Layout Optimization Model for Multi-Recipe and Multi-Route Problems with Application to the Design of a Steel Factory

Simulated annealing procedure with MILP model for the layout of the scrap yard, given a left / right split, to explore the space of possible loading sequences for each grade

```
from itertools import permutations, product
import random
import math

from datetime import datetime

import numpy as np
import pandas as pd
import matplotlib.pyplot as plt

from IPython.core.magic import register_cell_magic
@register_cell_magic
def skip(line, cell):
    return
```

- ✓ DATA
- Scrapyard data

Width of the 40m deep box for each scrap type

```
box_width_dict = {0: 11.4, 1: 10.0, 2: 11.7, 3: 10.0, 4: 10.0, 5: 10.0, 6: 23.4, 7: 10.0, 8: 34.4, 9: 12.4, 10: 10.0, 11: 10.0, 12: 38.3, 13: 26.5, 14: 56.9, 15: 43.6, 16: 27.5, 17: 14.3, 18: 69.3, 19: 27.2, 20: 56.1, 21: 38.4, 22: 26.0, 23: 10.0, 24: 33.6, 25: 31.3, 26: 14.4, 27: 30.9, 28: 16.0, 29: 10.0, 30: 14.3, 31: 15.5}
```


Each grade contains a given quantity of certain scrap types

```
grade ingredients dict = \{'601': [6, 8, 4, 5, 0, 1, 2, 7, 9, 16, 20],
 'G02': [6, 8, 4, 5, 0, 1, 3, 7, 16, 20],
 'G03': [6, 8, 4, 0, 3, 7, 9, 16, 20],
 'G04': [6, 8, 18, 4, 5, 7, 9, 11, 17, 30, 16, 19, 20, 27],
 'G05': [8, 5, 0, 1, 7, 17, 16, 20],
 'G06': [6, 8, 0, 1, 3, 9, 16, 20],
 'G07': [6, 8, 18, 4, 5, 0, 1, 3, 16, 20],
 'G08': [8, 28, 22, 15, 17, 14, 16, 21, 19, 24, 27],
 'G09': [12, 13, 15, 29, 14, 19, 24],
 'G10': [6, 8, 7, 15, 14, 19, 24],
 'G11': [22, 23, 15, 21, 19, 20, 24],
 'G12': [12, 13, 18, 28, 0, 1, 2, 3, 29, 30, 16, 31, 20, 24],
 'G13': [12, 13, 15, 29, 19, 24, 25],
 'G14': [12, 15, 29, 14, 19, 24],
 'G15': [6, 8, 28, 5, 16, 19, 20],
 'G16': [6, 8, 5, 7, 11, 15, 29, 14, 20, 24],
 'G17': [12, 13, 15, 29, 14, 19, 24, 25],
 'G18': [6, 8, 12, 13, 0, 9, 15, 29, 14, 19, 24, 25],
 'G19': [12, 15, 20, 24],
 'G20': [8, 12, 13, 15, 29, 19, 24, 25],
 'G21': [6, 8, 10, 4, 5, 9, 11, 15, 20, 24],
 'G22': [8, 10, 5, 7, 15, 29, 14, 20, 24],
 'G23': [8, 12, 15, 20],
 'G24': [6, 8, 12, 5, 7, 9, 15, 14, 20, 24],
 'G25': [6, 8, 4, 5, 7, 11, 15, 14, 20, 24],
 ICOCI. [10 10 1F 00 04 0F]
```

```
'G26': [12, 13, 15, 20, 24, 25],
'G27': [6, 8, 10, 12, 4, 5, 7, 9, 15, 20, 24],
'G28': [6, 8, 5, 0, 3, 9, 17, 16, 20, 27],
'G29': [12, 23, 15, 21, 19, 24],
'G30': [12, 15, 29, 14, 21, 19, 24],
'G31': [12, 13, 23, 15, 29, 21, 19, 24, 25],
'G32': [12, 22, 15, 21, 19, 24, 25],
'G33': [12, 13, 22, 23, 15, 29, 14, 21, 19, 24, 25],
'G34': [6, 8, 5, 0, 1, 2, 3, 17, 16, 20],
'G35': [8, 10, 28, 5, 16, 31, 20, 27],
'G36': [8, 10, 28, 4, 11, 15, 17, 16, 20, 27],
'G37': [6, 8, 18, 4, 5, 15, 30, 16, 20, 27],
'G38': [12, 15, 29, 14, 19, 24, 25],
'G39': [12, 22, 23, 15, 29, 21, 19, 24, 25],
'G40': [6, 8, 18, 28, 4, 7, 9, 15, 17, 16, 20, 27],
'G41': [8, 12, 13, 22, 15, 29, 14, 21, 19, 24, 25],
'G42': [12, 23, 15, 29, 14, 21, 19, 24],
'G43': [12, 13, 15, 21, 19, 24, 25],
'G44': [12, 15, 24, 25],
'G45': [23, 15, 21, 19, 20, 24],
'G46': [12, 13, 28, 15, 17, 29, 14, 16, 19, 24, 25],
'G47': [12, 15, 24],
'G48': [12, 0, 15, 29, 14, 24],
'G49': [12, 15, 29, 14, 24],
'G50': [8, 18, 28, 0, 2, 23, 17, 30, 16, 21, 20, 27],
'G51': [18, 26, 28, 16, 19],
'G52': [6, 8, 10, 12, 18, 28, 0, 2, 9, 16, 20, 25],
'G53': [12, 15, 14, 24, 25],
'G54': [12, 13, 15, 29, 14, 24],
'G55': [12, 15, 24, 25],
'G56': [6, 8, 18, 28, 0, 3, 9, 16, 20],
'G57': [12, 26, 19, 25],
'G58': [6, 8, 10, 28, 11, 16, 19, 24],
'G59': [6, 8, 4, 9, 11, 30, 16, 19, 24],
'G60': [8, 12, 13, 28, 16, 19, 20],
'G61': [8, 10, 18, 4, 5, 11, 17, 16, 19, 24],
'G62': [12, 15, 29, 14, 24],
'G63': [15, 14, 20, 24],
'G64': [12, 13, 15, 14, 19, 24],
'C65': [12 12 15 20 1/
```

```
עטט : [12, 13, 13, 29, 14, 19, 24, 23],
'G66': [12, 13, 15, 14, 19, 24, 25],
'G67': [15, 29, 21, 24],
'G68': [6, 8, 12, 5, 15, 19, 24],
'G69': [12, 13, 21, 19, 24, 25],
'G70': [12, 22, 21, 20, 24],
'G71': [12, 15, 16, 24, 25],
'G72': [0, 3, 15, 14, 16, 24],
'G73': [12, 18, 0, 1, 15, 14, 16, 24, 27],
'G74': [12, 13, 15, 16, 24],
'G75': [8, 4, 5, 0, 1, 2, 7, 9, 16, 20],
'G76': [6, 8, 0, 3, 16, 20],
'G77': [8, 4, 0, 1, 3, 9, 16, 20],
'G78': [6, 8, 4, 0, 3, 7, 9, 16, 20],
'G79': [6, 8, 18, 28, 0, 1, 16, 20],
'G80': [18, 0, 2, 17, 30, 16, 31, 20, 27],
'G81': [18, 28, 0, 17, 30, 16, 31, 20, 27],
'G82': [0, 3, 30, 16, 20, 27],
'G83': [18, 0, 17, 30, 16, 20]}
```

