two:

- local is general-purpose storage for local variables.
- **constant** holds the constant *i* at each 15-bit address *i*. This "memory" is read-only and doesn't correspond to any physical ROM or RAM.

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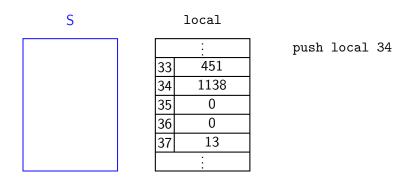
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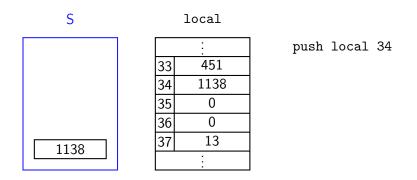
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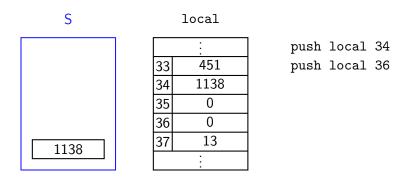
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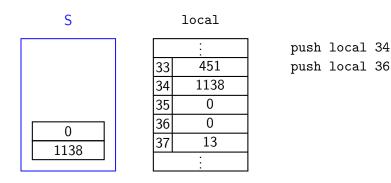
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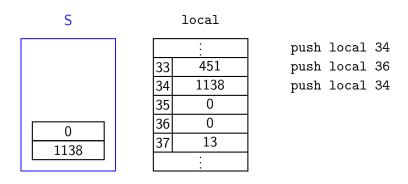
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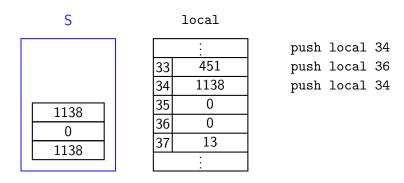
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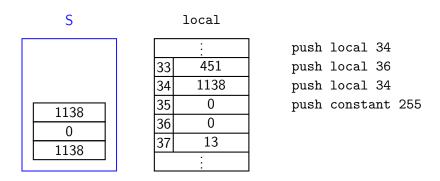
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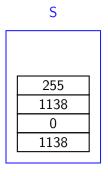
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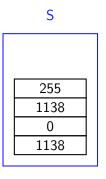


	10001
	:
33 34	451
	1138
35	0
36	0
37	13
	:

local

push local 34
push local 36
push local 34
push constant 255

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IUCal			
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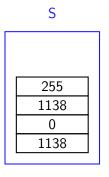
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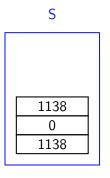
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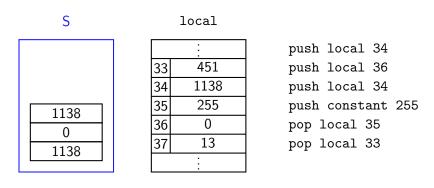
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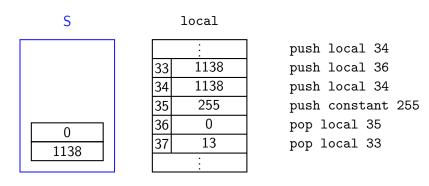
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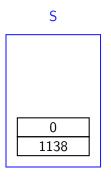
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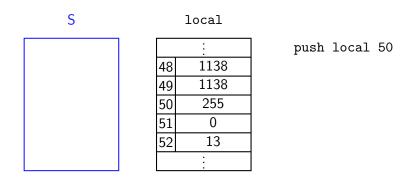
Note that pushing and popping are our *only* form of memory management. For example, to copy the value of local 4 into local 250, we would write:

push local 4
pop local 250

S	local	
		:
	48	1138
	49	1138
	50	255
	51	. 0
	52	13
		:

