

MSc in Computer Science and Engineering

**Advanced Algorithms 2016-2017**

**Connectivity in Forests:**

In this project students had to implement an API to maintain the connectivity information of and underlying forest. Maintaining the connectivity of information is a well know problem for computing nearest common ancestor, solving various network flow problems including finding maximum flows, blocking flows, and acyclic flows, computing certain kinds of constrained minimum spanning trees and implementing the network simplex algorithm for minimum-cost flows.

1. **INTRODUCTION:**

The goal of this project is to maintain the connectivity information of an underlying forest. To store this information, we are going to use the Link/Cut tree data structure (with some minor changes that we will explain in section 2). The motivation behind this is that if we represent the forest as a regular collection of parent pointer trees, it might take us a long time to find the root of a given node, however if we represent each tree in the forest as a Link/Cut tree we can do all operations in amortized time where n is the number of nodes in the structure.

The forest in this project consists of a set of vertexes linked by edges, such that no set of edge forms a cycle.

The API developed to resolve this project consists in 3 operations: *link*, *cut* and *connected* which we will explain better in sections 3.

1. **BACKGROUND**:

Explain splay, and access.

1. **DATA STRUCTURE AND API:**
   1. **Link/Cut Tree Structure:**

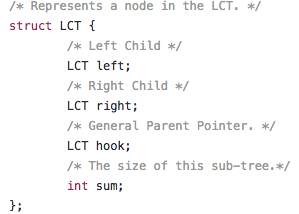


Figure - Link/Cut tree node C structure

The Link/Cut tree underlying structure is shown in figure 1.

The left and right pointers are used to represent the pointers in the auxiliary splay tree. The hook contains the parent of that node. If the parent points back to the node either by a right pointer or a left pointer than it represents a parent otherwise the hook is representing a path pointer and the node pointed by the hook is a path parent. The sum field should represent the depth of the node but in the context of this project it is only used as a bit. If the sum field is -1 than the tree is conceptually reversed, meaning that the order of the nodes in the sub-tree is from right to left instead of left to right.

* 1. **ConnectQ Operation:**
  2. **Link Operation:**

The Link operation is evoked by command where u and v are the number of 2 different nodes. This operation will add an edge linking to . If such edge already exists or would create a cycle this operation has no effect.

To do this operation both and need to be in the top of the

* 1. **Cut Operation:**

Cut explaination

1. **EXPERIMENTAL ANALYSIS:**
2. **DISCUSSION:**

Blab la bla

1. **REFERENCES:**

# Algorithms on Strings, Trees, and Sequences: Dan Gusfield 1997 Cambridge University Press

* Introduction to Algorithms: Thomas H. Cormen, Charles E. Leiserson, Rolnald L.Rivest and Clifford Stain 2009 MIT Press