The quantity of the scrap type required determines how many grabs the crane has to do

```
total grabs dict = {'G01': 25, 'G02': 25, 'G03': 28, 'G04': 36, 'G05': 32,
                     'G06': 26, 'G07': 32, 'G08': 46, 'G09': 33, 'G10': 41,
                     'G11': 27, 'G12': 47, 'G13': 30, 'G14': 30, 'G15': 31,
                    'G16': 40, 'G17': 32, 'G18': 44, 'G19': 26, 'G20': 33,
                     'G21': 38, 'G22': 37, 'G23': 28, 'G24': 37, 'G25': 37,
                     'G26': 30, 'G27': 36, 'G28': 34, 'G29': 41, 'G30': 41,
                     'G31': 42, 'G32': 39, 'G33': 38, 'G34': 40, 'G35': 43,
                     'G36': 46, 'G37': 45, 'G38': 31, 'G39': 40, 'G40': 47,
                     'G41': 37, 'G42': 32, 'G43': 34, 'G44': 22, 'G45': 24,
                    'G46': 34, 'G47': 22, 'G48': 23, 'G49': 21, 'G50': 28,
                     'G51': 41, 'G52': 43, 'G53': 23, 'G54': 25, 'G55': 22,
                     'G56': 31, 'G57': 22, 'G58': 42, 'G59': 39, 'G60': 33,
                     'G61': 38, 'G62': 21, 'G63': 16, 'G64': 30, 'G65': 32,
                     'G66': 34, 'G67': 27, 'G68': 24, 'G69': 38, 'G70': 32,
                     'G71': 22, 'G72': 26, 'G73': 31, 'G74': 23, 'G75': 26,
                     'G76': 25, 'G77': 27, 'G78': 28, 'G79': 28, 'G80': 32,
```

```
'G81': 32, 'G82': 33, 'G83': 32}
```

Based on the real production plan, there is a maximum time available for the loading of each grade

Scrap types data

The layer of each scrap type

```
scrap_layer_dict = {6: 1.0, 8: 1.0, 10: 1.0, 12: 1.0, 13: 1.0, 18: 1.0, 26: 1.0, 28: 2.0, 4: 3.0, 5: 3.0, 0: 4.0, 1: 4.0, 2: 4.0, 3: 4.0, 7: 4.0, 9: 4.0, 11: 4.0, 22: 4.0, 23: 4.0, 15: 5.0, 17: 5.0, 29: 5.0, 30: 5.0, 14: 6.0, 16: 6.0, 21: 6.0, 31: 6.0, 19: 7.0, 20: 7.0, 24: 7.0, 25: 7.0, 27: 7.0}
```

✓ Production plan data

(Real) Production plan data

```
'G44', 'G44', 'G44', 'G67', 'G67', 'G67', 'G67',
                      'G67', 'G47', 'G47', 'G47', 'G47', 'G47', 'G11', 'G11',
                       'G11', 'G11', 'G11', 'G65', 'G65', 'G65']
jobs eaf2 list RPP = ['G11', 'G11', 'G11', 'G40', 'G40', 'G40', 'G11', 'G11',
                      'G11', 'G28', 'G28', 'G28', 'G09', 'G09', 'G09', 'G11',
                      'G11', 'G11', 'G07', 'G07', 'G07', 'G28', 'G28', 'G28',
                       'G07', 'G07', 'G78', 'G78', 'G78', 'G08', 'G08', 'G08',
                       'G47', 'G47', 'G78', 'G78', 'G78', 'G11', 'G11', 'G65',
                      'G65', 'G65'1
# Grades that appear in the real production plan
grades list RPP = ['G07', 'G08', 'G09', 'G11', 'G13', 'G28', 'G40', 'G44',
                    'G46', 'G47', 'G64', 'G65', 'G67', 'G78']
Leveled Production plan data (LPP)
jobs eaf1 list LPP = ['G40', 'G12', 'G08', 'G37', 'G35', 'G31', 'G29', 'G51',
                      'G59', 'G32', 'G33', 'G24', 'G25', 'G22', 'G46', 'G28',
                       'G66', 'G60', 'G82', 'G80', 'G42', 'G17', 'G07', 'G73',
                      'G15', 'G14', 'G26', 'G78', 'G79', 'G77', 'G11', 'G75',
                       'G72', 'G76', 'G54', 'G68', 'G74', 'G48', 'G55', 'G44',
                       'G49'1
jobs eaf2 list LPP = ['G36', 'G18', 'G52', 'G58', 'G30', 'G10', 'G16', 'G39',
                      'G34', 'G21', 'G61', 'G69', 'G41', 'G04', 'G27', 'G43',
                       'G20', 'G09', 'G65', 'G70', 'G81', 'G83', 'G05', 'G56',
                       'G38', 'G13', 'G64', 'G23', 'G50', 'G03', 'G67', 'G19',
                      'G06', 'G01', 'G02', 'G45', 'G53', 'G71', 'G57', 'G47',
                      'G62', 'G63']
# Complete list of grades
grades list LPP = ['G01', 'G02', 'G03', 'G04', 'G05', 'G06', 'G07', 'G08',
                    'G09', 'G10', 'G11', 'G12', 'G13', 'G14', 'G15', 'G16',
                   'G17', 'G18', 'G19', 'G20', 'G21', 'G22', 'G23', 'G24',
                    'G25', 'G26', 'G27', 'G28', 'G29', 'G30', 'G31', 'G32',
```

```
'G33', 'G34', 'G35', 'G36', 'G37', 'G38', 'G39', 'G40', 'G41', 'G42', 'G43', 'G44', 'G45', 'G46', 'G47', 'G48', 'G49', 'G50', 'G51', 'G52', 'G53', 'G54', 'G55', 'G56', 'G57', 'G58', 'G59', 'G60', 'G61', 'G62', 'G63', 'G64', 'G65', 'G66', 'G67', 'G68', 'G69', 'G70', 'G71', 'G72', 'G73', 'G74', 'G75', 'G76', 'G77', 'G78', 'G79', 'G80', 'G81', 'G82', 'G83']
```

Start coding or generate with AI.