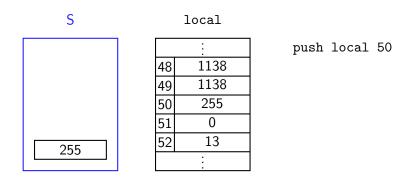
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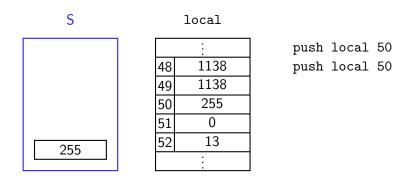
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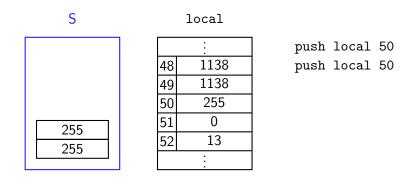
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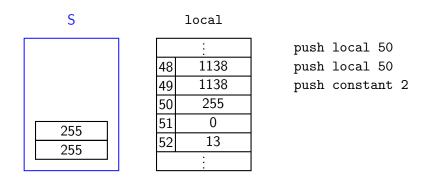
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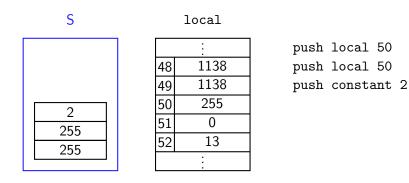
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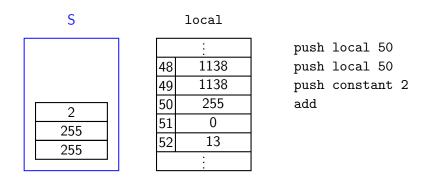
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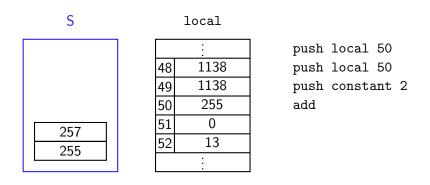
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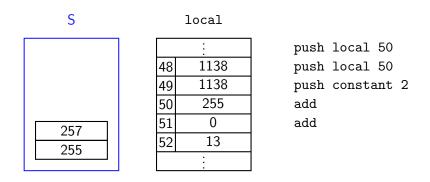
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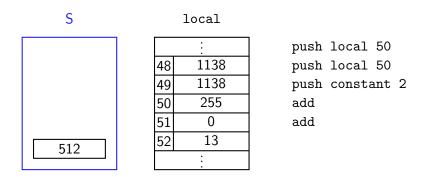
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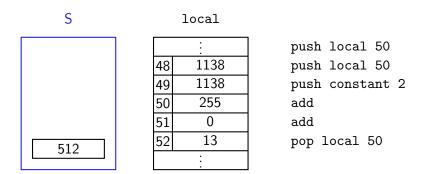
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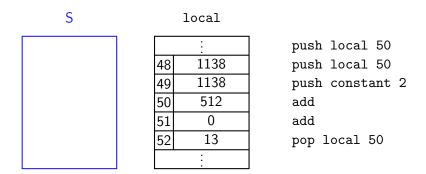
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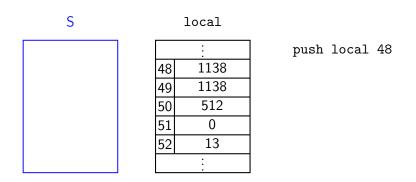


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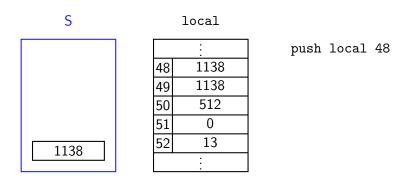
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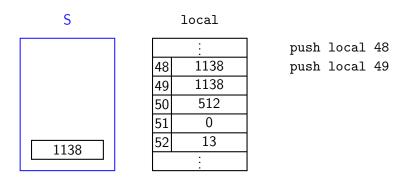
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The Hack VM represents a result of true by 0xFFFF, and false as 0x0000. (We'll talk more about how the Hack VM uses the results of comparisons later.)

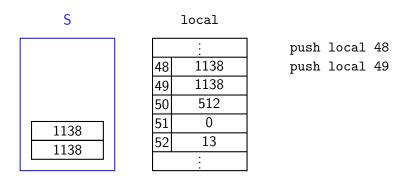


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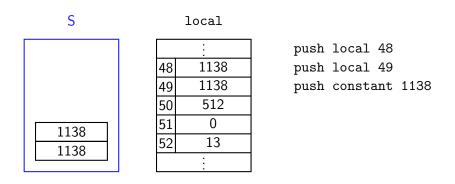
The Hack VM represents a result of true by 0xFFFF, and false as 0x0000. (We'll talk more about how the Hack VM uses the results of comparisons later.)



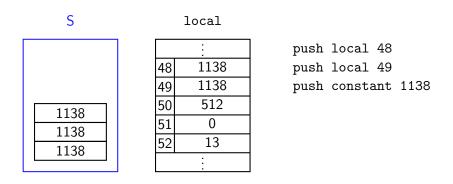
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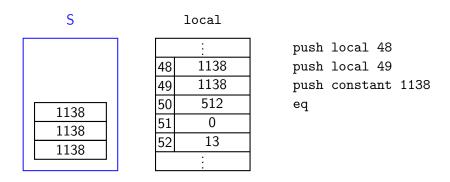
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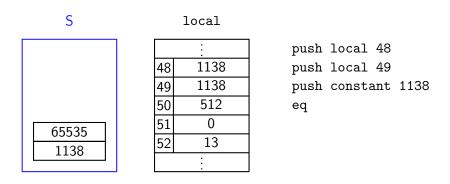
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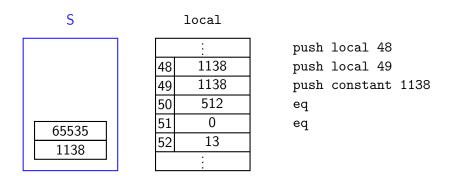
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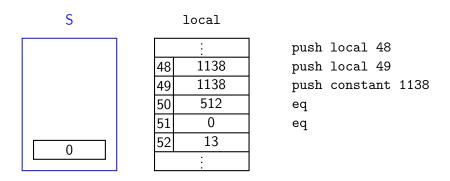
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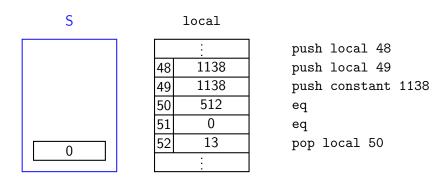
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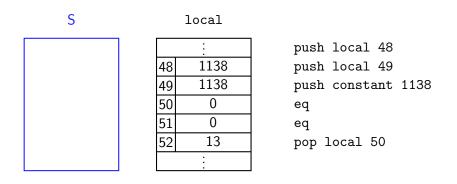
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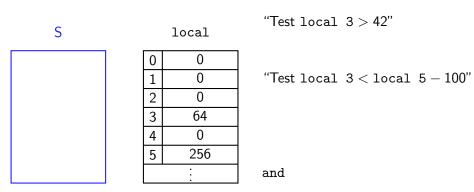
Logical comparisons work the same way. For example, the eq command pops the top two values of the stack, checks whether they're equal, then pushes the result back onto the stack.

Command	Pops	Computes	Comment	
add	2 values	x + y	Integer addition	
sub	2 values	x-y	Integer subtraction	
neg	1 value	-y	Arithmetic negation	
and	2 values	x&y	Bitwise AND	
or	2 values	$x \mid y$	Bitwise OR	
not	1 value	!y	Bitwise NOT	
eq	2 values	x == y	Test equality	
gt	2 values	x > y	Test greater than	
1t	2 values	x < y	Test less than	

- For operations that pop two values, y is the first value popped and x is the second value. E.g. push constant 3, push constant 1, sub will end with 2 on top of the stack rather than -2.
- All arithmetic uses twos complement, so e.g. -x = !x + 1.
- All logic writes true as 0xFFFF and false as 0x0000.
   (This means bitwise operations double as logical operations!)
- You will have this table as a reference in the exam.

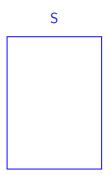
S		local
	0	0
	1	0
	2	0
	3	64
	4	0
	5	256
		:

For example, to test (local 3 > 42) and (local 3 < local <math>5 - 100):



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• Test local 3 > 42 and local 3 < local 5 - 100 separately, then and them. (Remember and, or and not are *both* bitwise *and* logical operations!)



local

0	0
1	0
2	0
3	64
4	0
5	256
	:

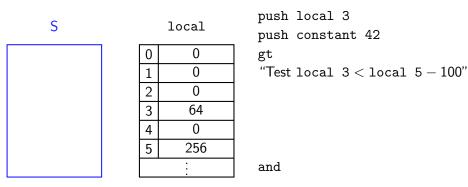
"Test local 3 > 42"

"Test local 3 < local 5 - 100"

and

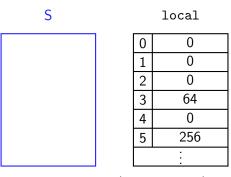
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- ullet To test local 3 > 42, push local 3 and 42, then gt them.



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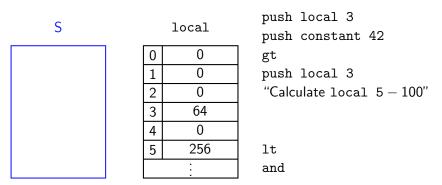
push local 3  $\label{eq:push_constant_42}$  gt  $\label{eq:gt} \mbox{"Test local 3} < \mbox{local 5} - 100 \mbox{"}$ 