✓ SPLITS

Split (0) - left / right split of boxes from the Layout 0 (for Layout 0 star)

```
split0star_left_scraps = sorted([26, 18, 13, 4, 1, 23, 22, 3, 15, 14, 31, 24, 19, 25])
split0star_right_scraps = sorted([10, 6, 8, 12, 28, 5, 2, 11, 7, 9, 0, 30, 17, 29, 16, 21, 20, 27])
```

Split (1) - optimized left/right split of scrap types based on the perfect balance between the total length of both sides of the yard

```
split1_left_scraps = [0, 2, 8, 9, 14, 17, 18, 20, 22, 24, 27, 30, 31]
split1_right_scraps = [1, 3, 4, 5, 6, 7, 10, 11, 12, 13, 15, 16, 19, 21, 23, 25, 26, 28, 29]
```

Split (2a) - optimized left/right split of scrap types based on:

- 1. balance between the total length of both sides of the yard;
- 2. balanced split for scraps of the layers in A.

```
split2a_left_scraps = [0, 3, 4, 5, 6, 7, 15, 16, 18, 19, 21, 22, 25, 26, 27]
split2a_right_scraps = [1, 2, 8, 9, 10, 11, 12, 13, 14, 17, 20, 23, 24, 28, 29, 30, 31]
```

Split (2b) - optimized left/right split of scrap types based on:

- 1. balanced split for scraps of the layers in A;
- 2. balance between the total length of both sides of the yard.

```
split2b_left_scraps = [0, 2, 4, 5, 7, 9, 11, 13, 16, 17, 18, 20, 21, 24, 26, 29, 30]
split2b_right_scraps = [1, 3, 6, 8, 10, 12, 14, 15, 19, 22, 23, 25, 27, 28, 31]
```

Split (3) - optimized left/right split of scrap types based on the balance between the total length of both sides of the yard with weight 0.5 and the balance between the split for scraps of layer 1, 4, 5, 6 and 7 with weight 0.5.

```
# alpha = 1.0
split3 10 left scraps = [0, 2, 8, 9, 14, 17, 18, 20, 22, 24, 27, 30, 31]
split3_10_right_scraps = [1, 3, 4, 5, 6, 7, 10, 11, 12, 13, 15, 16, 19, 21, 23, 25, 26, 28, 29]
# alpha = 0.9
split3 09 left scraps = [2, 7, 8, 9, 10, 11, 12, 13, 14, 17, 20, 23, 24, 28, 29, 30, 31]
split3 09 right scraps = [0, 1, 3, 4, 5, 6, 15, 16, 18, 19, 21, 22, 25, 26, 27]
# alpha = 0.8
split3 08 left scraps = [4, 5, 7, 11, 13, 16, 17, 18, 19, 21, 22, 23, 25, 26, 27, 29, 30]
split3 08 right scraps = [0, 1, 2, 3, 6, 8, 9, 10, 12, 14, 15, 20, 24, 28, 31]
# alpha = 0.7
split3_07_left_scraps = [4, 5, 7, 11, 13, 16, 17, 18, 19, 21, 22, 23, 25, 26, 27, 29, 30]
split3 07 right scraps = [0, 1, 2, 3, 6, 8, 9, 10, 12, 14, 15, 20, 24, 28, 31]
# alpha = 0.6
split3 06 left scraps = [0, 2, 4, 5, 9, 11, 13, 16, 17, 18, 20, 21, 23, 24, 26, 29, 30]
split3_06_right_scraps = [1, 3, 6, 7, 8, 10, 12, 14, 15, 19, 22, 25, 27, 28, 31]
```

```
# alpha = 0.5
split3 05 left scraps = [0, 2, 6, 8, 9, 10, 11, 12, 14, 15, 20, 23, 24, 28, 31]
split3 05 right scraps = [1, 3, 4, 5, 7, 13, 16, 17, 18, 19, 21, 22, 25, 26, 27, 29, 30]
\# alpha = 0.4
split3 04 left_scraps = [6, 7, 8, 10, 11, 12, 14, 15, 19, 22, 23, 25, 27, 28, 31]
split3_04_right_scraps = [0, 1, 2, 3, 4, 5, 9, 13, 16, 17, 18, 20, 21, 24, 26, 29, 30]
# alpha = 0.3
split3 03 left scraps = [4, 5, 7, 11, 13, 16, 17, 18, 19, 21, 22, 23, 25, 26, 27, 29, 30]
split3_03_right_scraps = [0, 1, 2, 3, 6, 8, 9, 10, 12, 14, 15, 20, 24, 28, 31]
\# alpha = 0.2
split3 02 left scraps = [6, 7, 8, 10, 11, 12, 14, 15, 19, 22, 23, 25, 27, 28, 31]
split3_02_right_scraps = [0, 1, 2, 3, 4, 5, 9, 13, 16, 17, 18, 20, 21, 24, 26, 29, 30]
\# alpha = 0.1
split3 01 left scraps = [0, 1, 2, 6, 8, 9, 10, 12, 14, 15, 20, 23, 24, 28, 31]
split3 01 right scraps = [3, 4, 5, 7, 11, 13, 16, 17, 18, 19, 21, 22, 25, 26, 27, 29, 30]
# alpha = 0.0
split3 00 left scraps = [0, 2, 4, 5, 9, 11, 13, 15, 16, 18, 20, 21, 23, 24, 26, 28]
split3 00 right scraps = [1, 3, 6, 7, 8, 10, 12, 14, 17, 19, 22, 25, 27, 29, 30, 31]
# Function to set left scraps and right scraps according to the split
def get scraps(split):
    left var name = f"{split} left scraps"
```

```
right_var_name = f"{split}_right_scraps"

# Fallback if split is not recognized
if left_var_name not in globals() or right_var_name not in globals():
    left_var_name = split3_05_left_scraps
    right_var_name = split3_05_right_scraps
    print('Error! Using Split 3 0.5 as default')

left_scraps = globals()[left_var_name]
right_scraps = globals()[right_var_name]
return left_scraps, right_scraps
```

Start coding or generate with AI.

✓ LAYER PERMUTATION

```
laver 1 = [key for key in scrap layer dict.keys() if scrap layer dict[key] == 1.0]
layer 2 = [key for key in scrap layer dict.keys() if scrap layer dict[key] == 2.0]
layer 3 = [key for key in scrap layer dict.keys() if scrap layer dict[key] == 3.0]
layer 4 = [key for key in scrap layer dict.keys() if scrap layer dict[key] == 4.0]
layer 5 = [key for key in scrap layer dict.keys() if scrap layer dict[key] == 5.0]
layer 6 = [key for key in scrap layer dict.keys() if scrap layer dict[key] == 6.0]
layer 7 = [key for key in scrap layer dict.keys() if scrap layer dict[key] == 7.0]
#print(layer 1)
#print(layer 2)
#print(layer 3)
#print(layer 4)
#print(layer 5)
#print(layer 6)
#print(layer 7)
layer 1 perms = list(permutations(layer 1))
layer 2 perms = list(permutations(layer 2))
layer 3 perms = list(permutations(layer 3))
laver 4 perms = list(permutations(laver 4))
```

```
layer 5 perms = list(permutations(layer 5))
layer 6 perms = list(permutations(layer 6))
layer 7 perms = list(permutations(layer 7))
#layer 1 perms
perms = [layer 1 perms, layer_2_perms, layer_3_perms, layer_4_perms, layer_5_perms, layer_6_perms, layer_7_perms]
Function to get recipe out of a permutation for all layers
def get recipe(grade, sigma):
    # Input: a grade (eg. 'G07') and a sequence of all scraps in each layer
    # Output: the recipe for the grade using the sequences
    ingredients = grade ingredients dict[grade]
    recipe = [scrap for scrap in sigma[0] if scrap in ingredients]
    recipe += [scrap for scrap in sigma[1] if scrap in ingredients]
    recipe += [scrap for scrap in sigma[2] if scrap in ingredients]
    recipe += [scrap for scrap in sigma[3] if scrap in ingredients]
    recipe += [scrap for scrap in sigma[4] if scrap in ingredients]
    recipe += [scrap for scrap in sigma[5] if scrap in ingredients]
    recipe += [scrap for scrap in sigma[6] if scrap in ingredients]
    return recipe

    ✓ Layout

def get precedences(scraps):
    precedences = []
    for i in scraps:
      for j in scraps:
        if x[i.il.X == 1:
```

```
±1 (1,±1),1(
          precedences.append(f'[{i},{j}]')
    return precedences
def print row(scraps, precedences):
   aux = []
   for i in sorted(scraps):
     for j in sorted(scraps):
       if f'[{i},{j}]' in precedences:
          aux.append(i)
    row = []
   for k in range(len(scraps)):
     for i in sorted(scraps):
       if aux.count(i) == k:
          row.append(i)
    return row
  Yard total length
def compute side length(side):
   length = 20*2 + 1.7
   for scrap in side:
     length += box_width_dict[scrap] + 1.7
    return length
def compute yard length(L, R):
    return max(compute side length(L), compute side length(R))
```

Loading time for the production plan

```
def compute midpoints(L, R):
   midpoints = {}
   L aux = L.copy()
   L aux.reverse()
   midpoint = 20 + 1.7 + box_width_dict[L_aux[0]]/2
   midpoints[L aux[0]] = midpoint
   for i in range(1,len(L aux)):
      midpoint += box width dict[L aux[i-1]]/2 + 1.7 + box width dict[L aux[i]]/2
      midpoints[L aux[i]] = midpoint
   R aux = R.copy()
   R aux.reverse()
   midpoint = 20 + 1.7 + box width dict[R aux[0]]/2
   midpoints[R aux[0]] = midpoint
   for i in range(1,len(R aux)):
      midpoint += box width dict[R aux[i-1]]/2 + 1.7 + box width dict[R aux[i]]/2
     midpoints[R aux[i]] = midpoint
    return midpoints
def get grade loading time(grade, sigma, L, R):
  recipe = get recipe(grade, sigma)
  total grabs = total grabs dict[grade]
  midpoint = compute midpoints(L,R)
  time = 6.2 + 2*1.47 + 0.67*total grabs + (midpoint[recipe[0]] + midpoint[recipe[-1]])/60
  for i in range(len(recipe)-1):
   time += abs(midpoint[recipe[i]]-midpoint[recipe[i+1]])/40
  return time
def get eaf loading time(prodplan, sigma, L, R):
    time = 0
    for grade in produlant
```

```
time += get_grade_loading_time(grade, sigma, L, R)
return time

def get_prod_plan_loading_time(prodplan1, prodplan2, sigma, L, R):
    return max(get_eaf_loading_time(prodplan1, sigma, L, R), get_eaf_loading_time(prodplan2, sigma, L, R))

Start coding or generate with AI.
```


This is the model to be run in each iteration of the simulated annealing. For each grade, there is a single recipe to consider.

✓ Sets

S is the set of scrap types

 ${\cal L}$ is the set of scraps on the left side of the scrap yard

R is the set of scraps on the right side of the scrap yard

G is the set of grades

P is the sequence of jobs in EAF1

Q is the sequence of jobs in EAF2

∨ Parameters

- ullet For each scrap type $s\in S$ we are given the width of the box containing the scrap, w_s .
- ullet For each grade $g\in G$ we are given a recipe, z_q .

- ullet For each grade $g\in G$ we are given the total number of grabs required to load the necessary quantities, n_q .
- ullet (ONLY FOR REAL PROD PLAN) For each grade $g\in G$ we are given the maximum time allowed for the loading of the bucket, r_q (in ms).
- ullet For each job $p\in P$ in EAF1 we are given the corresponding grade g_p .
- ullet For each job $q\in Q$ in EAF2 we are given the corresponding grade h_q .

∨ Variables

For each scrap type $s \in S$:

• m_s is a non-negative continuous variable describing the midpoint of the box containing s, starting at the entry of the scrap yard closer to the EAFs.

For each pair of scrap types $s_1, s_2 \in S$:

- x_{s_1,s_2} is a binary variable that equals 1 iff s_1 and s_2 are both on the left or both on the right side of the scrap yard and scrap type s_1 is closer to the EAFs that s_2 ;
- d_{s_1,s_2} is a non-negative continuous variable describing the distance between m_{s_1} and m_{s_2} (regardless of their being or not in the same side of the scrap yard).