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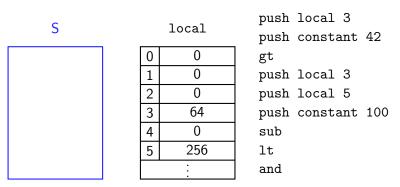
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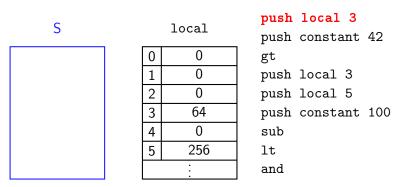
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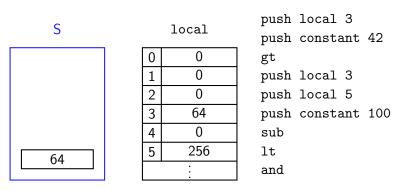
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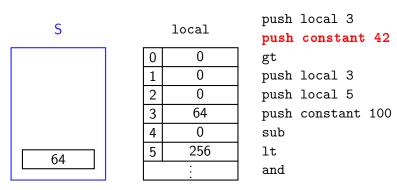
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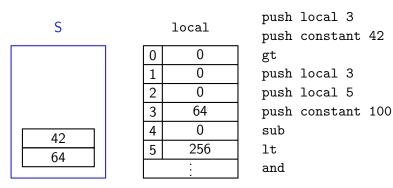
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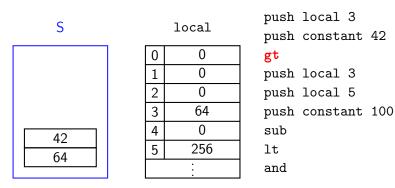
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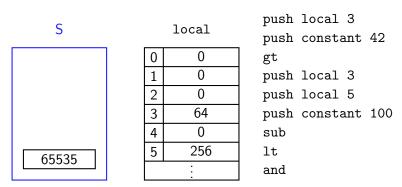
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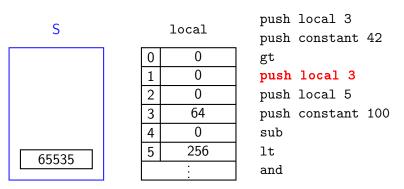
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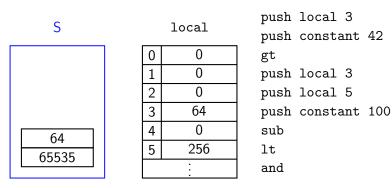
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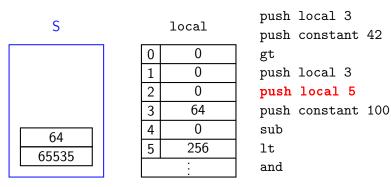
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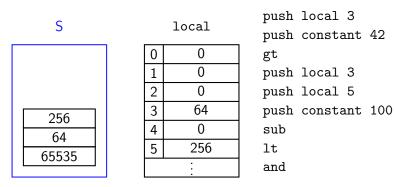
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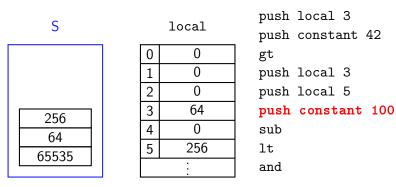
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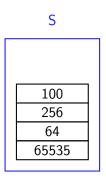
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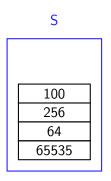


local		
0	0	
1	0	
2	0	
3	64	
4 5	0	
5	256	
	:	

push local 3
push constant 42
gt
push local 3
push local 5
push constant 100
sub
lt
and

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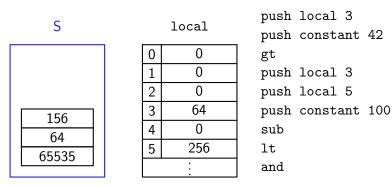


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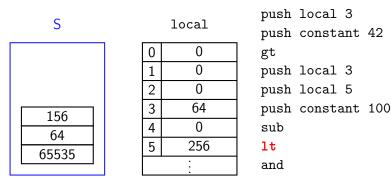
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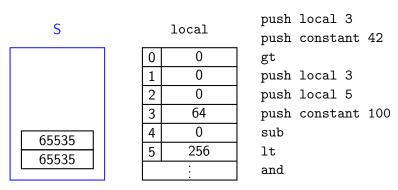
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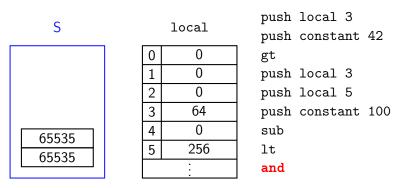
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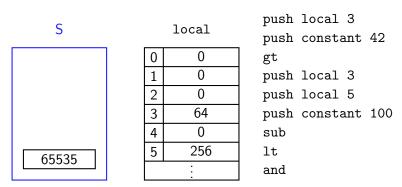
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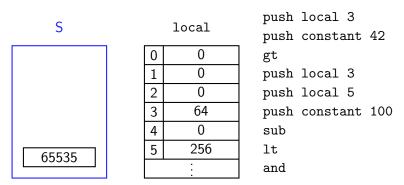
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Later in Programming in C you'll see a general algorithm to parse an arithmetic expression and turn it into "stack order", a.k.a. "Reverse Polish Notation".

For now, it's enough to see how it's possible.

[See video for a demonstration on the VM emulator.]