For each grade $g \in G$:

• t_g is a non-negative continuous variable describing the time it takes to have the bucket loaded with z_g ready at the EAF, including the unloading of the previous mixture.

And also:

- ullet U is a non-negative continuous variable describing the total time taken to load all grades bound to EAF1;
- ullet V is a non-negative continuous variable describing the total time taken to load all grades bound to EAF2;
- ullet W is a non-negative continuous variable describing the total time taken to load the whole production plan.

∨ Constraints

• Fach midpoint m_s is given by (in meters):

- Laon inaponit n_{s} is given by (in ineters).

$$m_s = 20 + 1.7 + \Big(\sum_{s^*=0}^{31} (w_{s^*} + 1.7) x_{s^*,s}\Big) + rac{w_s}{2} \,, \quad orall \, s \in S_s \,.$$

• Given any two scrap types on the same side of the scrap yard, exactly one sits closer to the EAFs:

$$egin{aligned} x_{s_1,s_2} + x_{s_2,s_1} &= 1 \,, & orall \, s_1, s_2 \in L \ x_{s_1,s_2} + x_{s_2,s_1} &= 1 \,, & orall \, s_1, s_2 \in R \end{aligned}$$

• No scrap type preceeds itself:

$$x_{s,s}=0\,,\quadorall\,s\in S$$

• Given any two scrap types on different sides of the scrap yard, no one preceeds the other:

$$egin{aligned} x_{s_1,s_2} &= 0 \,, & orall \, s_1 \in L, s_2 \in R \ x_{s_1,s_2} &= 0 \,, & orall \, s_1 \in R, s_2 \in L \end{aligned}$$

Variables x are transitive:

$$egin{aligned} x_{s_1,s_2} &= x_{s_2,s_3} = 1 \Rightarrow x_{s_1,s_3} = 1\,, &orall \, s_1,s_2,s_3 \in L \ x_{s_1,s_2} &= x_{s_2,s_3} = 1 \Rightarrow x_{s_1,s_3} = 1\,, &orall \, s_1,s_2,s_3 \in R \end{aligned}$$

The distance between any two scrap types:

$$d_{s_1,s_2} = \left| m_{s_1} - m_{s_2}
ight|, \quad orall \, s_1,s_2 \in S$$

ullet The time necessary to load a grade $g\in G$ into the bucket (incluinding the unloading of the previous grade) is given by (in minutes):

$$t_g = 6.2 + 1.47 imes 2 + 0.67 n_g + rac{m_{z_g[0]} + m_{z_g[-1]}}{60} + \sum_{i=0}^{\mathrm{len}(z_g)-2} rac{d_{z_g[i],z_g[i+1]}}{40} \,, \quad orall \, g \in G_i \,.$$

ullet (ONLY FOR REAL PROD PLAN) The time necessary to load a grade $g\in G$ into the bucket cannot exceed the maximum time allowed:

$$t_g \leq rac{r_g}{1000} \,, \quad orall \, g \in G \,.$$

• The total time it takes to load all grades in the production plan:

$$U = \sum_{p \in P} t_{g_p} \ V = \sum_{q \in Q} t_{h_q}$$

The variable to minimize:

$$W \geq U$$

∨ Objective function

The objective is to minimize the total time taken to produce all the grades in the production plan. This can be stated as $\min W$

Start coding or generate with AI.


```
!pip install gurobipy # install gurobipy, if not already installed
import gurobipy as gp # import the installed package
    Requirement already satisfied: qurobipy in /usr/local/lib/python3.11/dist-packages (12.0.2)
from gurobipy import *
from gurobipy import GRB # explicitly import GRB from gurobipy
# Create an environment with your WLS license
params = {
"WLSACCESSID": '
"WLSSECRET": '
"LICENSEID":
env = qp.Env(params=params)
# Create the model within the Gurobi environment
model = gp.Model(env=env)
    Set parameter WLSAccessID
    Set parameter WLSSecret
    Set parameter LicenseID to value
```

Start coding or generate with AI.

▼ MODEL IMPLEMENTATION & SIMULATED ANNEALING

```
%%skip
k = random.randint(1, 5000)
random.seed(k)
k = 4251
random.seed(k)
```

Chosing the neighbour

Neighbour functions considered:

- **v1** Chooses 1 layer in σ , chooses 2 scraps in that layer and swaps their boxes
- **v2** Chooses 1 layer in σ and replaces the entire layer permutation for another
- **v3** Chooses 2 layers in σ , chooses 2 scraps in each and swaps their boxes
- **v4** Chooses 2 layers in σ and swaps their entire permutation for another
- **v5** Chooses n layers in σ , chooses 2 scraps in each and swaps their boxes
- **v6** Chooses n layers in σ and swaps their entire permutation for another
- # Function to choose 2 scraps (within same layer) and swap them in sigma
 def choose_and_swap(layer):
 - # Make copy as a list to allow modification

```
new layer perm = list(sigma[layer-1])
    # Pick two different scraps in the layer
    scrap1 = random.choice(sigma[layer-1])
    scrap2 = random.choice(sigma[layer-1])
    while scrap2 == scrap1:
        scrap2 = random.choice(sigma[layer-1])
    # Swap them
    new layer perm = [scrap2 if x == scrap1 else scrap1 if x == scrap2 else x for x in new layer perm]
    return new_layer_perm
# Function to choose new permutation of a given layer
def choose new perm(layer):
    # Pick random permutation in layer
    new perm = random.choice(perms[layer-1])
    while new perm == sigma[layer-1]:
        new perm = random.choice(perms[layer-1])
    # Return the new permutation
    return new perm
# v1 Chooses 1 layer and swaps 2 scraps in that layer
def get neighbour v1(sigma):
   # Make copy
    new sigma = sigma.copy()
    # Pick random layer
    i = random.choice([1,3,4,5,6,7])
    # Pick two different scraps in the chosen layer
    scrap1 = random.choice(sigma[i-1])
    scrap2 = random.choice(sigma[i-1])
    while scrap2 == scrap1:
        scrap2 = random.choice(sigma[i-1])
    # Swap them
```

```
new sigma[i-1] = [scrap2 if x == scrap1 else scrap1 if x == scrap2 else x for x in sigma[i-1]]
    return new sigma
# v2 Chooses 1 layer and replaces the layer's permutation for another
def get neighbour v2(sigma):
    # Make copy
    new sigma = sigma.copy()
    # Pick random layer
    i = random.choice([1,3,4,5,6,7])
    # Pick random permutation in layer i
    new layer perm = random.choice(perms[i-1])
    while new_layer_perm == sigma[i-1]:
        new layer perm = random.choice(perms[i-1])
    # Replace old layer i perm by new layer i perm in sigma
    new sigma[i-1] = new layer perm
    return new sigma
# v3 Chooses 2 layers and swaps 2 scraps in each
def get neighbour v3(sigma):
    # Make copy
    new sigma = sigma.copy()
    # Pick two different random layers
    i = random.choice([1,3,4,5,6,7])
    j = random.choice([1,3,4,5,6,7])
    while j == i:
        j = random.choice([1,3,4,5,6,7])
    # Swap scraps in chosen layers
    new sigma[i-1] = tuple(choose and swap(i))
    new_sigma[j-1] = tuple(choose_and_swap(j))
```

```
return new sigma
# v4 Chooses 2 layers and swaps its permutation for another
def get_neighbour_v4(sigma):
    # Make copy
    new sigma = sigma.copy()
    # Pick two different random layers
    i = random.choice([1,3,4,5,6,7])
    j = random.choice([1,3,4,5,6,7])
    while i == i:
        j = random.choice([1,3,4,5,6,7])
    # Swap scraps in chosen layers
    new sigma[i-1] = tuple(choose new perm(i))
    new sigma[j-1] = tuple(choose new perm(j))
    return new_sigma
# v5 Chooses n layers to be modified and swaps 2 scraps in each
def get neighbour v5(sigma):
    # Make copy
    new sigma = sigma.copy()
    # Pick the number of layers which will be changed
    n = random.randint(1, 6)
    print(n)
    # Pick n different random layers
    layers = random.sample([1,3,4,5,6,7], n)
    print(layers)
    # Swap scraps in chosen layers
    for i in layers:
        new sigma[i-1] = tuple(choose and swap(i))
```

```
return new sigma
# v6 Chooses n layers to be modified and swaps their permutation for another
def get neighbour v6(sigma):
    # Make copy
    new sigma = sigma.copy()
    # Pick the number of layers which will be changed
    n = random.randint(1, 6)
    print(n)
    # Pick n different random layers
    layers = random.sample([1,3,4,5,6,7], n)
    print(layers)
    # Swap scraps in chosen layers
    for i in layers:
        new sigma[i-1] = tuple(choose new perm(i))
    return new sigma
# v7 Chooses n»2 layers to be modified and swaps their permutation for another
def get neighbour v7(sigma):
    # Make copy
    new sigma = sigma.copy()
    # Pick the number (at least 2) of layers which will be changed
    n = random.randint(2, 6)
    print(n)
    # Pick n different random layers
    layers = random.sample([1,3,4,5,6,7], n)
    print(layers)
    # Swap scraps in chosen layers
```

```
for i in layers:
    new_sigma[i-1] = tuple(choose_new_perm(i))
return new sigma
```

✓ Implementing & runing the model

```
def run model(sigma, time limit, left scraps, right scraps, grades list, jobs eaf1 list, jobs eaf2 list):
   global x
   model.reset()
   # OPTIONAL: Limit each iteration to time limit seconds
   #model.setParam("TimeLimit", time limit)
   # Sets
   L = left scraps # Use the passed left scraps argument
   R = right scraps # Use the passed right_scraps argument
   S = sorted(left scraps + right scraps)
   G = grades list
   P = list(range(len(jobs eaf1 list)))
   Q = list(range(len(jobs eaf2 list)))
   # Parameters
   box width = {s:box width dict[s] for s in S}
   recipes = {q:qet recipe(q, sigma) for q in G}
   total grabs = {q:total grabs dict[q] for q in G}
   # Comment for LPP:
   max time = {g:grades max time dict[g]/1000 for g in G}
   jobs eaf1 = dict(zip(list(range(len(jobs eaf1 list))), jobs eaf1 list))
   jobs eaf2 = dict(zip(list(range(len(jobs eaf2 list))), jobs eaf2 list))
   # Variables
   midpoint = model.addVars(S, name="midpoint")
   x = model.addVars(S, S, vtype=GRB.BINARY, name="x")
   aux = model.addVars(S, S, lb=-gp.GRB.INFINITY, name="aux")
   dist = model.addVars(S, S, name="dist")
```

```
timetoready = model.addVars(G, name="timetoready")
U = model.addVar(name="U")
V = model.addVar(name="V")
W = model.addVar(name="W")
# Constrains
model.addConstrs((x[i,j] + x[j,i] == 1 for i in L for j in L if j != i), name="sides1a")
model.addConstrs((x[i,j] + x[j,i] == 1 for i in R for j in R if j != i), name="sides1b")
model.addConstr((sum(x[i,i] for i in S) == 0), name="sides2")
model.addConstrs((x[i,j] == 0 for i in L for j in R), name="sides3a")
model.addConstrs((x[i,j] == 0 for i in R for j in L), name="sides3b")
model.addConstrs((x[i,k] >= 1 - 10*(1-x[i,j]) - 10*(1-x[j,k]) for i in L for j in L for k in L), name="sides4a")
model.addConstrs((x[i,k] >= 1 - 10*(1-x[i,j]) - 10*(1-x[j,k]) for i in R for j in R for k in R), name="sides4b")
model.addConstrs((midpoint[s] == 20 + 1.7 + sum((box width[y] + 1.7)*x[y,s] for y in S) + box width[s]/2
    for s in S), name="midpoints")
for i in S:
    for j in S:
        model.addConstr(aux[i, j] == midpoint[i] - midpoint[j], name=f'distanceaux {i} {j}')
        model.addConstr(dist[i,j] == abs (aux[i,j]), name=f'distance {i} {j}')
# Comment for LPP:
model.addConstrs((timetoready[q] <= max time[q] for q in G), name="maxtime")</pre>
model.addConstrs((timetoready[q] ==
    (6.2 + 2*1.47 + 0.67*total grabs[q] + (midpoint[recipes[q][0]] + midpoint[recipes[q][-1]])/60
     + sum( dist[recipes[q][i],recipes[q][i+1]]
    for i in range(len(recipes[g])-1))/40) for g in G), name="time")
model.addConstr((U == sum( timetoready[jobs eaf1[p]] for p in P)), name="totaltime1")
model.addConstr((V == sum( timetoready[jobs eaf2[q]] for q in Q)), name="totaltime2")
model.addConstr((U <= W), name = "totaltimeW1")</pre>
model.addConstr((V <= W), name = "totaltimeW2");</pre>
# Objective function
model.setObjective(W, GRB.MINIMIZE)
# Run model
model.optimize()
# do IIS if the model is infeasible
if model.Status == GRB.INFEASIBLE:
    model.computeIIS()
```

```
# Output results
new_t = W.X
new_output = model.getVars()

print(f'Sigma: {sigma}')
print(f'Time: {new_t}')

left_precedences = get_precedences(left_scraps)
new_left_row = print_row(left_scraps, left_precedences)
#print(f'Left row: {new_left_row}')
right_precedences = get_precedences(right_scraps)
new_right_row = print_row(right_scraps, right_precedences)
#print(f'Right row: {new_right_row}')

return new_t, new_output, new_left_row, new_right_row
```

Making the decision

```
def get decision(current t, current sigma, current output, current left row, current right row,
                 new t, new sigma, new output, new left row, new right row, beta, step):
    if new t < current t:</pre>
        current t = new t
        current sigma = new sigma
        current output = new output
        current left row = new left row
        current right row = new right row
        print('New best solution found!')
        print(f'New left row: {current left row}')
        print(f'New right row: {current right row}')
    else:
        p = random.random()
        if p < math.exp((current t - new t)/5*(1+beta*step)):</pre>
            current t = new t
            current sigma = new sigma
            current output = new output
            current left row = new left row
```

```
current_right_row = new_right_row
print('p update!')
print(f'New left row: {current_left_row}')
print(f'New right row: {current_right_row}')
else:
print('No update!')
#pass
return current_t, current_sigma, current_output, current_left_row, current_right_row
```

✓ Simulated Annealing algorithm

```
currentWs = []
newWs = []
def simulated annealing(prod plan, split, n iterations, time limit, neighbour fn, beta, sigma):
   # Prod plan
   if prod plan == 'RPP':
       grades list = grades list RPP
       jobs eaf1 list = jobs eaf1 list RPP
       jobs eaf2 list = jobs eaf2 list RPP
    else:
       grades list = grades list LPP
       jobs eaf1 list = jobs eaf1 list LPP
       jobs eaf2 list = jobs eaf2 list LPP
   # Split
   left scraps, right_scraps = get_scraps(split)
   # Initial sigma
   current sigma = sigma
    # Intial solution
   current_t, current_output, current_left_row, current_right_row = run_model(current_sigma, time_limit,
                                                                              left_scraps, right_scraps,
```

```
grades list, jobs eatl list, jobs eat2 list)
currentWs.append(current t)
newWs.append(current t)
print(f'Left row: {current left row}')
print(f'Right row: {current right row}')
for i in range(n iterations):
    print(f'\nIteration {i}')
   # Neighbout fn
    if neighbour fn == 'v1':
      new sigma = get neighbour_v1(current_sigma)
   elif neighbour fn == 'v2':
      new sigma = get neighbour v2(current sigma)
    elif neighbour fn == 'v3':
      new sigma = get neighbour v3(current sigma)
    elif neighbour fn == 'v4':
      new sigma = get_neighbour_v4(current_sigma)
   elif neighbour fn == 'v5':
      new sigma = get neighbour v5(current sigma)
    elif neighbour fn == 'v6':
      new sigma = get neighbour v6(current sigma)
    else:
      new sigma = get neighbour v7(current sigma)
   new t, new output, new left row, new right row = run model(new sigma, time_limit, left_scraps, right_scraps,
                                                               grades list, jobs eaf1 list, jobs eaf2 list)
    print(f'Current W: {current t}')
    print(f'New W: {new t}')
    print(f'Current sigma: {current sigma}')
    print(f'New sigma: {new sigma}')
    print(f'Current left row: {current left row}')
    print(f'New left row: {new left row}')
    print(f'Current right row: {current right row}')
    print(f'New right row: {new right row}')
    current_t, current_sigma, current_output, current_left_row, current_right_row = get_decision(current_t,
```

```
currentWs.append(current_t)
    newWs.append(new_t)
    print(f'Current W: {current_sigma}')
    print(f'Current sigma: {current_sigma}')
    print(f'Current left row: {current_left_row}')
    print(f'Current right row: {current_right_row}')

return current_t, current_sigma, current_output, current_left_row, current_right_row

Start coding or generate with AI.
```

∨ SA parameters

```
prod_plan = 'RPP'  # RPP / LPP
split = 'split3_05'  # split0 / split1 / split2a / split2b / split3_xx
n_iterations = 250
time_limit = None  # OPTIONAL; in seconds
beta = 0.05
neighbour_fn = 'v5'  # v1 / v2 / v3 / v4 / v5 / v6

# Layer permutations in increasing order
sigma0 = [perms[i][0] for i in range(7)]

# Random inital sigma
sigma = [random.choice(perms[i]) for i in range(7)]
```

current_sigma,
current_output,
current_left_row,
current_right_row,
new_t,
new_sigma,
new_output,
new_left_row,
new_right_row,
beta,
i)

```
start time = datetime.now()
# run SA
final t, final sigma, final output, final left row, final right row = simulated annealing(prod plan,
                                                                                           split,
                                                                                           n iterations,
                                                                                           time limit,
                                                                                           neighbour fn,
                                                                                           beta,
                                                                                           sigma)
    Streaming output truncated to the last 5000 lines.
       208
                                     3344.9095833 3094.22197 7.49%
                                                                       129
                                                                             22s
    Н
             148
       234
             151
                                     3337.2220833 3094.22197 7.28%
                                                                       132
                                                                             22s
       234
                                     3328.3345833 3094.22197 7.03%
                                                                             22s
             128
                                                                       132
             124
                                                                             22s
       234
                                     3326.5795833 3094.22197
                                                              6.98%
                                                                       132
       234
             123
                                     3324.8245833 3094.22197 6.94%
                                                                       132
                                                                             22s
       260
             124
                                     3314.2812500 3098.46493
                                                              6.51%
                                                                       141
                                                                             23s
       324
             147
                                     3310.7712500 3108.89122 6.10%
                                                                       144
                                                                             24s
    H 325
                                     3306.0462500 3108.89122
             145
                                                              5.96%
                                                                       144
                                                                             24s
                      cutoff
                                       3306.04625 3112.17611 5.86%
       361
             159
                               13
                                                                       143
                                                                             25s
       766
             207
                      cutoff
                                7
                                       3306.04625 3204.84847 3.06%
                                                                       144
                                                                             30s
    H 1021
             223
                                     3306.0462497 3227.82040 2.37%
                                                                       141
                                                                             33s
                                   143 3306.04625 3237.91008 2.06%
      1141
             225 3303.49702
                                                                       141
                                                                             35s
                                       3306.04625 3273.27958 0.99%
      1635
             160
                      cutoff
                               39
                                                                       131
                                                                             40s
    Cutting planes:
      Gomory: 1
      Cover: 7
      MIR: 52
      Flow cover: 6
      Inf proof: 6
    Explored 1858 nodes (234697 simplex iterations) in 41.47 seconds (23.89 work units)
```

Thread count was 2 (of 2 available processors)

```
Solution count 10: 3306.05 3306.05 3310.77 ... 3352.75
Optimal solution found (tolerance 1.00e-04)
Best objective 3.306046249669e+03, best bound 3.305785499071e+03, gap 0.0079%
Time: 3306.0462496692694
Current W: 3288.2562499999945
New W: 3306.0462496692694
Current sigma: [(26, 18, 8, 12, 13, 6, 10), (28,), (5, 4), (2, 1, 9, 0, 3, 11, 7, 23, 22), (17, 29, 15, 30), (16, 21, 14,
New sigma: [(26, 18, 8, 12, 13, 6, 10), (28,), (5, 4), (2, 1, 9, 0, 3, 11, 7, 23, 22), (15, 29, 30, 17), (16, 21, 14, 31),
Current left row: [2, 11, 10, 31, 8, 6, 9, 0, 28, 20, 14, 24, 15, 12, 23]
New left row: [2, 10, 11, 31, 8, 6, 9, 0, 28, 20, 14, 24, 15, 12, 23]
Current right row: [30, 26, 18, 5, 4, 1, 3, 7, 17, 16, 27, 25, 19, 21, 29, 13, 22]
New right row: [30, 26, 18, 5, 4, 1, 3, 7, 17, 16, 27, 25, 19, 29, 21, 13, 22]
No update!
Current W: 3288.2562499999945
Current sigma: [(26, 18, 8, 12, 13, 6, 10), (28,), (5, 4), (2, 1, 9, 0, 3, 11, 7, 23, 22), (17, 29, 15, 30), (16, 21, 14,
Current left row: [2, 11, 10, 31, 8, 6, 9, 0, 28, 20, 14, 24, 15, 12, 23]
Current right row: [30, 26, 18, 5, 4, 1, 3, 7, 17, 16, 27, 25, 19, 21, 29, 13, 22]
Iteration 207
3
[3, 7, 1]
Discarded solution information
Gurobi Optimizer version 12.0.2 build v12.0.2rc0 (linux64 - "Ubuntu 22.04.4 LTS")
CPU model: Intel(R) Xeon(R) CPU @ 2.20GHz, instruction set [SSE2|AVX|AVX2]
Thread count: 1 physical cores, 2 logical processors, using up to 2 threads
Academic license 2619152 - for non-commercial use only - registered to fi @isel.pt
Optimize a model with 2167121 rows, 652289 columns and 6183265 nonzeros
Model fingerprint: 0xe6ffd3fa
Model has 214016 simple general constraints
```

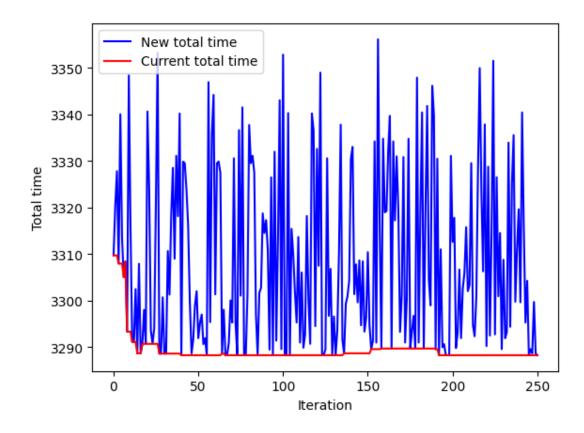
Start coding or <u>generate</u> with AI.

∨ SA results

```
end_time = datetime.now()
runtime = (end time - start time).total seconds()
```

```
print('Runtime (sec): {}'.format(runtime))
    Runtime (sec): 9147.083473
print(f'Prod plan: {prod plan}')
print(f'Split: {split}')
print(f'Initial sigma: sigma0')
                                                       # sigma0 / random
if n iterations != 0:
   print(f'Number of iterations: {n iterations}')
   print(f'Time limit: {time limit}')
   print(f'beta: {beta}')
   print(f'Neighbiour fn: {neighbour fn}')
   print(f'Seed: {k}')
    Prod plan: RPP
    Split: split3 05
    Initial sigma: sigma0
    Number of iterations: 250
    Time limit: None
    beta: 0.05
    Neighbiour fn: v5
    Seed: 4251
print(f'Final W: {final t}')
print(f'Final sigma: {final sigma}')
print(f'Final left row: {final left row}')
print(f'Final right row: {final right row}')
    Final W: 3288.2562499999954
    Final sigma: [(26, 18, 8, 12, 13, 6, 10), (28,), (5, 4), (2, 1, 9, 0, 3, 11, 7, 23, 22), (17, 29, 15, 30), (16, 21, 14, 31)
    Final left row: [2, 10, 11, 31, 8, 6, 9, 0, 28, 20, 14, 24, 15, 12, 23]
    Final right row: [26, 30, 18, 5, 4, 1, 3, 7, 17, 16, 27, 25, 19, 21, 29, 13, 22]
print(f'currentWs = {currentWs}')
print(f'newWs = {newWs}')
    currentWs = [3309.701250000001, 3309.701250000001, 3309.701250000001, 3307.94625, 3307.94625, 3307.94625, 3305.03458333332
    newWs = [3309.701250000001, 3320.332500000001, 3327.79125, 3307.94625, 3340.0187499999843, 3313.4062499999977, 3305.034583
```

```
xs = [x for x in range(len(currentWs))]
plt.plot(xs, newWs, 'b')
plt.plot(xs, currentWs, 'r')
plt.legend(['New total time', 'Current total time'])
plt.xlabel('Iteration')
plt.ylabel('Total time')
plt.show()
# Make sure to close the plt object once done
plt.close()
```



Start coding or <u>generate</u> with AI.